

# Simulation of thermal field dynamics in the erected reinforced concrete structure

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**Abstract.** During the heat treatment of concrete, temperature field in the structure can be controlled by changing the initial concrete temperature, the heating power of the heating elements, and heat transfer conditions at the surface of the structure. There is the task of finding such heat treatment mode in which the temperature field has the desired characteristics. These characteristics include temperature, rate of rise and temperature gradient. The first step in the solution of the heat treatment operation problem is to create a sufficient point of a mathematical model of the temperature field in the hardening concrete. The second stage should be devoted to the numerical solution of the equations of the model, which allows a computer to determine the temperature field in hardening concrete structure. With this method, you can use a computer to study the dynamics of the temperature field at various modes of heat treatment and to develop the most rational modes without the need for a large series of scientific experiments. For the numerical solution of model equations, a locally one-dimensional scheme of the method of full approximation is applied. This scheme is economical, relatively simple to program, does not require a lot of memory, and allows performing calculations on a computer.

## 1 Introduction

During the heat treatment of concrete, temperature field in the structure can be controlled by changing the initial concrete temperature, the heating power of the heating elements and heat transfer conditions at the surface of the structure [1-3]. There is the task of finding such heat treatment mode, in which the temperature field has the desired characteristics. These characteristics include temperature, rate of rise and temperature gradient [16, 20].

The first step in the solution of the heat treatment operation the problem is to create a sufficient point of a mathematical model of the temperature field in the hardening concrete.

The second stage should be devoted to the numerical solution of the equations of the model, which allows a computer to determine the temperature field in hardening concrete structure. With this method, you can use the computer to study the dynamics of the temperature field at various modes of heat treatment and to develop the most rational modes, without the need for a large series of scientific experiments. For the numerical solution of the model equations applied locally one-dimensional scheme (VOC) total

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approximation method [5]. This scheme is economical, relatively simple to program [5] does not require a lot of memory, allowing you to perform calculations on a computer.

## 2 Methods

Replacing the three-dimensional heat equation chain-dimensional equations.

We introduce in G bound grid with steps  $h_p$ , formed by three families of the  $G_p$  straight, parallel to the coordinate axes  $x_p$ , division points  $P = 1, 2, 3$ . Let's consider the problem on the segment  $[0, t_0]$  and divide it by division points

$$t_j = (j - 1)\tau; j = 1, \dots, j_0, \tau = \frac{t_0}{j_0}.$$

At each interval  $(t_0; t_{j+1})$  three-dimensional heat equation we replace the chain-dimensional equations

$$\frac{1}{3} c \frac{\partial u_p}{\partial t} = L_p u_p + f_p \text{ when } t_x + \frac{P-1}{3} \tau \leq t_j + \frac{P}{3} \tau$$

along all lines

$$G_p, P = 1, 2, 3, \sum_{p=1}^3 f_p = f$$

with the initial conditions

$$u_1(\vec{x}, t_j) = u(\vec{x}, t_j); u_2\left(\vec{x}, t_j + \frac{1}{3}\tau\right) = u_1\left(\vec{x}, t_j + \frac{1}{3}\tau\right);$$

$$u_3\left(\vec{x}, t_j + \frac{2}{3}\tau\right) = u_2\left(\vec{x}, t_j + \frac{2}{3}\tau\right).$$

The boundary conditions for each equation chains are set at the intersection of the corresponding line  $G_p$  family to the border area.

The equation of heat kinetics similar to replace a chain of equations

$$\frac{1}{3} \frac{\partial \omega_p}{\partial t} = E_p, \sum_{p=1}^3 E_p = E.$$

You can not do this, you need only follow choby heat contribution to the value  $f(\tau)$  during the time  $\tau$  is equal to  $(Q_{\max}, E, \tau)$  at every point of the field.

Physically replacing the three-dimensional heat equation chain-dimensional equations means that the thermal conductivity of the process occurring in the space is replaced by a sequence of one-dimensional processes coordinate directions.

## 3 Results

Let heat-proof partitions installed on the  $X_2$  and  $X_3$  directions in point of time  $t_i$ , i.e. heat spreads only in the direction  $X_1$ .

At time  $t = t_j + \tau$  directions  $X_1$  and  $X_2$  are changing roles, and at the time  $t = t_j + 2\tau$  applies heat only in the direction  $X_3$ . As a result, at the time  $t_j + 3\tau$  will have the same temperature distribution, and that at the time  $t = t_j + \tau$  in a three-dimensional thermal conductivity.

For the numerical solution of the model equations on the interval  $[0, t_0]$  need to consistently get the decision on the intervals  $[t_j, t_{j+1}, j= 1, \dots, j_0]$ , and the solution of the problem in the previous half-interval is the initial condition for the problem in the future. In turn, the solution of the problem on each half-interval  $[t_j, t_{j+1}]$  are conducted sequentially in three directions.

Approximation of the one-dimensional differential equations of a system of linear differential equations along each line of the family C, the system of differential equations

$$\frac{1}{3}c \frac{\partial u_p}{\partial t} = L_p u_p + f_p,$$

$$\frac{1}{3} \frac{\partial \omega_p}{\partial t} = E_p.$$

approximated by a system of linear differential equations

$$c_i \frac{\widehat{u}_i - u}{\tau} = \frac{1}{h_p} \left( a_{i+1} \frac{\widehat{u}_{i+1} - \widehat{u}_i}{h_p} - a_i \frac{\widehat{u}_i - \widehat{u}_{i-1}}{h_p} \right) + f_{pi}; \quad i = 2, \dots, N - 1;$$

$$\frac{\widehat{\omega}_i - \omega_i}{\tau} = E_{pi}, \quad i = 1, \dots, N;$$

$$a_{i+1} = \frac{1}{2} (\lambda_{p(i+1)} + \lambda_{pi}),$$

where the function arguments are taken in the  $i$ -th node on the line at the time  $G_p$

$$\left( t_j + \frac{P-1}{3} \tau \right),$$

if the symbol  $\widehat{\phantom{x}}$  is absent, and at time  $(t_j + \frac{P}{3} \tau)$ , if the caret is present.

The resulting system comprises  $(2N - 2)$  linear equations and  $2N$  unknowns  $-\widehat{u}_i$  and  $\widehat{\omega}_i$ . The values  $u_i$  and  $\omega_i$  solutions known from the previous step. This system is complemented by the two equations poluchaemymy from the boundary conditions at the points of intersection of the line with the boundary of  $G_p$

$$\widehat{u}_i = x_i \widehat{u}_2 + \mu_1,$$

$$\widehat{u}_N = x_2 \widehat{u}_{N-1} + \mu_2,$$

where the following notation:

$$x_1 = \frac{\tau a_2}{h_p^2 \Delta_1}, \quad \Delta_1 = \frac{\tau}{h_p^2} a_2 + \frac{1}{2} c_1 + \frac{1}{h_p} \left( c_{n_1} + \frac{\tau}{R_1} \right),$$

$$\mu_1 = \frac{1}{\Delta_1} \left\{ \frac{1}{h_p} \left[ c_{n_1} u_1 + \tau \left( \frac{V_1}{R_1} + q_{n_1} \right) \right] + \frac{1}{2} [c_1 u_1 + \tau f_{p1}] \right\},$$

$$x_2 = \frac{\tau a_N}{h_p^2 \Delta_2}, \quad \Delta_2 = \frac{\tau}{h_p^2} a_N + \frac{1}{2} c_N + \frac{1}{h_p} \left( c_{n_N} + \frac{\tau}{R_N} \right),$$

$$\mu_2 = \frac{1}{\Delta_2} \left\{ \frac{1}{h_p} \left[ c_{n_N} u_N + \tau \left( \frac{V_N}{R_N} + q_{n_N} \right) \right] + \frac{1}{2} [c_N u_N + \tau f_{pN}] \right\}.$$

This system of equations is solved by the sweep method known, and reliable streaming option to apply this method, gives the best results for systems with highly changeable coefficients [5].

## 4 Discussion

The dependence of the thermal conductivity of concrete coefficients on the coordinates and direction, caused by the presence of steel reinforcement, can not be directly considered in the differential equations, as the grid spacing greater than the diameter of the reinforcing bar. Imagine that the rebar in concrete is artificially allocated such that the total thermal resistance of the rod and the surrounding concrete is not changed. Suppose, for example, the rebar is located along a straight line of the family  $G, f$  and has a cross section. Then the effective thermal conductivity coefficient determined from the equation

$$\lambda_B(S' - S_A) + \lambda_A S_A = \lambda' S',$$

where

$\lambda_B$  and  $\lambda_A$  - concrete and steel thermal conductivity,  $W / (m^2 \text{ } ^\circ C)$ ;

$S' = h_2 h_3$  and  $\lambda'$  - column concrete area with the conditional distribution of valves,  $m^2$  and thermal conductivity of the concrete,  $W / (m^2 \text{ } ^\circ C)$ .

Consequently,

$$\lambda' = \lambda_B + (\lambda_A - \lambda_B) \frac{S_A}{S'}.$$

This value must be submitted to the corresponding difference equation.

Recommended absence of VOC is absolutely stable and uniformly at a rate of  $O(\tau + |h|^2)$ . We do not recommend the use of explicit schemes, as a three-dimensional explicit scheme is stable only if  $\tau < h^2/6\alpha$  restrictions ( $\alpha$  - conductivity-temperature coefficient,  $m^2/s$ ), which results in very small time step. In order to solve a particular problem for the present method is to beat the compiled program to calculate over then varying the control actions and to carry out calculations of the temperature field, select the most efficient mode of heat treatment.

There are a number of methods to search for the minimum of non-linear functions of several variables. Libraries of standard programs usually contain a program implementing one of these methods. For the independent preparation of such a program, you can recommend the most simple method of descent.

The above method of calculating the heat release function coefficients provides a function that best experimental data according heat intensity  $(\frac{dQ}{dt})$  temperature ( $u$ ) and concrete heat ( $Q$ ), positioning with a minimum of data. It suffices to have the results of only one of concrete heat dissipation experiment temperature mode, which covers the entire temperature range of interest. This is achieved through the use of the recommended method of mathematical processing of the experimental results.

## Conclusion

Consider the example of the calculation of the temperature field of concrete for the area, which is about the size of parallelepiped,  $0.48 \times 0.48 \times 2.7$  m (fragment of a column). The lower part of the area previously occupied by the size  $0.48 \times 0.48 \times 1.7$  m laid concrete with a coefficient of relative heat  $\omega_0 = 0.9$ , and the upper part of the size  $0.48 \times 0.48 \times 1$  m takes concrete mix with  $\omega_0 = 0.01$ . On top of concrete covered with mat thickness  $c = 0.05$  m with a coefficient of thermal conductivity  $d = 0.05$   $W/m^2 \text{ } ^\circ C$ . The heat transfer coefficient of the outer surface of the structural  $\alpha = 25$   $W/m^2 \text{ } ^\circ C$ , ambient temperature  $U_B = -10^\circ C$  [14, 15].

We place the origin at the lower top of the box and send J-axis; up edge and the axis  $X_1$  and  $X_2$  horizontal at the base of the ribs. The heating formwork to the side faces, starting

from a height  $X_3 = 1.5$  m. In concrete, the distance in the vertical direction through four lateral edges of the reinforcing rod diameter of 0.02 m at a distance of 0.06 meters from the lateral faces. Since the column is symmetric about the vertical axis passing through the center of the box to hold enough account for a quarter of the field, cut-out planes  $X_1 = 0.24$  m and  $X_2 = 0,24$  m. Heat flow through these planes will be zero. We introduce in the grid with steps  $h_1 = 0.03$  m,  $h_2 = 0.03$  and  $h_3 = 0.06$  m, respectively, on the axes  $X_1$ ,  $X_2$  and  $X_3$ . The total number of grid points  $9 \times 9 \times 46 = 3726$ . Rebar passes the nodes  $(3, 3, N)$  with  $N = 1, \dots, 46$ , so the thermal conductivity in the  $X_3$  direction in these nodes should be calculated from the formula (5)

$$\lambda' = \lambda_B \left[ 1 + \left( \frac{\lambda_A}{\lambda_B} - 1 \right) \frac{S_A}{S'} \right],$$

Where  $S_A = 3,14 * (0,01)^2 \text{ m}^2$ ;  $S' = h_1 h_2 = (0,03)^2 \text{ m}^2$

Let us  $\lambda_A = 40 \text{ W}/(\text{m}^0\text{C})$ ;  $\lambda_B = \lambda_0 - \omega(\lambda_0 - \lambda_1)$ ;

$\lambda_0 = 3 \text{ W}/(\text{m}^0\text{C})$ ;  $\lambda_1 = 2,6 \text{ w}/(\text{m}^0\text{C})$ . The coefficients in the equation of concrete heat release kinetics:  $Q_{max} = 1,25 * 10^5 \text{ kJ}/\text{m}^3$ ;  $K = 4,77 * 10^{-6} \text{ c-1}$ ;  $u_3 = -6,7^\circ\text{C}$ ;  $\zeta = 2,3$ ;  $\nu = 2,2$ .

Specific volume heat capacity of concrete  $SB = 2000 \text{ kJ}/(\text{m}^3\text{C})$ .

The initial value of the relative heat take  $\omega_0 = 0,9$  in the nodes  $(I, J, N)$  at  $I \leq N \leq 29$  ( $0 \leq x_3 \leq 1,7$  m - previously poured concrete) and  $\omega_0 = 0,1$  in the nodes  $(I, J, N)$  at  $29 < N \leq 46$  ( $1,7 < x_3 < 2,7$  m - concrete). Suppose that the initial temperature of the concrete mix  $u_0 = +5^\circ\text{C}$  in the nodes  $(I, J, N)$  at  $29 < N \leq 46$ , and the initial temperature of the previously poured concrete  $u_0 = -9^\circ\text{C}$  in sites  $(I, J, N)$ ,  $I \leq N \leq 29$ .

Specific power heating formwork  $q_n = 1 \text{ kW}/\text{m}^2$ , the thickness of the insulation layer of the deck  $d = 0,04$  m, the thermal conductivity of insulation material  $\lambda_{u_3} = 0,04 \text{ W}/(\text{m}^0\text{C})$ , and the specific heat of the deck  $c_n = 20 \text{ kJ}/(\text{m}^2\text{C})$ . Suppose the lower face of the box  $1/R = 0$ ,  $c_n = 0$ ,  $q_n = 0$ . Heat flow is also zero in the plane  $x_1 = 0.24$  m and  $x_2 = 0.24$  m.

On the open side faces of the heat exchange takes place:  $1/R = \alpha = 25 \text{ kJ}/(\text{m}^2\text{C})$ ,  $c_n = 20 \text{ kJ}/\text{m}^2$ ,  $q_n = 1 \text{ kW}/\text{m}^2$ . On the upper face:  $R = 1,04 (\text{m}^2\text{C})/\text{W}$ ,  $c_n = 0$ ,  $q_n = 0$ .

Calculation of the temperature field for this task can be performed using a specialized computer program.

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