# Current in lighting wire grounded in each tower determination under short circuit to tower or short circuit to earth escape tower 

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#### Abstract

The algorithms for short circuit (SC) currents as well as induced in grounded in each tower lighting wire (LW) currents are presented for the case of SC to overhead transmission line (OTL) tower and to the ground passing the tower.


## Introduction

Overhead transmission lines (OTL) are equipeed by lighting wires ontaining fiber optical communication channels (FOLW). FOLW technically are grounded in each OTL tower. OTL damaged phase current magnetic field (MF) as well as short circuit (SC) current in FOLW under SC is created the current, and this current value should not exceed the value permissible by thermal stability. In the report of this workshop 2018 [1,2] Double-circuit 220 kV OTL 46.956 km length without transpositions in tower Itph220-2+5 brand is discussed (Figure 1). There are determined self- and mutualinductive resistance, earth resistance as well as electromotive force


Fig. 1. 220 kV double-circuit OTL on intermediate tower. induced in LF under known single-phase SC to the ground for phases and LW by Carson equations [3,4,5] when $\rho_{3}=100 \mathrm{Ohm} / \mathrm{m}$ ground resistivity and 0.33 km span long. There are calculated induced by SC to the ground MF nearest to the wire C2 phase in LW at $0.5 ; 1 ; 2$; 3; 4; 5; 7.8 and 10 km from substation 2 for OTL connection to substation 2 with less network resistance and idling (Id) at substation 1 side. Calculations are carried out for following brands LW: FOLW-c-1-24(G.652)-18,7/93, FOLW-c-1-16(G.652)-14,7/61, FOLW-c-1-24(G.652)-13,1/54 and FOLW-ц-1-48(G.652)-12/94. Maximal current value was
induced in 6th span under SC at 5 km distance from substation 2 for all FOLW (for FOLW-...-18.7/93 $\mathrm{I}_{\mathrm{Wmax}}=$ $\mathrm{I}_{\mathrm{W} 6}=5.48 \mathrm{kA}$ ). There are determined the currents induced in FOLW for simultanious C 1 and C2 phases SC to the ground at 5 km distanse from substation 2 unlikely case. This case for FOLW -...-18.7/93 $\mathrm{I}_{\mathrm{Wmax}}=\mathrm{I}_{\mathrm{W} 6}=6.296 \mathrm{kA}$. In [2] there was discussed the case of 220 kV OTL C2 phase (connected to substation 1 and substation 2 and operation without power transmission) SC to the ground at 5 km distance from substation 2, and FOLW-...-18.7/93 $\mathrm{I}_{\mathrm{W}_{\text {max }}}=\mathrm{I}_{\mathrm{W} 6}=5.152 \mathrm{kA}$. SC current and induced in LW current simultaneous determination were carried out for 220 kV OTL idling case at substation 1 (S1) side and C2 phase SC to the ground at 5 km distance from substation 2 [1,2] (Figure 2).
Current simultaneous determination method allows taking into account the current in LW affect to SC current as well as SC current flowing into LW. Under case of simultaneous calculation method current greatest value in LW is accounts for first span from substation 2 (S2), and for 220 kV OTL FOLW-...-18.7/93 $\mathrm{I}_{\mathrm{W}_{\max }}=\mathrm{I}_{\mathrm{W} 1}$ $=6.876 \mathrm{kA}$.


Fig. 2. The sheme of simultanious determination of C 2 phase SC current to the ground, and currents induced in LW.

## 1 Current in LW depend on distance from C2 phase operating in idle regime at S1 side SC to the ground place

For FOLW testing brands let's make a simultaneous determination of SC current and currents in wires under

[^0]C 2 phase SC to the ground at the ends of span. The number (No.) of SC span: $1 \div 5,8,10 \div 15$ and 18 . Maximal current module value in FOLW for all calculated cases were in first from S2 span, i.e. current $\mathrm{I}_{\mathrm{W} 1}$ has the maximal value.
Figure 3 shows the histogram of current module value of 220 kV OTL with FOLW -...-18.7/93, figure 4 - with FOLW-..-14.7/61 and FOLW-...-13.1/54, and figure 5 - with FOLW-...-12/94.
$\mathrm{I}_{\mathrm{W} 1}$ Greatest current values for:
FOLW-...-18.7/93 under SC span $\mathrm{No} .=12, \mathrm{I}_{\mathrm{LW}}=7.42 \mathrm{kA}$; FOLW-...-14.7/61 under SC span $\mathrm{No} .=11, \mathrm{I}_{\mathrm{LW}}=6.86 \mathrm{kA}$; FOLW-...-13.1/54 under SC span $\mathrm{No} .=10, \mathrm{I}_{\mathrm{LW}}=6.42 \mathrm{kA}$; FOLW-...-12.0/94 under SC span $\mathrm{No} .=8, \mathrm{I}_{\mathrm{LW} 1}=4.64$ кА.


Fig. 3. The histograms of $\mathrm{I}_{\mathrm{LW} 1}$ currents for 220 kV OTL with FOLW-...-18.7/93 under C2 phase SC to the ground at the end of span number: $1,3,5,11,12,14$ and 18


Fig. 4. The histograms of $\mathrm{I}_{\mathrm{LW} 1}$ currents for 220 kV OTL with FOLW-...-14.7/61 and FOLW-...-13.1/54 under C2 phase SC to the ground at the end of span number: $1,3,5,10,11,12,14$ and 18


Fig. 5. The histograms of $\mathrm{I}_{\mathrm{LW} 1}$ currents for 220 kV OTL with FOLW-...-12/94 under C2 phase SC to the ground at the end of span numbers:1, $3,5,8,10,13$ и 18

## 2 Current in LW depending on distance to S2 from C1 and C2 phases 220 kV OTL operating in idle mode at S1 side SC to the ground place

Let's calculate the currents of simultaneous C1 and C2 phases SC to the ground as well as currents in LW. SC is at the end of 15 th span from 220 kV S 2 operating in idle mode. The sheme of calculation is shown in figure 6.


Fig. 6. The scheme of C 1 and C 2 phases simultanious SC to the ground at the end of 15th span from S2.
Let's analyse 220 kV OTL with FOLW-...-18.7/93. Then for figure 6 sheme: $\underline{Z}_{\mathrm{C} 1}=R_{\mathrm{C} 1}+\mathrm{j} X_{\mathrm{LC} 1}=\underline{Z}_{\mathrm{C} 2}=R_{\mathrm{C} 2}+$ $\mathrm{j} X_{\mathrm{LC} 2}=0.02433+\mathrm{j} 0.23388$ Ohm; $\underline{Z}_{\mathrm{LW}}=R_{\mathrm{W}}+\mathrm{j} X_{\mathrm{LW}}=$ $0.0667+\mathrm{j} 0.2422$ Ohm; $Z_{\mathrm{e}}=0.01533$ Ohm; $\underline{Z}_{\mathrm{WC} 1}=$ $0.0154+\mathrm{j} 0.100$ Ohm; $\quad \underline{Z}_{\mathrm{WC} 2}=0.015+\mathrm{j} 0.101$ Ohm; $\underline{Z}_{\mathrm{C} 1 \mathrm{C} 2}=0.0155+\mathrm{j} 0.1167$ Ohm; $\underline{Z}_{\mathrm{S} 2}=R_{\mathrm{S} 2}+\mathrm{j} X_{\mathrm{LS} 2}=$ $0.841+\mathrm{j} 5.796 \mathrm{Ohm} ; \underline{Z}_{\mathrm{NE}}=1.257+\mathrm{j} 0.816 \mathrm{Ohm} ; R_{\mathrm{GDS}}=$ $0.5 \mathrm{Ohm} ; R_{\mathrm{GD}}=10 \mathrm{Ohm} ; R_{\mathrm{A}}=0.42 \mathrm{Ohm} ; \boldsymbol{E}_{\mathrm{C} 2}=$ $127017 \angle 120^{\circ} \mathrm{B}$.
System of equations by the method of contour currents:

$$
\begin{aligned}
& \dot{J}_{0}\left(\underline{Z}_{\mathrm{s} 2}+15 \underline{Z}_{\mathrm{c} 2}+15 Z_{\mathrm{e}}+R_{\mathrm{A}}+R_{\mathrm{CDS}}\right)+\dot{J}_{1}\left(R_{\mathrm{CDS}}+Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC}}\right)+\dot{J}_{2}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{Wc}}\right)+. \\
& \ldots+\dot{J}_{15}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{Wc} 2}\right)+\dot{J}_{16}\left(\underline{Z}_{\mathrm{S} 2}+R_{\mathrm{A}}+15 Z_{\mathrm{e}}+R_{\text {G0S }}+15 \underline{Z}_{\mathrm{clC}}\right)=\dot{E}_{\mathrm{C} 2} ; \\
& \dot{J}_{0}\left(R_{\mathrm{GDS}}+Z_{\mathrm{c}}+\underline{Z}_{\mathrm{WC}}\right)+\dot{J}_{1}\left(\underline{Z}_{\mathrm{LW}}+R_{\mathrm{GD}}+Z_{\mathrm{e}}+R_{\mathrm{GDS}}\right)-\dot{J}_{2} R_{\mathrm{GD}}+ \\
& +\dot{J}_{16}\left(R_{\text {grs }}+Z_{\mathrm{e}}+\underline{Z}_{\text {wcl }}\right)=0 \text {; } \\
& \dot{J}_{0}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC} 2}\right)-\dot{J}_{1} R_{\mathrm{GD}}+\dot{J}_{2}\left(\underline{Z}_{\mathrm{LW}}+2 R_{\mathrm{GD}}+Z_{\mathrm{e}}\right)-\dot{J}_{3} R_{\mathrm{GD}}+\dot{J}_{16}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC}}\right)=0 ; \\
& \dot{J}_{0}\left(Z_{\mathrm{e}}+\underline{\mathrm{Z}}_{\mathrm{WC}}\right)-\dot{J}_{13} R_{\mathrm{GD}}+\dot{J}_{14}\left(\underline{Z}_{\mathrm{LW}}+2 R_{\mathrm{GD}}+Z_{\mathrm{e}}\right)-\dot{J}_{\mathrm{IS}} R_{\mathrm{CD}}+\dot{J}_{16}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WCI}}\right)=0 ; \\
& \dot{J}_{0}\left(Z_{\mathrm{c}}+\underline{Z}_{\mathrm{Wc} 2}\right)-\dot{J}_{14} R_{\mathrm{GD}}+\dot{J}_{15}\left(\underline{Z}_{\mathrm{Lw}}+Z_{\mathrm{NE}}+Z_{\mathrm{c}}+R_{\mathrm{GD}}\right)+\dot{J}_{\mathrm{I}}\left(Z_{\mathrm{c}}+\underline{Z}_{\mathrm{WCI}}\right)=0 \text {; } \\
& \dot{J}_{0}\left(\underline{Z}_{\mathrm{s} 2}+15 \underline{Z}_{\mathrm{Cl}}+15 Z_{\mathrm{c}}+R_{\mathrm{A}}+R_{\mathrm{GDS}}\right)+\dot{J}_{1}\left(R_{\mathrm{GDS}}+Z_{\mathrm{c}}+\underline{Z}_{\mathrm{WC}}\right)+\dot{J}_{2}\left(Z_{\mathrm{c}}+\underline{Z}_{\mathrm{wc}}\right)+ \\
& \ldots+\dot{J}_{14}\left(Z_{\mathrm{e}}+\underline{Z}_{\text {wcl }}\right)+\dot{J}_{15}\left(Z_{\mathrm{e}}+\underline{Z}_{\text {wcl }}\right)+ \\
& +\dot{J}_{16}\left(Z_{\mathrm{s} 2}+15 \underline{Z}_{\mathrm{C} 1}+15 Z_{\mathrm{e}}+R_{\mathrm{A}}+R_{\mathrm{CDS}}\right)=\dot{E}_{\mathrm{C} 2}
\end{aligned}
$$

Solving equations system and considering that $\boldsymbol{I}_{\mathrm{C} 12}=$ $\boldsymbol{J}_{16}, \boldsymbol{I}_{\mathrm{C} 12}=\boldsymbol{J}_{0}, \boldsymbol{I}_{\mathrm{LW} 1}=\boldsymbol{J}_{1}, \boldsymbol{I}_{\mathrm{LW} 15}=\boldsymbol{J}_{15}$, and $\boldsymbol{I}_{\mathrm{A}}=\boldsymbol{J}_{0}+\boldsymbol{J}_{16}$, will obtain:
$\boldsymbol{I}_{\mathrm{C} 12}=7.868 \angle 43.5^{\circ} \mathrm{kA} ; \quad \boldsymbol{I}_{\mathrm{C} 22}=7.822 \angle 43.3^{\circ} \mathrm{kA} ;$
$\boldsymbol{I}_{\mathrm{A}}=15.691 \angle 43.4^{\circ} \mathrm{kA}$;
$\boldsymbol{I}_{\mathrm{LW} 1}=8.055 \angle-138.3^{\circ} \mathrm{kA} ; \boldsymbol{I}_{\mathrm{LW} 2}=7.696 \angle-138.2^{\circ} \mathrm{kA}$;
$\boldsymbol{I}_{\mathrm{LW} 3}=7.357 \angle-137.8^{\circ} \mathrm{kA} ; \ldots ; \boldsymbol{I}_{\mathrm{LW} 13}=4.160 \angle-133.0^{\circ} \mathrm{kA}$;
$\boldsymbol{I}_{\mathrm{LW} 14}=3.767 \angle-134.5^{\circ} \mathrm{kA} ; \boldsymbol{I}_{\mathrm{LW} 16}=3.358 \angle-137.5^{\circ} \mathrm{kA}$.
Ток $I_{\text {LW } 1}$ current has maximal value.
There were carried out simultanious SC current determination as well as currents in LWs under C1 and C 2 SC to the ground at the end of span (all analised FOLW brands). No. of span: 1, 3, 5, 8, 10, 11, 12, 13, 14, 18 (Figures 7, 8 and 9).
Maximal current values $\boldsymbol{I}_{\mathrm{LW} 1}$ for:
FOLW-...-18.7/93 under SC span No. $=13, I_{\mathrm{LW} 1}=8.09 \mathrm{kA}$;
FOLW-...-14.7/61 under SC span No. $=12, I_{\mathrm{LW} 1}=7.45 \mathrm{kA}$;
FOLW-...-13.1/54 under SC span No. $=12, I_{\text {LW }}=6.96 \mathrm{kA}$;

FOLW-...-12.0/94 under SC span No. $=8, I_{\text {LW1 }}=4.93 \mathrm{kA}$. $I_{\mathrm{w} 1}$, kA


Fig. 7. The histograms of $\mathrm{I}_{\text {LW }}$ currents for 220 kV OTL with FOLW-...-18.7/93 under C1 and C2 phase SC to the ground at the end of span number: $1,3,5,8,10,12,13,14$ и 18


Fig. 8. The histograms of $\mathrm{I}_{\mathrm{LW} 1}$ currents for 220 kV OTL with FOLW -...-14.7/61 and FOLW-...-13.1/54 under C1 and C2 phase SC to the ground at the end of span number: $1,3,5,8$, $11,12,13,15$ и 18


Fig. 9. The histograms of $\mathrm{I}_{\text {LW }}$ currents for 220 kV OTL with FOLW -...-12/94 under C1 and C2 phase SC to the ground at the end of span number: $=1,3,5,8,10,11,12,13$ и 14

## 3 Current in LW depending on the distance from 220 kV OTL (operating in in connected mode, but without power transmission) C2 phase SC to tower place to $\mathbf{S 2}$

Currents in LW 220 kV OTL operating in connected to both side mode but without power transmission SC current and and C2 phase SC to tower of first from S2 span current simultanious calculation will make (Figure 10).


Fig. 10. The scheme of OTL 220 kV operating in both side connection but without power transmission C 2 phase SC to tower of $1^{\text {st }}$ from S2 span.
The system of equations by countur current method:

$$
\begin{aligned}
& \dot{J}_{1}\left[\underline{Z}_{\mathrm{s} 2}+\underline{Z}_{\mathrm{C} 2}+Z_{\mathrm{e}}+R_{\mathrm{A}}+R_{\mathrm{GD}}+R_{\mathrm{GDS}}\right]+ \\
& +\dot{J}_{2}\left(R_{\mathrm{GDS}}+Z_{\mathrm{e}}+R_{\mathrm{GD}}+\underline{Z}_{\mathrm{WC} 2}\right)-\dot{J}_{3} R_{\mathrm{GD}}+0+\ldots+0+ \\
& +0-\dot{J}_{144}\left(R_{\mathrm{GD}}+R_{\mathrm{A}}\right)+\dot{J}_{145}\left(\underline{Z}_{\mathrm{S} 2}+R_{\mathrm{GDS}}+Z_{\mathrm{e}}+\underline{Z}_{\mathrm{CIC} 2}\right)=\dot{E}_{\mathrm{C} 2} ; \\
& \dot{J}_{1}\left(R_{\mathrm{GDS}}+Z_{\mathrm{e}}+R_{\mathrm{GD}}+\underline{Z}_{\mathrm{WC} 2}\right)+\dot{J}_{2}\left(\underline{Z}_{\mathrm{LW}}+R_{\mathrm{GD}}+Z_{\mathrm{e}}+R_{\mathrm{GDS}}\right)-\dot{J}_{3} R_{\mathrm{GD}}+0+\ldots+0- \\
& -\dot{J}_{144} R_{\mathrm{GD}}+\dot{J}_{145}\left(R_{\mathrm{GDS}}+Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WCl}}\right)=0 \text {; } \\
& -\dot{J}_{1} R_{\mathrm{GD}}-\dot{J}_{2} R_{\mathrm{GD}}+\dot{J}_{3}\left(\underline{Z}_{\mathrm{LW}}+2 R_{\mathrm{GD}}+Z_{\mathrm{e}}\right)-\dot{J}_{4} R_{\mathrm{GD}}+0+\ldots+0+ \\
& +0+\dot{J}_{144}\left(Z_{\mathrm{e}}+R_{\mathrm{GD}}+\underline{Z}_{\mathrm{WC} 2}\right)+\dot{J}_{145}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC} 1}\right)=0 ; \\
& 0+\ldots+0-\dot{J}_{142} R_{\mathrm{GD}}+\dot{J}_{143}\left(\underline{Z}_{\mathrm{LW}}+R_{\mathrm{GDS}}+R_{\mathrm{GD}}+Z_{\mathrm{e}}\right)+ \\
& +\dot{J}_{144}\left(R_{\mathrm{GDS}}+Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC} 2}\right)+\dot{J}_{145}\left(R_{\mathrm{GDS}}+Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC} 1}\right)=0 ; \\
& -\dot{J}_{1}\left(R_{3 \mathrm{Y}}+R_{\mathrm{A}}\right)-\dot{J}_{2} R_{\mathrm{GD}}+\dot{J}_{3}\left(R_{\mathrm{GD}}+Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC} 2}\right)+\dot{J}_{4}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC} 2}\right)+ \\
& +\dot{J}_{5}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC} 2}\right)+\ldots+\dot{J}_{141}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC} 2}\right)+\dot{J}_{142}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC} 2}\right)+ \\
& +\dot{J}_{143}\left(R_{\mathrm{GDS}}+Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC} 2}\right)+\dot{J}_{144}\left[\underline{Z}_{\mathrm{S} 1}+141\left(\underline{Z}_{\mathrm{C} 2}+Z_{\mathrm{e}}\right)+R_{\mathrm{A}}+R_{\mathrm{GD}}+R_{\mathrm{GDS}}\right]+ \\
& +\dot{J}_{145}\left(\underline{Z}_{\mathrm{S} 1}+R_{\mathrm{GDS}}+141 Z_{\mathrm{e}}+141 \underline{Z}_{\mathrm{CIC} 2}\right)=-\dot{E}_{\mathrm{C} 1} \text {; } \\
& \dot{J}_{1}\left(\underline{Z}_{\mathrm{S} 2}+R_{\mathrm{GDS}}+Z_{\mathrm{e}}+\underline{Z}_{\mathrm{CIC2}}\right)+\dot{J}_{2}\left(R_{\mathrm{GDS}}+Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC} 1}\right)+\dot{J}_{3}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC1}}\right)+ \\
& +\dot{J}_{4}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WCI}}\right)+\ldots+\dot{J}_{141}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WCI}}\right)+\dot{J}_{142}\left(Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WCI}}\right)+ \\
& +\dot{J}_{143}\left(R_{\mathrm{GDS}}+Z_{\mathrm{e}}+\underline{Z}_{\mathrm{WC1}}\right)+\dot{J}_{144}\left(\underline{Z}_{\mathrm{S} 1}+R_{\mathrm{GDS}}+141 Z_{\mathrm{e}}+141 \underline{Z}_{\mathrm{CIC2}}\right)+ \\
& +\dot{J}_{145}\left[\underline{Z}_{\mathrm{s} 2}+\underline{Z}_{\mathrm{S} 1}+142\left(\underline{Z}_{\mathrm{C} 1}+Z_{\mathrm{e}}\right)+2 R_{\mathrm{GDS}}\right]=\dot{E}_{\mathrm{C} 2}-\dot{E}_{\mathrm{C} 1} .
\end{aligned}
$$

The solving of eguation system give the values of SC current, currents in LW as well as in C1 and C2 phases. Figure 11 shows the hisogramms of current modules for 220 kV OTL with FOLW-..-18.7/93 ( $\mathrm{Z}_{\mathrm{LW}}=0.066+$ $\mathrm{j} 0.240 \mathrm{Ohm})$ and with FOLW-...-12/94 ( $\mathrm{Z}_{\mathrm{LW}}=0.368+$ j 0.249 Ohm ), and in figure 12 - with FOLW-...-14.7/61 $\left(\underline{Z}_{\mathrm{LW}}=0.109+\mathrm{j} 0.245 \mathrm{Ohm}\right)$ and with FOLW-..-13.1/54 $\left(\underline{Z}_{L W}=0.146+j 0.427\right.$ Ohm $)$.
Under C2 phase SC to $1^{\text {st }}$ span tower arc current were: for FOLW-...-18.7/93 $\boldsymbol{I}_{\mathrm{A}}=24.74 \angle 43.3^{\circ} \mathrm{kA}$, for FOLW-$\ldots-12 / 94 \boldsymbol{I}_{\mathrm{A}}=24.01 \angle 43.0^{\circ} \mathrm{kA}$, for FOLW-...-14.7/61 $\boldsymbol{I}_{\mathrm{A}}$ $=24.65 \angle 44.0^{\circ} \mathrm{kA}$, and for FOLW-..-13.1/54 $\boldsymbol{I}_{\mathrm{A}}=$ $24.54 \angle 44.5^{\circ} \mathrm{kA}$.
Figure 13 shows the histogram of currents under SC of C2 phase of OTL with FOLW-...-18.7/93 and with FOLW-$\ldots-12 / 94$ to $5^{\text {th }}$ tower from substation 2 , and figure $14-$ to $30^{\text {th }}$ tower from substation 2 .
The distance of SC to tower place from substation 2 lead to phase current values as well as current in LW and arc current $I_{\mathrm{A}}$ dicrease. Current higher value in LW is achieved in the span located in the direction of the nearest from the tower on which was SC substation. In our case in the substation 2 direction. The greatest value is current $I_{\mathrm{W} 1}$ under SC to $1^{\text {st }}$ span tower.
Figure 15 shows the histograms of greatest current module values $I_{\mathrm{Wmax}}$ in LW under SC to tower of $1 \div 5$ th, 10th, 15th, 20th, 30th and 40th span from S2 side for FOLW-c-1-24(G.652)-18.7/93 and FOLW-c-1-48(G.652)-12/94.


Fig. 11. Current modules under SC of C 2 phase SC to $1^{\text {st }}$ span from S2 for FOLW-...-18.7/93 and FOLW-...-12/94.


Fig. 12. Current modules under SC of C 2 phase SC to $1^{\text {st }}$ span from S2 for FOLW-...-14.7/61 and FOLW-...-13.1/54.


Fig. 13. Current modules under SC of C 2 phase SC to $5^{\text {th }}$ span from S2 for FOLW-...-18.7/93 and FOLW-...-12/94.

When OTL is powered from S 1 side, idle at S 2 side and SC to $1^{\text {st }}$ from S 1 tower $\mathrm{I}_{\mathrm{W} 1}$ current has a lower value (Fig. 16), because $\underline{Z}_{\mathrm{N} 1}=0.93+\mathrm{j} 8.46$ Ohm network resistance at S 1 side is more network resistance $\underline{Z}_{\mathrm{N} 2}=0.84+\mathrm{j} 5.00$ Ohm at S 2 side.


Fig. 14. Current modules under SC of C 2 phase SC to $30^{\text {th }}$ span from S2 for FOLW-...-18.7/93 and FOLW-...-12/94.


Fig. 15. Current module $I_{\mathrm{Wmax}}$ change under C 2 phase SC to towers in span from S2 side: $1 \div 5$ th, 10th, 15th, 20th, 30th and 40th for FOLW-...-18.7/93 and FOLW-...-12/94.


Fig. 16. Current module in LW and 220 OTL phases change under C 2 phase SC to 1 st from S1 and S2 tower for FOLW-c-1-24(G.652)-18.7/93.
$\mathrm{I}_{\mathrm{W} 1}$ greatest values under SC to $1^{\text {st }}$ from S 2 span tower:

$$
\begin{aligned}
& \text { FOLW- } \ldots-18.7 / 93, \mathrm{I}_{\mathrm{W} 1}=21.1 \mathrm{kA} ; \\
& \text { FOLW-...-14.7/61, } \mathrm{I}_{\mathrm{W} 1}=20.9 \mathrm{kA} ; \\
& \text { FOLW-...-13.1/54, } \mathrm{I}_{\mathrm{W} 1}=20.7 \mathrm{kA} ; \\
& \text { FOLW-...-12.0/94, } \mathrm{I}_{\mathrm{W} 1}=19.6 \mathrm{kA} .
\end{aligned}
$$

## 4 SC currents as well as currents in LW of 220 kV OTL operating in connected mode but without power transmission under simultanious C1 and C2 SC to first from S2 span tower

Let's simultanious calculate C 1 and C 2 phases SC to the ground current as well as currents in LW induced by MF of SC to 1st span from S2 current of 220 kV OTL operating in connected mode but without power trznsmission (Fig. 17).


Fig. 17. The scheme of C 1 and C 2 phases SC to 1 1st span current determination as well as currents in LW induced by MF of SC currents in 220 kV OTL operating in connected mode but witout power transmission.

Figure 18 shows the histograms of countour current modules in LW spans as well as currents in C1 and C2 under simultanious C 1 and C 2 phases SC to 1 st span tower for LW executed by FOLW-c-1-24(G.652)-18.7/93 and FOLW-c-1-48(G.652)-12/94, and figure 19 -executed by FOLW-c-1-16(G.652)-14.7/61 and FOLW-c-1-24(G.652)-13.1/54.
In case of simultanious C 1 and C 2 SC to tower of 1st span arc currents were: for FOLW-c-1-24(G.652)-18.7/93 $\boldsymbol{I}_{\mathrm{A}}=$ $25.01 \angle 43.4^{\circ} \mathrm{kA}$, for FOLW-c-1-48(G.652)-12/94 $\boldsymbol{I}_{\mathrm{A}}=$ $24.27 \angle 46.7^{\circ} \mathrm{kA}$, for FOLW-c-1-16(G.652)-14.7/61 $\boldsymbol{I}_{\mathrm{A}}=$ $24.92 \angle 44.1^{\circ} \mathrm{kA}$, and for FOLW-c-1-24(G.652)-13.1/54 $\boldsymbol{I}_{\mathrm{A}}$ $=24.78 \angle 44.6^{\circ} \mathrm{kA}$.


Fig. 18. Current module in LW and 220 kV OTL phases changes under simultaneous C 1 and $\mathrm{C} 2 \quad \mathrm{SC}$ to the tower of $1^{\text {st }}$ span for FOLW-c-1-24(G.652)-18.7/93 and FOLW-c-1-48(G.652)-12/94


Fig. 19. Current module in LW and 220 kV OTL phases changes under simultaneous C 1 and $\mathrm{C} 2 \quad \mathrm{SC}$ to the tower of $1^{\text {st }}$ span for FOLW-c-1-16(G.652)-14.7/61 and FOLW-c-1-24(G.652)13.1/54.

The greatest $I_{\mathrm{W} 1}$ current values under C 1 and C 2 SC to the tower of first from S2 span:

$$
\begin{aligned}
& \text { FOLW- } \ldots-18.7 / 93, I_{\mathrm{W} 1}=21.31 \mathrm{kA} \text {; } \\
& \text { FOLW }-\ldots-14.7 / 61, I_{\mathrm{W} 1}=21.09 \mathrm{kA} \text {; } \\
& \text { FOLW }-\ldots-13.1 / 54, I_{\mathrm{W} 1}=20.88 \mathrm{kA} \text {; } \\
& \text { FOLW }-\ldots-12.0 / 94, I_{\mathrm{W} 1}=19.85 \mathrm{kA} .
\end{aligned}
$$

## Conclusion

Currents created in LW have the greates values under its simultanious determination with currents of joint C 1 and C 2 SC to the first span from S 2 tower.

Maximal limit time of SC current shutdown ( $t_{\text {Mlshutd }}$ ) at S2 will find by FOLW thermal stability (ThS, $\mathrm{kA}^{2} \mathrm{~s}$ ) and recieved current $\left(I_{\mathrm{W} 1}\right)$ highest value in LW span: $t_{\mathrm{Mlshutd}}=\mathrm{ThS} / I_{\mathrm{W} 1}^{2}$. Maximal limit time of SC current shutdown $t_{\text {Mlshutd }}$ at S 2 calculation results for analyzed FOLW brands are presented in table.
Table. Maximal limit time of SC current shutdown ( $t_{\text {Mlshutd }}$ ) at S2

| FOLW | $18.7 / 93$ | $14.7 / 61$ | $13.1 / 54$ | $12 / 94$ | $22.5 / 113$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ThS, <br> $\mathrm{kA}^{2} \mathrm{~s}$ | 350.2 | 132.7 | 78.7 | 31.2 | 969.9 |
| $I_{\mathrm{W} 1}, \mathrm{kA}$ | 21.31 | 21.09 | 20.88 | 19.85 | 21.48 |
| $t_{\text {Mlshutd, }}, \mathrm{s}$ | 0.771 | 0.298 | 0.164 | 0.079 | 2.102 |

Analyzed FOLW brands have low maximal limit time of SC current and shutdown ( $t_{\text {Mlshutd }}$ ) (less than 1s). So FOLW-c-1-24(G.652)-22.5/113 with 22.5 mm diameter, $0.12 \mathrm{Ohm} / \mathrm{km}$ resisitivity and $\mathrm{ThS}=969.9 \mathrm{kA}^{2} \cdot$ s thermal stability was chosen. This FOLW has under C1 and C2 phases SC to the 1st span from S2 tower $I_{\mathrm{W} 1}=21.48 \mathrm{kA}$, $I_{\mathrm{C} 11}=10.16 \mathrm{kA}, I_{\mathrm{C} 21}=10.42 \mathrm{kA}, I_{\mathrm{C} 12}=2.24 \mathrm{kA}, I_{\mathrm{C} 22}=$ 2.26 kA and $t_{\mathrm{Mlshutd}}=2.1 \mathrm{~s}$.

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