Method of determining the optimal version of the piezometer of gas distribution networks of medium and high pressure

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Abstract. The article deals with the issues of determining the optimal type of piezometric pressure graph in high-and medium-pressure gas pipelines in the design of gas distribution networks. Along with the most commonly used ways to reduce the cost of building gas distribution networks by finding the optimal configuration of gas pipelines, which give a great economic and environmental effect, it is necessary to rationally use the pressure drop provided to the network. This step in engineering practice allows you to additionally get money savings. The use of various schemes for supplying consumers with gas in cities and villages also has a great economic effect, but modern equipment allows you to make the transition to a single-stage scheme of gas distribution networks for cities. When designing gas distribution networks, the available pressure drop can be used by implementing various technical solutions, but the correct choice of pressures in the nodal points contributes to an economic effect. The designed configuration of the gas distribution network with the adopted type of piezometric graph can ensure reliable operation for a long time. The results obtained are recommended for use in the design of gas distribution networks of cities, other settlements and distribution networks of industrial enterprises

1 Introduction

Modern gas distribution systems are a complex of structures consisting of low, medium and high pressure networks, gas distribution stations, gas control points and installations. The multi-stage gas distribution system has become widespread. The gas passes sequentially through high-pressure, medium-pressure, and low-pressure gas pipelines [1].

Currently, in European countries and Russia, a single-stage gas distribution system with the installation of combined pressure regulators is increasingly being used. In this case, the combined pressure regulator can be installed in each entrance of a multi-storey building, each house, individual buildings.

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2 Literature review

The gas distribution scheme becomes flexible: independence of connection of any object is achieved, metal consumption is reduced, investments in construction are reduced by reducing the diameter of gas pipelines. In this case, the distribution gas network is completely designed for medium pressure. When choosing a dead-end gas network of medium pressure, it is necessary to make a technical and economic calculation, in which it is possible to determine the optimal shape of the piezometer, which will contribute to achieving the minimum cost of the gas distribution network.

The choice of the optimal pressure drop for dead-end networks is considered in the works [2, 3], but these recommendations and algorithms affect and are applicable only for low-pressure networks, and there are no recommendations for choosing the optimal form of the piezometric pressure drop graph for high-and medium-pressure networks. In this paper, we will consider this issue. The classical scheme of pressure distribution in a dead-end gas distribution network is shown in Figure 1



Fig. 1. Pressure change in the gas pipeline

3 Materials and methods

When designing gas distribution networks, it is necessary to be guided by both technical parameters: ensuring the required pressure in front of subscribers, sufficient reliability of gas distribution networks and mandatory safety of the subsequent safety of operation of these networks. But it is also very important to use economic parameters in your calculations. An interesting fact is that some technical recommendations can immediately provide economic efficiency. Often, in optimization tasks to improve the efficiency of gas distribu-

tion systems, they change the connection schemes of subscribers or find the most rational configuration of the gas distribution network [4 - 24]. We will consider the technical and economic calculation of a dead-end gas network of high (medium) pressure and will obtain a mathematical algorithm for determining the optimal shape of the piezometric graph in the design of gas distribution networks. Let's imagine a gas distribution network of a dead-end structure in Figure 2.



Fig. 2. Diagram of a dead-end gas network of high (medium) pressure

Gas networks are designed for a given pressure drop. The task of technical and economic calculation of dead-end gas networks is reduced to the choice of optimal diameters with a rational distribution of pressure differences between the sequentially connected sections of gas pipelines.

Dead-end gas pipelines are branched networks that feed gas at one point and distribute it to consumers. Any section of an extensive network has a one-way power supply, so the gas consumption for the sections is determined unambiguously. Gas costs for consumers are assumed to be equal Q_i and the length of the sections L_i .

The calculated pressure drop is set $\delta p = p_b^2 - p_e^2$. Index "b"-indicates the initial parameters, and index "e" - the final parameters. Consider the equations that determine the calculation

$$\mathbf{K} = b \cdot dl; \, \delta p = a \frac{Q^2}{4525} \cdot l \tag{1}$$

$$\sum_{1}^{n} k = \sum_{1}^{n} b \cdot a^{0,19} \cdot Q^{0,38} \cdot l^{1,19} \cdot \delta p^{-0,19}$$
(2)
$$\sum \delta p_{i} - \delta p = 0$$
(3)

The number of equations (3) is equal to the number of nodes with specified pressures, that is, the number of end points (points A, B, and C in Fig. 1)

Equations 2 and 3 define the problem, which is reduced to finding the minimum of the function $\sum_{i=1}^{n} k_i$. Let's write a Lagrange function and equate its partial derivatives to zero. We get a system of equations:

$$\frac{\partial \phi}{\partial \Delta p_i} = 0$$

The number of equations is equal to the number of unknowns. We introduce the limiting conditions 4, 5, 6.

$$\delta \mathbf{p}_1 + \delta_2 - \delta \mathbf{p} = 0 \tag{4}$$

$$\delta \mathbf{p}_1 + \delta_3 + \delta_4 - \delta \mathbf{p} = 0 \tag{5}$$

$$\delta \mathbf{p}_1 + \delta_3 + \delta_5 - \delta \mathbf{p} = 0 \tag{6}$$

We will write a Lagrange function:

$$\varphi = \sum_{1}^{5} ba^{0,19} \cdot Q^{0,38} \cdot l^{1,19} \cdot \delta p^{-0,19} + \lambda_{A} \cdot (\delta p_1 + \delta p_2 - \delta p) + \lambda_{B} \cdot (\delta p_1 + \delta p_3 + \delta p_4 - \delta p) + \lambda_{C} \cdot (\delta p_1 + \delta p_3 + \delta p_5 - \delta p)$$
(7)

where λ_A , λ_B , λ_C - undefined multipliers

Equate the partial derivatives of the function φ to zero:

$$\frac{\partial \varphi}{\partial \delta p_1} = -ba^{0,19} \cdot Q_1^{0,38} \cdot l_1^{1,19} \cdot 0,19\delta p_1^{-0,19} + \lambda_A + \lambda_B + \lambda_C = 0$$
(8)

$$\frac{\partial \phi}{\partial \delta p_2} = -ba^{0,19} \cdot Q_2^{0,38} \cdot l_2^{1,19} \cdot 0,19\delta p_2^{-0,19} + \lambda_A = 0$$
(9)

$$\frac{\partial \varphi}{\partial \delta p_3} = -ba^{0,19} \cdot Q_3^{0,38} \cdot l_3^{1,19} \cdot 0,19\delta p_3^{-0,19} + \lambda_B + \lambda_C = 0$$
(10)

$$\frac{\partial \varphi}{\partial \delta p_4} = -ba^{0,19} \cdot Q_4^{0,38} \cdot l_4^{1,19} \cdot 0,19\delta p_4^{-0,19} + \lambda_B = 0$$
(11)

$$\frac{\partial \varphi}{\partial \delta p_5} = -ba^{0,19} \cdot Q_5^{0,38} \cdot l_5^{1,19} \cdot 0,19\delta p_5^{-0,19} + \lambda_C = 0$$
(12)

By subtracting the corresponding equations 8, 9, 10, 11, 12, we exclude undefined factors. From equation 8, subtract 9, 10, and from equation 10, subtract equations 11 and 12.

$$Q_2^{0,\overline{38}} l^{1,19} \delta p_2^{-1,19} + Q_3^{0,38} l_3^{1,19} \cdot \delta p_3^{-1,19} - Q_1^{0,38} \cdot l_1^{1,19} \delta p_1^{-1,19} = 0 \quad (13)$$

$$Q_4^{0,38} l^{1,19} \delta p_4^{-1,19} + Q_5^{0,38} l_5^{1,19} \delta p_5^{-1,19} - Q_3^{0,38} l_3^{1,19} \delta p_3^{-1,19} = 0$$
(14)

The number of equations is equal to the number of nodes with undefined pressures. Equation 13 represents the balance of expressions of the type $Q_i^{0,38} \cdot l^{1,19} \cdot \delta p^{-1,19}$ for node I, and 14 for node II. If the gas flow approaches the node, then a minus sign is provided before the expression $Q_i^{0,38} \cdot l^{1,19} \cdot \delta p^{-1,19}$, if it departs from the node – a plus sign.

4 Results of research

These equations allow us to determine the economically optimal pressure differences for each section.

We call it

$$A_i = Q_i^{0,38} \cdot l^{1,19} \tag{15}$$

(18)

(1.0)

then for a branched network we have:

$$\sum \delta p_i = \delta p \tag{16}$$

$$\sum A_i \, \delta p_i^{-1,19} = 0 \tag{17}$$

The balances in the nodes are not observed, as shown by equation 18:

$$A_i \, \delta p_i^{-1,19} = \Delta$$

Σ. where Δ is the balance discrepancy in the node.

The correction nodal pressures $\Delta \delta p$ are obtained from the equations: -1.19 Λ Sp -1.19 Λ Sp -1.19

$$A_{2}\delta p_{2}^{-1,19} + A_{3}\delta p_{3}^{-1,19} - A_{1}\delta p_{1}^{-1,19} = \Delta_{I}$$
(19)

$$A_4 \delta p_4^{-1,19} + A_5 \delta p_5^{-1,19} - A_3 \delta p_3^{-1,19} = \Delta_{II}$$
(20)

By entering the correction nodal pressures Δp_{I} and Δp_{II} , we obtain:

$$A_{2}(\delta p_{2} + \Delta p_{I})^{-1,19} + A_{3}(\delta p_{3} + \Delta p_{I} - \Delta p_{II})^{-1,19} - A_{1}(\delta p_{1} + \Delta p_{I})^{1,19} = 0 \quad (21)$$

$$A_{1}(\delta p_{4} + \Delta p_{II})^{-1,19} + A_{5}(\delta p_{5} + \Delta p_{II})^{-1,19} - A_{3}(\delta p_{3} - \Delta p_{II} + \Delta p_{I})^{-1,19} = 0 \quad (22)$$

Decomposing the expressions in parentheses in the Maclaurin series we get a system of

equations:

$$\sum_{I} A_{i} \, \delta p_{i}^{-1,19} - 1,19 \sum_{I} \frac{A_{i} \delta p_{i}^{-1,19}}{\delta p_{i}} \Delta p_{I} + 1,19 \frac{A_{3} \delta p_{3}^{-1,19}}{\delta p_{3}} \Delta p_{II} = 0$$
(23)

$$\sum_{II} A_i \, \delta p_i^{-1,19} - 1,19 \sum_{II} \frac{A_i \delta p_i^{-1,19}}{\delta p_i} \, \Delta p_{II} + 1,19 \frac{A_3 \delta p_3^{-1,19}}{\delta p_3} \Delta p_I = 0$$
(24)

The values of the correction pressure losses we get the equations:

$$\Delta p' = \frac{\sum A_i \delta p_i^{-1,19}}{1,19 \sum \frac{A_i \delta p_i^{-1,19}}{\delta p_i}};$$
(25)

$$\Delta p'' = \frac{\sum \Delta P'_{cy} \left(\frac{A\delta p^{-1,19}}{\delta p}\right)_{y.c.y}}{1.19 \sum^{A_i \delta p_i^{-1,19}}};$$
(26)

$$\Delta p = \Delta p' + \Delta p'' \tag{27}$$

where $\Delta p'$ is the part of the correction without taking into account the influence of neighboring nodes;

 Δp " - part of the correction that takes into account the influence of neighboring nodes;

 $\Delta p'_{c.v.}$ - the first approximation of the correction in the neighboring node.

The value of $\Delta p'_{c.y.}$ is multiplied by $(\frac{A\delta p^{-1,19}}{\delta p})$ of the section that has a neighboring node. The number of terms $\sum \Delta p'_{c.y.}$ $(\frac{A\delta p^{-1,19}}{\delta p})$ is equal to the number of neighboring nodes. When determining the correction, keep in mind that an expression of the type $\frac{A_i \delta p_i^{-1,19}}{\delta p_i}$ is always positive.

5 Conclusions

The developed technique of technical and economic calculations of dead-end gas networks of medium and high pressure. This technique allows for the specified pressure differences $P_b^2 - P_e^2$. to determine the economical diameters with the optimal distribution of pressure differences between successive sections.

As a result of preliminary calculations, the residual in the nodes is obtained. To minimize the discrepancy, we reduce or increase the correction pressures in the nodes to satisfy the economical node equations.

There are many possible piezometers, and the implementation of design solutions for each of them corresponds to a certain cost of a dead-end network of medium and high pressure. This technique of technical and economic calculation of a dead-end gas network of medium (high) pressure makes it possible to find the optimal shape of the piezometer, at which the cost of the network will be minimal.

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