

# Deformation analysis based on GNSS measurements in Tashkent region

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**Abstract.** This paper presents the results of the GNSS geodetic network deformation analysis in the Tashkent region, as an example of an urban area, where obtaining reliable information for assessing hazard risk is of great importance. A software package in Delphi language has been developed for the assessment of the datum differences between 2009 and 2011 by implementing the 3D Helmert transformation method. The result revealed that there is significant translation and rotation in the network, while the scale of the network remains almost constant during two years period. The area strain was estimated by the finite element method. Most of the Tashkent region can be considered to be in a high compression (negative dilatation) strain state with maximum value  $-230 \times 10^{-8}$ . On the contrary, remarkable positive dilatation strain is concentrated on the coastline of the Charvak water reservoir, where large strain is about  $351 \times 10^{-8}$ .

**Keywords.** GNSS network, strain accumulation, finite element method.

## 1 Introduction

Tashkent region is located in the Middle Tien-Shan zone at the boundary two large components. It is a part of the post-platform mobile region and is located in the transition zone between the Tien-Shan orogenic territory and the Turan plate. The mountain ranges (Karzhantau, Chatkal and Kurami), covered by young structures in some areas, surround this field and decrease in southwest direction. Recent up thrusts and deflections characterize plain part of the territory [1, 2]. According the results are presented in map of Peak Ground Acceleration, the region belongs one of the two fields in the country of very high seismic activity (up to  $4.8 \text{ m/s}^2$ ) [3]. The magnitude of the maximum ground velocity must exceed values for 50 years  $50 \text{ cm / s}$  with probability  $P = 0.99$  according the analysis the velocity graphs of  $M=3.8-6.2$  earthquakes [4]. Significant velocity rates between  $30 \text{ mm/year}$  and  $60 \text{ mm/year}$  were found to the tectonic fault zones and mountainous part of the area, the flat, foothills zones show velocity rate up to  $15 \text{ mm / year}$  [5]. Charvak water reservoir with area around  $40 \text{ km}^2$  and with the volume of 2 billion m was constructed for hydropower generating, irrigation purpose and for controlling river flow. In 1970, construction of the

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NSSP) were used. Coordinates of the test network estimated by six solutions have both different epochs and different datum. For accurate calculation of station displacement vectors, it is necessary to take into account the measurement errors that arise as a result of the choice of the reference system. As a result, “rotation” and “deformation” of the network arise. To eliminate the effect of visible “rotation” and “deformations” it is recommended to use the transformation methods. This study was aimed to compare the coordinate difference between the campaign’s epochs and referencing them into the first epoch of measurements by using 3D Helmert transformation method for the possibility of an accurate assessment of network deformations and strain accumulation computation.

## 2 Materials and methods

### 2.1 Datum investigation with 3-D Helmert transformation

Usually, the processing of geodetic measurements to identify modern movements of the earth's crust is performed on relatively stable geological structures. However, for the study area, there is not yet a sufficiently accurate tectonic model and, accordingly, there is no sure confirmation that the points will remain stable. The territory of the Tashkent region is subject not only to modern tectonic movements, but also a change in the water level in the Charvak reservoir can be the cause of the induced disturbances of the Earth's surface. One of the solutions to the problem is the implementation in network processing of continuously working stations, for example IGS data. Taking into account that our network was processed relative to several high-precision stations of the IGS, in this study, all 31 points were used to perform the transformation procedure. Another reason was to look at how and where there will be more horizontal movement for further redefinition of the regional tectonic model.

The network adjustment error is usually influenced by two factors: orientation and scale of the network. Therefore, a 7-parameter transformation method was chosen in the work to analyze deformation between two epochs and strain parameters in the geodetic network, three-dimensional conformal (it preserves shapes of objects) coordinate transformation is also known as seven-parameter similarity transformation was applied. It converts separate surveys into a common reference coordinate system and it can be thought of as a three-step process: scaling, rotation and translation. The seven parameters of the transformation between convertible  $(x,y)$  and reference  $(X,Y)$  systems (epochs) - one scaling ( $m$ ), three rotations ( $R_x, R_y, R_z$ ) and three rotations translations ( $T_x, T_y, T_z$ ) can be determined uniquely with the minimum of three common points for both systems [7, 8]:

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_i = \begin{bmatrix} T_x \\ T_y \\ T_z \end{bmatrix} + (1+m) \begin{bmatrix} 1 & -R_z & R_y \\ R_z & 1 & -R_x \\ -R_y & R_x & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}_i \quad (1)$$

When more than three stations are present, the solution is obtained by the conventional least square adjustment procedure and the equations system can be written in the matrix form:

$$A_i dp = L + V \quad (2)$$

Where  $L$ -coordinate difference,  $V$ -vector of residuals. The design matrix  $A_i$  for station  $i$  of the are defined as

$$A_i = \begin{bmatrix} 1 & 0 & 0 & x_i & 0 & 0 & y & z & 0 & 0 & z & -y \\ 0 & 1 & 0 & 0 & y & 0 & x & 0 & z & -z & 0 & x \\ 0 & 0 & 1 & 0 & 0 & z & 0 & x & y & y & -x & 0 \end{bmatrix} \quad (3)$$

The adjustment of the slightly overdetermined system (2) via normal equations yields the parameter vector  $dp$  of unknown transformation parameters (scaling, three rotations and three rotations translations)  $dp = [dT_x \ dT_y \ dT_z \ dm \ d\omega_x \ d\omega_y \ d\omega_z]^T$

$$dp = (A^T A)^{-1} A^T L \quad (4)$$

Once parameters of the transformation are determined, the coordinates  $(x, y, z)$  are transformed to new  $(X, Y, Z)$  coordinate system using eq. (1). The coordinate values for all sessions were transformed to the topocentric coordinate system  $(E, N, U)$ :

$$\begin{bmatrix} E_n \\ N_n \\ U_n \end{bmatrix} = \begin{bmatrix} -\sin L_0 & \cos L_0 & 0 \\ -\sin B_0 \cos L_0 & -\sin B_0 \sin L_0 & \cos B_0 \\ \cos B_0 \cos L_0 & \cos B_0 \sin L_0 & \sin B_0 \end{bmatrix} \begin{bmatrix} X_n - X_0 \\ Y_n - Y_0 \\ Z_n - Z_0 \end{bmatrix} \quad (5)$$

where  $(X_0, Y_0, Z_0)$  and  $(B_0, L_0)$  are geocentric and geodetic coordinates (latitude and longitude) respectively of the center of gravity of the network (marked as red circle on fig.1). First epoch (Sept. 2009) of the measurement was choosing as reference for further calculations and the horizontal displacement vectors of pairs first – second (Nov. 2009), first – third (June 2010), first – fourth (Nov. 2010), first – fifth (May 2011) and first -six (Nov. 2011) epochs of each GNSS monitoring station was calculated as

$$R_n = \sqrt{(N'_n - n_n)^2 + (E'_n - e_n)^2} \quad (6)$$

$dU_n = U'_n - u_n$  height component variations will be used for estimation of the network vertical deformation. A software package in Delphi has been developed for the assessment of the datum differences between 2009 and 2011 by implementing the 3D Helmert transformation method.

Data analysis was performed in the ArcGIS 10.1.

## 2.2 Estimation of strain accumulation by finite element model

The calculation of the network strain by the finite element method was used to assess the deformation effect. The principles and basics of finite element method are generally known and are described in numerous publications [9, 10]. In the first step, the network has been constructed of finite elements (triangles) based on the Delaunay triangulation (Green and Sibson, 1978) (fig.1). Local strain field was computed for each triangle in the network. The strain values  $(E)$  on the earth's surface can be expressed in terms of displacements between adjacent stations at initial and final epochs  $(l_0, l_t)$  [11]:

$$E = \frac{|l - l_0|}{l_0} \quad (7)$$

This equation is created for each baseline of a triangle. The coordinates of GNSS points were represented in the Mercator projection for calculating distances (radius-vectors) between the nearest stations.

Finally, all individual results are integrated for whole investigated region by creating homogeneous surface with the nearest neighbor interpolation method. It is based on comparison of the distribution of distance  $d$  between a point  $x$  and the nearest neighboring points  $y$  of a set of randomly distributed data [12]:

$$d(x, y) = \|x - y\| = \sqrt{(x - y)(x - y)} = ((\sum_i (x_i - y_i))^2)^{1/2} \quad (8)$$

The method has been investigated and used in recent work for assessment of normal heights surface for Fergana valley territory in Uzbekistan [13]. It showed more reliable results than commonly used polynomial interpolation method for creating surface over the high mountains region.

### 3 Results

The transformation parameters translations ( $T_x, T_y, T_z$ ), scale ( $m$ ) and rotations ( $\omega_x, \omega_y, \omega_z$ ) between the first-reference and subsequent (from second to sixth) epochs are given in the Table 1. The result revealed that there is significant translation and rotation in the network, while the scale of the network remains almost constant during two years period (from September 2009 to November 2011).

**Table 1.** The transformation parameters between different epochs of measurements

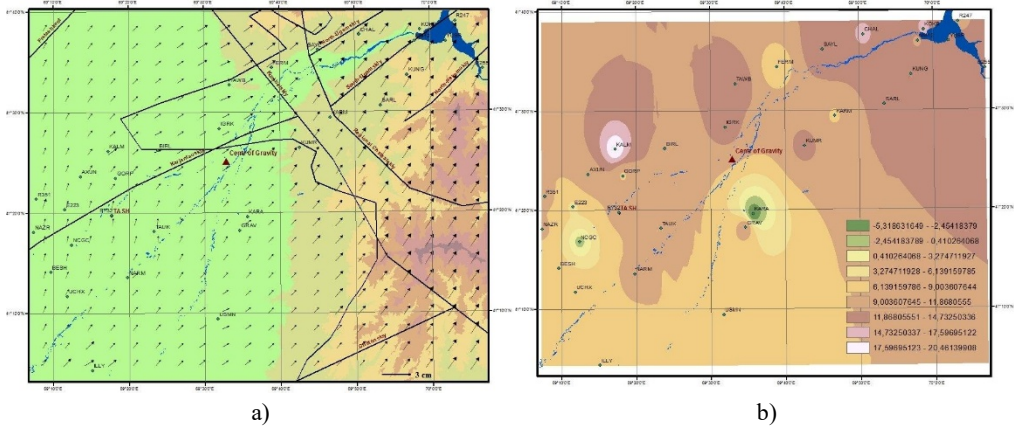
<i>Epochs</i>	<i>Period</i>	$T_x, m$	$T_y, m$	$T_z, m$	$m$	$\omega_x, sec$	$\omega_y, sec$	$\omega_z, sec$
1-2	09.2009-12.2009	-9.96	0.02	4.12	0.99	0.076	-0.294	0.185
1-3	09.2009-06.2010	-5.16	-2.04	-1.90	1.00	0.025	-0.028	0.160
1-4	09.2009-11.2010	2.48	-5.53	6.20	0.99	0.258	-0.006	-0.110
1-5	09.2009-05.2011	-6.99	1.35	9.24	0.99	0.157	-0.295	0.106
1-6	09.2009-11.2011	4.29	8.72	21.16	0.99	0.289	-0.112	-0.044

The horizontal displacement vectors were calculated using the eq. 5 and, for a more visual representation of the deformation of the whole region, the values were interpolated over the study area (eq. 7). The presented in fig. 2a result demonstrate horizontal displacements of the network with rates between 2 cm and 21 cm during whole observation period (first and sixth epochs) from September 2009 to November 2011. Analysis of calculated displacement vectors has been carried out separately for different parts of the region. The investigated field was conditionally divided into three main parts. The first one belongs to the Charvak coastal zone (KOKB, NM12, YUSP, CHAL, KUNG, R247, R255, SAYL, SARL, KARM, FERM) and divided from the others by the Kumbel fault. The second and the third are separated from each other by the largest Karjantau depression and hereinafter called conditionally the Northern coastal zone of the Chirchik river (AXUN, BIRL, E223, GORP, IGRK, KALM, NAZR, R351, TAWB) and the Southern coastal zone of the Chirchik river (KUMR, GRAV, KARA, TAU, R732, NARM, NCGC, BESH, UCHX, USMN, ILLY). It should be noted that deformations in the Chirchik river valley are less (about 1 cm) than in the coastal part.

The stations located in Northern coastal part of the river have displacement rate from 4 cm to 10 cm and the stations located in the Southern coastal zone have a displacement rates from 2 cm to 17 cm. Moreover, the stations located closely to a coastal part of the Charvak

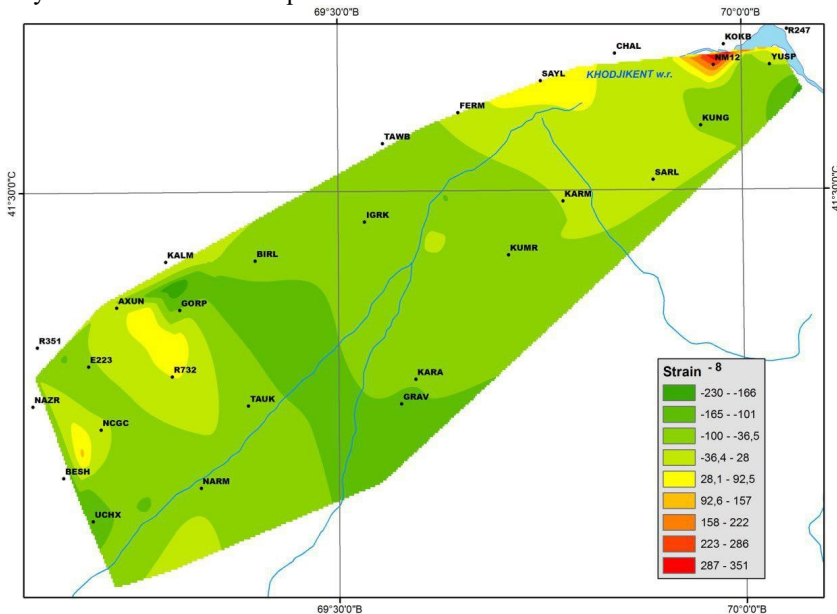
reservoir (R247, NM12, R255, YUSP) have a maximum displacement rates in this zone between 13 cm and 20 cm. There is a tendency to rotational movement along the Kumbel and Karjantau faults (fig2a).

The presented in fig. 2b result demonstrate vertical displacements of the network with rates between - 5 cm and 20 cm during the two years observation period. Station (KALM) located in this region shows relative to other stations a high rate of vertical displacement 20 mm, the cause of which may mainly be instrumental (antenna information, et al.) errors than tectonic effects. Therefore, this station was excluded from further analysis. It can be concluded that for this region, horizontal displacements are a consequence of both tectonic and hydrological processes. While vertical deformations are the result of most tectonic phenomena



**Fig.2** Horizontal (a) and vertical (b) deformations of the network during 2009-2011

The result revealed that there are significant horizontal displacements, therefore, it is necessary to estimate the strain accumulation regardless of the datum and the displacement vectors may be used to derive this parameter.



**Fig. 3.** The map of strain values based on GNSS data over region



Fig. 3 shows the principal strains rate distribution. Most of the area can be considered to be in a high compression (negative dilatation) strain state. Strain rate for the southwestern part near stations GRAV, KARA, AXUN, GORP as maximum value with  $-230 \times 10^{-8}$ . Minimum values of extension are found in with a value of  $10 \times 10^{-8}$  in flat areas. The results are very similar to the [5]: the strain rate at intersection of active faults Karzhantau, Kumbel and Ugam confirmed 80% of the value major shear stress caused by the tectonic movements of the whole region. On the contrary, remarkable positive dilatation strain is concentrated on the coastline of the water reservoir, where large strain is about  $351 \times 10^{-8}$ . The result clear demonstrates that, along strain caused by the tectonic movements, the water level variations in the reservoir is also a major factor determining the displacement and stability of the area.

## 4 Conclusions

The effect of the deformation processes in Tashkent region, was studied by strain deformation calculation with GNSS data. In this regard, as the first step, GNSS stations coordinates were transformed to a datum of the first epoch using the 3D Helmert transformation method, and the horizontal displacement vectors were determined for each station. The result revealed that there are significant horizontal displacements with a maximum value up to 20 cm in the network and vertical displacements with rates between - 5 cm and 20 cm. The calculation of the network strain was used to assess the network deformation. The network has been constructed of finite elements (triangles) based on the Delaunay triangulation. We found that most of the Tashkent region can be considered to be in a high compression (negative dilatation) strain state confirmed, surely, of the value major shear stress caused by the tectonic movements of the whole region. On the contrary, remarkable positive dilatation strain is concentrated on the coastline of the water reservoir, where large strain is about  $351 \times 10^{-8}$ . We can conclude that more GNSS campaigns in combination with gravity measurements are needed in this area in order to better constrain the relatively small deformation rates.

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