Determination of optimal values for the technical characteristics of construction machinery unit with application of fractional linear programming

Victoria Fomicheva, Anna Zanina, and Anton Radaev*

Peter the Great St.Petersburg Polytechnic University, 195251 Polytekhnicheskaya str., 29, St.Petersurg, Russia

Abstract. Paper covers issues connected to the determination of the technical characteristics of construction machinery unit performing a certain category of work. On the basis of the results of the review and analysis of scientific works concerning the problem under consideration the key disadvantages have been identified for the existing techniques. Optimization model for determination of the technical characteristics of construction machinery unit has been created. Initial form of the model is not linear toward unknown variables but it can be transformed to the linear form that allows application of simplex method for efficient solution of the problem. The created model has been implemented on a practical case – the obtained results indicated the adequacy of the developed tool.

1 Introduction

Modern conditions of the construction industry's development are characterized by the large variety of corresponding machinery models with different technical characteristics and, as sequence, different rental costs and productivity indicators. That circumstance determines the high relevance of the problems connected to formation of optimal structure for construction machinery fleet on the basis of time and cost criteria in conditions of complex structure of the construction projects and large amount of variants for machines' design and productivity. The relatively sophisticated approach is based on the use of the modern simulation and optimization techniques that are based on mixed-integer linear programming [1–3], particle swarm optimization [4], ant colony optimization [5], genetic algorithms [6], etc. The corresponding scientific developments assume creation and implementation of complex mathematical models and algorithms to take into account the large number of important factors that have influence on the machinery fleet's efficiency indicators and obtain adequate results. Still, the corresponding calculations' conduction process require high qualification in the field of mathematics and programming for the person solving the task. The more simple (in terms of practical application) approach is based on the ranking of the available machinery variants (models) connected to the certain

^{*} Corresponding author: tw-inc@yandex.ru

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category of work with further selection of the appropriate number of the most preferred machinery models (in accordance with the rank and available number) to provide the required productivity of construction machinery complex for each category of work. To calculate the rank for machinery variants under consideration, it's necessary to justify the composition and values of the reference characteristics for the machinery unit - it will allow to calculate the deviations between actual and reference values of characteristics for each machinery model and determine the rank in accordance with the following principle: the less the value of generalized deviation for machinery model, the bigger the value of corresponding rank. However, the preliminary analysis of the scientific works connected to the justification of the machinery unit's characteristics showed the lack of effective tools providing calculation of reference values for machinery characteristics with full and objective taking into account of cost and productivity indicators. On the basis of the features indicated above the conclusion has been made about the necessity for conduction of the research aimed to the creation of the tools for the determination of the reference technical characteristics of construction machinery unit. The main tasks of the research have been formulated as follows:

- 1. Carrying out of the review and analysis of the modern scientific developments in the research field.
- 2. Creation of the optimization model for determination of optimal values for the technical characteristics of construction machinery unit with application of fractional linear programming.
- 3. Implementation of the created model on a practical example.

The object of the research is construction technological process that assumes performing of the certain category of work by cyclic-operating machinery unit within limited time interval. The subject of the research is the characteristics of the mentioned above process in terms of technical and cost characteristics of the machinery unit.

At the initial stages of the research the review and analysis of the scientific developments [1–17] in the field of determination of characteristics for the machinery unit within the technological (particularly, construction) process. Most scientific developments assume determination of the machinery's characteristics by selection of the most appropriate variant through the application of hierarchy analysis methods [7-16], fuzzy logic techniques [17, 18] and their combination [19]. The common disadvantage of the corresponding procedures is connected to the direct dependence of the solution search's laboriousness and the number of alternative variants of machinery. Additional disadvantages of the mentioned above categories of scientific developments are the following:

- dependence of the results on the expert opinion with a certain degree of subjectivity; the difficulty of providing an objective assessment of the objects of analysis [7-16,19];
- the difficulty of objective description of the interconnection between different categories of parameters (including qualitative and quantitative) [17, 18].

Mentioned above conclusions determined the necessity for creation of the optimization model which would provide determination of the technical characteristics of cyclicoperating construction machinery unit with adequate and objective account of the criteria of its productivity and economic efficiency. More detailed information is presented in the next sections of the work.

2 Methods

At the intermediate stage of the optimization model has been created on the basis of preliminarily formulated main provisions and supposed composition of initial data and unknown variables. Detailed description of the model's structure is provided within the corresponding subsections.

2.1 Main provisions

Main provisions of the elaborated model are the following:

- the object under consideration is the technological process connected to the handling of cargo units (CU) by a unit of construction handling machinery (CHM) of cyclic action with battery power supply within the corresponding technological cycles, implemented within a limited time interval.
- the technological cycles implemented by the CHM unit correspond to a certain category of work and therefore have similar configuration parameters of the corresponding technological routes.
- the similarity of the configuration of technological routes implemented by the CHM unit within the corresponding cycles of CU processing makes it possible to form the most probable (median) technological route, the implementation of which within the considered time interval will ensure the productivity of the CHM unit, equal to the actual productivity of the CHM during the implementation of technological routes with similar, but not identical configuration.
- the general composition of the CHM technical characteristics includes the main technical characteristics that directly determine the rental cost for a CHM unit, and additional characteristics that do not significantly affect the rental cost. The list of the main characteristics for the considered CHM is presented in Table 1.

No.	Name of the technical characteristic for CHM unit		Designation in the expressions for calculated characteristics		
			general	customized	
i	-	MSU	-	-	
1	Load carrying capacity value	kg	x_1	G_{c}	
2	Inverse value of stationary travel speed with CU	h/km	<i>x</i> ₂	$1/v_{ m trv}^+$	
3	CU lift height value	m	<i>x</i> ₃	$H_{ m lft}$	
4	Inverse value of the lifting speed for pickup device with CU	s/m	<i>x</i> ₄	$1/v_{ m lft}^+$	
5	Turning radius value	m	<i>x</i> ₅	$R_{\rm trn}$	
6	Nominal energy value for accumulator storage battery (ASB)	J	x_6	$A_{ m ASB}$	

Table 1. The list of the main characteristics for the considered CHM.

 the dependence of the rental cost for a CHM unit on its main technical characteristics is described by a linear analytical model defined by the expression:

$$\widetilde{y} = a_0 + \sum_{i=1}^{z} a_i \cdot x_i, \qquad (1)$$

where \tilde{y} – predictive value of the rental cost for a CHM unit, MU;

 a_0 – cost constant, MU;

- i index of CHM technical characteristic; i = 1, 2, ..., z;
- z number of CHM technical characteristic, units;
- a_i model parameter coefficient of proportionality of the value of the rental cost for a CHM unit to the value of technical characteristic *i* (*i* = 1, 2, ..., *z*), MU/*MSU*;

MSU denotes a variable measure unit, the description of which is presented in Table 1); x_i – value of technical characteristic *i* (*i* = 1,2,...,*z*), *MSU*.

- the configuration of the technological route describes the trajectory of the spatial movement of the CHM unit during the implementation of technological cycle and includes straight and curved (turns) sections;
- the passage of straight sections is carried out by a CHM unit at a stationary travel speed (for example, in the process of CU's transportation from the place of pickup to the place of release) or at a shunting travel speed (during operations of CU pickup or release).
- the passage of curved sections is carried out by a CHM unit only at shunting speed.
- there is a certain relationship between the travel speed of a CHM unit without CU and with it, the same for both stationary and shunting speeds.
- there is a certain ratio between the stationary and shunting travel speeds of a CHM unit, which is the same for the movement both with and without CU.
- there is a certain ratio between the speeds of the vertical movement of a CHM unit's pickup device with CU and without it, the same for the pickup device's lifting and lowering.
- there is a certain ratio between the speeds of lowering and lifting the load gripper, which is the same for the pickup device's movement both with and without CU.
- there is a certain ratio between the total mass of a CHM unit and its load carrying capacity.
- there is a certain ratio between the mass of a CHM unit's pickup device and its load carrying capacity.
- it is necessary to determine the values of the CHM technical characteristics, at which the maximum value of money saving for the rental of the CHM unit, referred to the average duration of the implemented technological cycle, is ensured.

2.2 Model description

Source data and unknown variables connected to the created optimization model are presented in Table 2 and Table 3 respectively.

Calculated characteristics used within the model and independent of its unknown variables, are presented in Table 4.

No.	Name of the source data element	Meas. unit	Designation / expression
1	Parameters of source data structure		
1.1	Number of CHM technical characteristics	unit	Z
2	Indexes		
2.1	Index of CHM technical characteristics	-	<i>i</i> = 1, 2,, <i>z</i>
3	Source data specified for technological process		<u>.</u>
3.1	Duration of the time interval of CHM continuous operation	h	T^{Σ}
3.2	CHM time utilization ratio	-	γ_{T}
3.3	Safety factor of the actual used energy volume for ASB ⁽²⁾	-	$\delta_{\scriptscriptstyle{ m ASB}}$
3.4	Maximal renting cost for a CHM unit	MU	C^{\max}
3.5	Cost constant ⁽³⁾	MU	<i>a</i> ₀
3.6	Minimal (maximal) value of average cycle time ⁽⁴⁾	S	$T_{\rm c}^{\rm min(max)}$

Table 2. Source data for the created optimization model.

No.	Name of the source data element	Meas. unit	Designation /
		(1)	expression
4	Source data specified for each CHM technical characteristic i (i	=1,2,,z)	-
4.1	Parameter of the analytical model, corresponding to the technical characteristic ⁽³⁾	MU/ <i>MSU</i>	a_i
4.2	Minimal (maximal) value of the characteristic ⁽⁴⁾	MSU	$x_i^{\min(\max)}$
5	Source data specified for technological route		
5.1	Total length of CHM straight-line movements at a stationary speed with CU (without CU)	m	$L_{ m trv}^{+(-)}$
5.2	Total length of CHM straight-line movements at a shunting speed with CU (without CU)	m	$L_{ m shn}^{+(-)}$
5.3	Turning radius calculated value	m	R
5.4	Turning angle value	rad	φ
5.5	Number of turns with CU (without CU)	unit	$n_{ m trn}^{+(-)}$
5.6	Height of CU lifting / lowering during pickup (release)	m	$H_{\rm pick (rel)}$
5.7	Average duration of additional operations during CU pickup (CU release)	S	$\Delta t_{\rm pick(rel)}$
6	Source data specified for construction handling machines' operation	tion	
6.1	Mass of CU being processed	kg	m
6.2	Gravity acceleration	m/s ²	g
6.3	Ratio of the CHM travel speed without CU to the CHM travel speed with CU	-	$k_{ m trv}$
6.4	Ratio of the CHM shunting speed of the CHM stationary speed	-	k _{trv s}
6.5	Ratio of the lifting speed of the CHM pickup device without CU to the lifting speed of the CHM pickup device with CU	-	$k_{ m lft}$
6.6	Ratio of the CHM pickup device lowering speed to the CHM pickup device lifting speed	-	$k_{ m lwr}$
6.7	Ratio of the mass of a CHM unit to its carrying capacity	-	k _{mas}
6.8	Ratio of the mass of a CHM unit's pickup device to CHM unit's carrying capacity	-	$k_{ m PD}$
6.9	Coefficient of resistance to CHM movement with stationary speed	-	$f_{ m trv}$
6.10	Coefficient of resistance to CHM movement with shunting speed	-	$f_{ m trv\ s}$
6.11	Efficiency of the CHM movement mechanism providing stationary speed	-	$\eta_{ m trv}$
6.12	Efficiency of the CHM movement mechanism providing shunting speed	-	$\eta_{ m trv\ s}$
6.13	Efficiency of the lifting mechanism for CHM unit's pickup device	-	$\eta_{ m lft}$
6.14	ASB limit discharge ratio	-	$\mu_{ m ASB}$

Table 2. Source data	for the created	optimization mode	(continued).

Note:

(1) the measure unit indicated for certain elements of source data and specified as MSU has a different meaning depending on the index of CHM technical characteristic (for more information, see Table 1);

⁽²⁾ Value of source data element must correspond to the condition $\delta_{ASB} \in [0;1]$

- (3) source data elements can be calculated on the basis of the set of CHM samples with further solving of system of equations with application of Cramer's rule;
- (4) source data elements can be calculated by the statistical processing of information connected of the set of CHM samples (in terms of values of technical characteristics under consideration) and

also must take into account features of the technological process's implementation – for example, CHM load carrying capacity G_c must be equal or higher the CU mass m, turning radius $R_{\rm trn}$ must be close to the corresponding calculated value of technological route R, etc.

No.	Name of the unknown variables' category	Meas. unit	Designation / expression	
1	Unknown variables of the base model (original unknown va	riables)		
1.1	Value of CHM technical characteristic ⁽²⁾ i ($i = 1, 2,, z$)	MSU	x_i	
2	Unknown variables of the modified model (modified unknown variables)			
2.1	Inverse value of the average cycle time, implemented by a CHM unit during CU processing	s^{-1}	$z_0 = \frac{1}{T_c}$	
2.2	The ratio of the value of CHM technical characteristic i ($i = 1, 2,, z$) to the value of the average cycle time	<i>MSU</i> /s	$z_i = x_i \cdot z_0 = \frac{x_i}{T_c}$	

Table 3. Unknown variables for the created optimization model.

Note:

(1) the measure unit indicated for certain categories of unknown variables and specified as MSU has a different meaning depending on the index of CHM technical characteristic (for more information, see Table 1);

⁽²⁾ alternative designations of unknown variables $\{x_i\}$ in expressions in items 1.1 and 2.2 are presented in Table 1.

Table 4.	Calculated	characteristics	for the	created	optimization mode	1.

No.	Name of calculated characteristic	Meas. unit	Expression
1	Characteristics of the duration of	the technolog	cial cycle
1.1	Specific average value of the distance of CU horizontal transportation provided by a CHM unit at a stationary speed	m	$\Lambda_{\rm trv} = L_{\rm trv}^+ + \frac{L_{\rm trv}^-}{k_{\rm trv}}$
1.2	Specific average value of the distance of CU horizontal transportation provided by a CHM unit at a shunting speed	m	$\Lambda_{\rm trvs} = \varphi \cdot R \cdot \left(n_{\rm trn}^+ + \frac{n_{\rm trn}^-}{k_{\rm trv}} \right) + L_{\rm shn}^+ + \frac{L_{\rm shn}^-}{k_{\rm trv}}$
1.3	Specific average value of the distance of CU vertical transportation provided by a CHM unit's pickup device	m	$\begin{split} \Lambda_{\mathrm{lft}} &= H_{\mathrm{pick}} \cdot \left(\frac{1}{k_{\mathrm{lft}}} + \frac{1}{k_{\mathrm{lwr}}} \right) + \\ &+ H_{\mathrm{rel}} \cdot \left(1 + \frac{1}{k_{\mathrm{lft}} \cdot k_{\mathrm{lwr}}} \right) \end{split}$
1.4	Average value of the duration of a part of the cycle, which does not depend on the CHM technical characteristics	S	$\Delta T = \Delta t_{\rm pick} + \Delta t_{\rm rel}$
2	Characteristics connected to the e implementation of technological		nption by a CHM unit during the
2.1	Ratio of the average value of the energy spent on CHM unit's movement at a stationary speed to the value of the load carrying capacity	J/kg	$\Theta_{\rm trv} = \frac{g \cdot f_{\rm trv}}{\eta_{\rm trv}} \cdot k_{\rm mas} \cdot \left(L_{\rm trv}^+ + L_{\rm trv}^-\right)$

No.	Name of calculated characteristic	Meas. unit	Expression
2.2	Ratio of the average value of the energy spent on CHM unit's movement at a shunting speed to the value of the load carrying capacity	J/kg	$\Theta_{\text{trv s}} = \frac{g \cdot f_{\text{trv s}}}{\eta_{\text{trv s}}} \cdot k_{\text{mas}} \times \\ \times \left(\varphi \cdot R \cdot \left(n_{\text{trn}}^+ + n_{\text{trn}}^- \right) + L_{\text{shn}}^+ + L_{\text{shn}}^- \right)$
2.3	Ratio of the average value of the energy spent on a CHM pickup device's lifting / lowering to the value of the load carrying capacity	J/kg	$\Theta_{\rm lft} = \frac{g}{\eta_{\rm lft}} \cdot k_{\rm mas} \cdot k_{\rm PD} \cdot 2 \cdot \left(H_{\rm pick} + H_{\rm rel}\right)$
2.4	Average value of the energy consumed by a CHM unit within the cycle, independent of the technical characteristics of the equipment	J	$\Delta A = m \cdot g \cdot \left(\frac{f_{\text{trv}}}{\eta_{\text{trv}}} \cdot L_{\text{trv}}^{+} + \frac{f_{\text{trv}\text{s}}}{\eta_{\text{trv}\text{s}}} \times \right)$ $\times \left(\varphi \cdot R \cdot n_{\text{trn}}^{+} + L_{\text{shn}}^{+} \right) + \frac{1}{\eta_{\text{lft}}} \cdot \left(H_{\text{pick}} + H_{\text{rel}} \right) $
2.5	Minimal permissible conditional value of ASB nominal energy	J	$A_{\text{ASB}}^{\text{condmin}} = x_6^{\text{consmin}} + \left(x_6^{\text{max}} - x_6^{\text{min}}\right) \cdot \delta_{\text{ASB}}$

Table 4. Calculated characteristics for the created optimization model.

Initial form of the optimization model corresponding to the main provisions specified in subsection 2.1 is described by the following expressions:

$$\begin{cases} \frac{C^{\max} - \left(a_{0} + \sum_{i=1}^{z} a_{i} \cdot x_{i}\right)}{\left(\Lambda_{trv} + \frac{\Lambda_{trvs}}{k_{trvs}}\right) \cdot x_{2} + \Lambda_{ift} \cdot x_{4} + \Delta T} \rightarrow \max; \qquad (2) \\ \frac{\left(\Theta_{trv} + \Theta_{trvs} + \Theta_{ift}\right) \cdot x_{1} + \Delta A}{\left(\Lambda_{trv} + \frac{\Lambda_{trvs}}{k_{trvs}}\right) \cdot x_{2} + \Lambda_{ift} \cdot x_{4} + \Delta T} \cdot T^{\Sigma} \cdot \gamma_{T} \cdot \mu_{ASB} \leq x_{6}; \qquad (3) \end{cases}$$

$$\left(\Lambda_{\text{trv}} + \frac{1}{k_{\text{trv}s}}\right) \cdot x_2 + \Lambda_{\text{lft}} \cdot x_4 + \Delta T$$

$$x_i^{\min} \le x_i \le x_i^{\max}, \ i = 1, 2, ..., z.$$
(4)

The expressions are based on the certain elements of the Table 4 with substitution of customized designations of technical characteristics for general designations in accordance with the information in Table 1.

Expression (2) represents objective function – money saving for the rental of the CHM unit, referred to the average cycle time – to be maximized. Expression (3) represents indirect constraints connected to the condition that total energy spent during the implementation of technological cycle by a CHM unit (taking into account ASB limit discharge ratio) must not exceed ASB nominal energy. Expression (4) describes the direct constraints for original unknown variables $\{x_i\}$.

It can be concluded that the model is not linear towards unknown variables $\{x_i\}$. However, expressions (2) – (4) include the elements corresponding to the fractional linear model and therefore can be transformed to the linear form by performing of the following changes: Substitution of the inverse value of the denominator in expressions (2) and (3) for the unknown variable z₀ = 1/T_c (item 2.1 in Table 3) with further replacement of original variables {x_i} by modified ones {z_i} in accordance with the expression

$$x_i = \frac{z_i}{z_0}; \tag{5}$$

corresponding results are described by the following expressions:

$$\frac{C^{\max} - \left(a_0 + \sum_{i=1}^{z} a_i \cdot x_i\right)}{T_c} = \left(C^{\max} - a_0\right) \cdot z_0 - \sum_{i=1}^{z} a_i \cdot z_i \to \max;$$
(6)

$$\left(\left(\Theta_{\rm trv} + \Theta_{\rm trv\,s} + \Theta_{\rm lft} \right) \cdot z_1 + \Delta A \cdot z_0 \right) \cdot T^{\Sigma} \cdot \gamma_{\rm T} \cdot \mu_{\rm ASB} \le x_6; \tag{7}$$

it's necessary to note that expression (5) is linear toward the variables z_0 , $\{z_i\}$; left part of the expression (7) is also linear towards the mentioned variables but the its right part is not (see expression (5).

2. Substitution of the expression (6) for two equivalent conditions defined by the following expressions

$$\int \left(\left(\Theta_{\text{trv}} + \Theta_{\text{trv s}} + \Theta_{\text{lft}} \right) \cdot z_1 + \Delta A \cdot z_0 \right) \cdot T^{\Sigma} \cdot \gamma_{\text{T}} \cdot \mu_{\text{ASB}} \le A_{\text{ASB}}^{\text{condmin}};$$

$$A^{\text{condmin}}_{\text{condmin}} = \zeta = z$$
(8)

$$A_{\rm ASB}^{\rm condmin} \cdot z_0 \le z_6. \tag{9}$$

3. Addition of integrity condition for the modified unknown variables z_0 , $\{z_i\}$; the mentioned condition is connected to the following expression:

$$\left(\Lambda_{\rm trv} + \frac{\Lambda_{\rm trv\,s}}{k_{\rm trv\,s}}\right) \cdot z_2 + \Lambda_{\rm lft} \cdot z_4 + \Delta T \cdot z_0 = 1.$$
⁽¹⁰⁾

- 4. Transformation of the expression (4) through the replacement of the original variables in accordance with the expression (5) and further multiplication of all parts of the expression by z_0 .
- 5. Addition of direct constraints for the variable z_0 with the use of inverse values of specific initial data elements (item 3.6 in Table 2)

As the result, the modified optimization model is defined by the following expressions

$$\left(C^{\max} - a_0\right) \cdot z_0 - \sum_{i=1}^{z} a_i \cdot z_i \to \max;$$
(11)

$$\left(\left(\Theta_{\text{trv}} + \Theta_{\text{trv s}} + \Theta_{\text{lft}} \right) \cdot z_1 + \Delta A \cdot z_0 \right) \cdot T^{\Sigma} \cdot \gamma_{\text{T}} \cdot \mu_{\text{ASB}} \le A_{\text{ASB}}^{\text{condmin}};$$
(12)

$$A_{\text{ASB}}^{\text{condmin}} \cdot z_0 \le z_6; \tag{13}$$

$$\left(\Lambda_{\rm trv} + \frac{\Lambda_{\rm trv\,s}}{k_{\rm trv\,s}}\right) \cdot z_2 + \Lambda_{\rm lft} \cdot z_4 + \Delta T \cdot z_0 = 1; \tag{14}$$

$$\frac{1}{T_{\rm c}^{\rm max}} \le z_0 \le \frac{1}{T_{\rm c}^{\rm min}};\tag{15}$$

$$x_i^{\min} \cdot z_0 \le z_i \le x_i^{\max} \cdot z_0, \, i = 1, 2, ..., z.$$
(16)

As it can be seen in expressions (11)–(16), the modified model is linear towards the variables z_0 , $\{z_i\}$ and therefore can be effectively implemented with the use of simplex method (that guarantees identification of optimal solution in case the corresponding feasible region exists) in the modern software tools of optimization modeling.

3 Results and discussion

At the final stage of the research created model has been implemented on the practical case – determination of the optimal values for the technical characteristics of the reach-trucks operating within the storage zone for construction materials. Preparation of the model was carried out in "Microsoft Excel" software, implementation of the model was conducted with the use of "Solver" add-in. The general view of the "Microsoft Excel" worksheet is shown in Fig. 1. The settings of "Solver" add-in are presented in Table 5.

		in Fig. 1. The settings of Solver	1 0	1 1 1		L.				0
1	A Table 1 S	B C D E F G	н	1	J	К	L	м	N	0
		Name of the source data element				e:	Mary mit	Value		
2	No.	Source data specified for technological process				Sign	Meas. unit	value		
3	1.1	Duration of the time interval of CHM continuous operation				T^{Σ}	h	8		
4 5 6 7 8 9	1.1	CHM time utilization ratio					n	0,9		
6	1.2	Safety factor of the actual used energy volume for ASB				γ _T		0,9		
7	1.3	Maximal renting cost for a CHM unit				δ_{ASB} C^{max}	ths.rub./unit	1737,6		
8	1.5	Cost constant				a ₀	ths.rub	2073,01		
9	1.6	Minimal value of average cycle time				Tmin	S	54,73		
10	1.7	Maximal value of average cycle time				T^{\max}	s	91,4		
11	2	Source data specified for technological route								
12	2.1	Fotal length of CHM straight-line movements at a stationary speed with CU L ⁺ _{mv} m				m	54,09			
13	2.2	Total length of CHM straight-line movements at a stationary speed	without CU			L try	m	59,68		
14	2.3	Total length of CHM straight-line movements at a shunting speed	with CU (with	hout CU)		$L^{+(-)}$ shn	m	2,40		
15	2.4	Turning radius calculated value				R	m	1,50		
16	2.5	Turning angle value				φ	rad	1,57		
17	2.6	Number of 90° turns with CU				n_{trn}^+	unit	5		
18	2.7	Number of 90° turns without CU					unit	3		
19	2.8	Height of CU lifting / lowering during pickup				n tm		0.12		
						Hpick	m			
20	2.9	Height of CU lifting / lowering during release				H _{rel}	m	5,10		
21	2.10	Average duration of additional operations during CU pickup				∆t pick	s	1		
22	2.11	Average duration of additional operations during CU release				Δt_{rel}	S	1		
23	3	Source data specified for construction handling machines' operation	m							
24	3.1	Mass of CU being processed				m	kg	1500		
25	3.2	Gravity acceleration				g	m/s ²	9,81		
26	3.3	Ratio of the CHM travel speed without CU to the CHM travel spee	d with CU			k uv	-	1,014		
27	3.4	Ratio of the CHM shunting speed of the CHM stationary speed				k try s	100	0,45		
28	3.5	Ratio of the lifting speed of the CHM pickup device without CU to	the similar s	peed with CU		k In	-	1,625		
29	3.6	Ratio of the CHM pickup device lowering speed to the CHM picku	p device lifti	ng speed		k lur	100	1,25		
30	3.7	Ratio of the mass of a CHM unit to its carrying capacity				k mas		2,36		
31	3.8	Ratio of the mass of a CHM unit's pickup device to CHM unit's ca	rrving canaci	ity		k PD	-	0,12		
32	3.9	Coefficient of resistance to CHM movement with stationary speed	arying cupue	,		f _{uv}		0,02		
33	3.10	Coefficient of resistance to CHM movement with stationary speed					-	0,02		
						f _{trv s}	1070			
34	3.11	Efficiency of the CHM movement mechanism providing stationar				$\eta_{\rm IN}$	-	0,83		
35	3.12	Efficiency of the CHM movement mechanism providing shunting	speed			$\eta_{\rm trv s}$		0,8		
36	3.13	Efficiency of the lifting mechanism for CHM unit's pickup device				77 1A		0,65		
37	3.14	ASB limit discharge ratio				μ_{ASB}	-	0,8		
38					-					
39	Table 2. S	ource data and unknown variables connected to CHM technica	characteris	tics						
40	Mann	Name of the characteristic	Ед. изм.	Proportion	Value of o	riginal unkno [,]	wn variable	Value of o	riginal unknov	wn variable
41	№ п.п.	Name of the characteristic	Ед. изм.	coefficient	minimal	maximal	actual	minimal	maximal	actual
42	i	-	MSU	a,	x^{\min}	x ^{max} ,	<i>x</i> ,	x_{i}^{\min} , z_0	$x \frac{\max}{1} \cdot z_0$	z,
43			-			MSU	MSU			
44	0				MSU			MSU/s	MSU/s	MSUIS
44	1 1 1 2 2 2 2	Inverse value of the average cycle time	e ⁻¹		MSU	-		MSU/s 0.01094053	MSU/s 0.0182699	MSU/s
-+0		Inverse value of the average cycle time	s ⁻¹	-	-	-	-	0,01094053	0,0182699	0,01323801
	1	Load carrying capacity value	kg	- 0,24247587 8629.93	- 1500	- 3000	- 1500	0,01094053 19,8570168	0,0182699 39,7140336	0,0132380
46	2	Load carrying capacity value Inverse value of stationary travel speed with CU	kg h/km	8629,93	- 1500 0,06752217	- 3000 0,1	- 1500 0,07583961	0,01094053 19,8570168 0,00077871	0,0182699 39,7140336 0,0013238	0,0132380 19,8570168 0,00100393
46 47	2 3	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value	kg h/km m	8629,93 0,06142835	- 1500 0,06752217 2200	- 3000 0,1 7495	- 1500 0,07583961 2200	0,01094053 19,8570168 0,00077871 29,1236246	0,0182699 39,7140336 0,0013238 99,218894	0,0132380 19,8570168 0,0010039 29,1236246
46 47 48	2 3 4	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value Inverse value of the lifting speed for pickup device with CU	kg h/km m s/m	8629,93 0,06142835 -496,54329	- 1500 0,06752217	- 3000 0,1 7495 4	- 1500 0,07583961 2200 3,65425261	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602	0,0182699 39,7140336 0,0013238 99,218894 0,05295204	0,01323801 19,8570168 0,00100397 29,1236240 0,04837504
46 47 48 49	2 3 4 5	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value Inverse value of the lifting speed for pickup device with CU Turning radius value	kg h/km m s/m mm	8629,93 0,06142835 -496,54329 -0,6632182	- 1500 0,06752217 2200 2 1440	- 3000 0,1 7495 4 1750	- 1500 0,07583961 2200 3,65425261 1750	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602 19,0627361	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196	0,0132380 19,8570168 0,00100397 29,1236246 0,04837504 23,1665196
46 47 48 49 50	2 3 4	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value Inverse value of the lifting speed for pickup device with CU	kg h/km m s/m	8629,93 0,06142835 -496,54329	- 1500 0,06752217 2200 2	- 3000 0,1 7495 4	- 1500 0,07583961 2200 3,65425261	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196	0,0132380 19,8570168 0,00100397 29,1236246 0,04837504 23,1665196
46 47 48 49 50 51	2 3 4 5 8	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB)	kg h/km m s/m mm	8629,93 0,06142835 -496,54329 -0,6632182	- 1500 0,06752217 2200 2 1440	- 3000 0,1 7495 4 1750	- 1500 0,07583961 2200 3,65425261 1750	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602 19,0627361	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196	0,01323801 19,8570168 0,00100397 29,1236246 0,04837504 23,1665196
46 47 48 49 50 51 52	2 3 4 5 8 Table 3. C	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) acutated characteristics	kg h/km m s/m mm W·h	8629,93 0,06142835 -496,54329 -0,6632182 0,0101586	- 1500 0,06752217 2200 2 1440	- 3000 0,1 7495 4 1750	- 1500 0,07583961 2200 3,65425261 1750	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602 19,0627361 538,522296	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196 667,195765	0,01323801 19,8570168 0,00100397 29,1236246 0,04837504 23,1665196 538,522296
46 47 48 49 50 51 52 53 54	2 3 4 5 8	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) alculated characteristics Name of calcula	kg h/km m s/m mm W·h	8629,93 0,06142835 -496,54329 -0,6632182 0,0101586	- 1500 0,06752217 2200 2 1440	- 3000 0,1 7495 4 1750	- 1500 0,07583961 2200 3,65425261 1750	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602 19,0627361	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196	0,01323801 19,8570168 0,00100397 29,1236240 0,0483750- 23,1665190 538,522290
46 47 48 49 50 51 52 53 54	2 3 4 5 8 Table 3. C No. 1	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) aculated characteristics Name of calcula Characteristics of the duration of the technological cycle	kg h/km m s/m mm W·h	8629,93 0,06142835 -496,54329 -0,6632182 0,0101586 istic	- 1500 0,06752217 2200 2 1440	- 3000 0,1 7495 4 1750	- 1500 0,07583961 2200 3,65425261 1750	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602 19,0627361 538,522296 Sign	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196 667,195765 Meas. unit	0,01323801 19,8570168 0,00100397 29,1236240 0,04837504 23,1665190 538,522290 Value
46 47 48 49 50 51 52 53 54 55	2 3 4 5 8 Table 3. C No. 1 1.1	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) acutated characteristics Name of calcula Characteristics of the duration of the technological cycle Specific average value of the distance of CU horizontal transportat	kg h/km m s/m mm W·h ted character	8629,93 0,06142835 -496,54329 -0,6632182 0,0101586 istic	- 1500 0,06752217 2200 2 1440	- 3000 0,1 7495 4 1750	- 1500 0,07583961 2200 3,65425261 1750	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602 19,0627361 538,522296 Sign Λ _{trv}	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196 667,195765	0,0132380 19,857016 0,0010039 29,123624 0,0483750 23,166519 538,52229 Value 112,95198
46 47 48 49 50 51 52 53 53 54 55 56	2 3 4 5 8 Table 3. C No. 1 1.1 1.2	Load carrying capacity value Inverse value of stationary travel speed with CU CU iff height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) aculated characteristics Name of calcule Characteristics of the duration of the technological cycle Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat	kg h/km m s/m mm W·h ted character	8629,93 0,06142835 -496,54329 -0,6632182 0,0101586 istic mary speed ting speed	- 1500 0,06752217 2200 2 1440 40680	- 3000 0,1 7495 4 1750 50400	- 1500 0,07583961 2200 3,65425261 1750	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602 19,0627361 538,522296 Sign <u>A_{trv}</u> A _{trv} s	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196 667,195765 Meas. unit m	0,0132380 19,857016 0,0010039 29,123624 0,0483750 23,166519 538,52229 Value 112,95198 23,518826
46 47 48 49 50 51 52 53 54 55 55 56 57	2 3 4 5 8 Table 3. C No. 1 1.1 1.2 1.3	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) acculated characteristics Name of calcule Characteristics of the duration of the technological cycle Specific average value of the distance of CU borizontal transportat Specific average value of the distance of CU borizontal transportation Specific average value of the distance of CU vertical transportation Specific average value of the distance of CU vertical transportation	kg h/km m s/m W·h ted character ion at a statio ion at a shunt provided by	8629,93 0,06142835 -496,54329 -0,6632182 0,0101586 istic mary speed ting speed a CHM unit's	- 1500 0,06752217 2200 2 1440 40680 pickup devic	- 3000 0,1 7495 4 1750 50400	- 1500 0,07583961 2200 3,65425261 1750	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602 19,0627361 538,522296 Sign Δ _{III} Δ _{III} Δ _{III} Δ _{III}	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196 667,195765 Meas. unit m m	0,0132380 19,8570163 0,0010039 29,1236244 0,0483750- 23,1665194 538,522294 Value 112,95198 23,518826 7,78061533
46 47 48 49 50 51 52 53 54 55 56 57 58	2 3 4 5 8 Table 3. C No. 1 1.1 1.2 1.3 1.4	Load carrying capacity value Inverse value of stationary travel speed with CU CU iff height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) acutated characteristics Characteristics of the duration of the technological cycle Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value	kg h/km m s/m W·h ted character ion at a statio ion at a shunt provided by epend on the	8629,93 0,06142835 -496,54329 -0,6632182 0,0101586 istic mary speed ting speed a CHM unit's	- 1500 0,06752217 2200 2 1440 40680 pickup devic	- 3000 0,1 7495 4 1750 50400	- 1500 0,07583961 2200 3,65425261 1750	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602 19,0627361 538,522296 Sign Λ _{IIV} Λ _{IIV} Λ _{IIV} Δ <i>T</i>	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196 667,195765 Meas. unit m m s	0,0132380 19,857016 0,0010039 29,123624 0,0483750 23,166519 538,52229 Value 112,95198 23,518826
46 47 48 49 50 51 52 53 53 55 55 55 56 57 58 59	2 3 4 5 8 Table 3. C No. 1 1.1 1.2 1.3 1.4 1.5	Load carrying capacity value Inverse value of stationary travel speed with CU CU iff height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) aculated characteristics Name of calcule Characteristics of the duration of the technological cycle Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal CH average value of the distance of CU horizontal CH average value of the distance of CU horizontal CH average value CH average value CH average value CH a	kg h/km m s/m W·h ted character ion at a statio ion at a shunt provided by epend on the	8629,93 0,06142835 -496,54329 -0,6632182 0,0101586 istic mary speed ting speed a CHM unit's	- 1500 0,06752217 2200 2 1440 40680 pickup devic	- 3000 0,1 7495 4 1750 50400	- 1500 0,07583961 2200 3,65425261 1750	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602 19,0627361 538,522296 Sign Δ _{1rv} Δ _{1rv} Δ _{1rv} Δ ₁ ψ _T	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196 667,195765 Meas. unit m m s s -	0,0132380 19,857016 0,0010039 29,123624 0,0483750 23,1665190 538,522290 Value 112,951988 23,518826 7,78061533 2 1
46 47 48 49 50 51 52 53 54 55 56 57 58 59 60	2 3 4 5 8 Table 3. C No. 1 1.1 1.2 1.3 1.4 1.5 1.6	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) aculated characteristics Name of calcule Characteristics of the duration of the technological cycle Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Aver, value of the duration of a part of the cycle, which does not d Ratio of the calculated value of average cycle time to the actual va	kg h/km m s/m wm W-h ted character ted character ion at a statio ion at a statio provided by epend on the ue	8629,93 0,06142835 -496,54329 -0,6632182 0,0101586 istic mary speed ting speed a CHM unit's CHM tech. ch	- 1500 0.06752217 2200 2 1440 40680 - pickup devic aracteristics	- 3000 0,1 7495 4 1750 50400	- 1500 0,07583961 2200 3,65425261 1750	0,01094053 19,8570168 0,00077871 29,1236246 0,02647602 19,0627361 538,522296 Sign Λ _{IIV} Λ _{IIV} Λ _{IIV} Δ <i>T</i>	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196 667,195765 Meas. unit m m s	0,0132380 19,857016 0,0010039 29,123624 0,0483750 23,166519 538,52229 Value 112,95198 23,51882c 7,7806153 2 1
46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61	2 3 4 5 8 Table 3. C No. 1 1.1 1.2 1.3 1.4 1.5 1.6 2	Load carrying capacity value Inverse value of stationary travel speed with CU CU iff height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) accutated characteristics Characteristics of the duration of the technological cycle Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Aver. value of the duration of a part of the cycle, which does not d Ratio of the calculated value of average cycle time to the actual va Actual value of average cycle duration	kg h/km m s/m W-h ted character ion at a statio ion at a statio provided by ppend on the ue	8629,93 0,06142835 -496,54329 -0,6632182 0,0101586 	- 1500 0,06752217 2200 2 1440 40680 - pickup devic aracteristics on of technolo	- 3000 0,1 7495 4 1750 50400 ee	- 1500 0.07583961 2200 3.65425261 1750 40680	$\begin{array}{c} 0.01094053\\ 19.8570168\\ 0.0007871\\ 99.1236246\\ 0.02647602\\ 19.0627361\\ 538.522296\\ \hline\\ Sign\\ \hline\\ \Lambda_{Irres}\\ \Lambda_{Irres}\\ \Lambda_{Irres}\\ \Lambda_{Irr}\\ \psi_{T}\\ T_{c}\\ \end{array}$	0,0182699 39,7140336 0,0013238 99,218894 0,05295204 23,1665196 667,195765 Meas. unit m m m s s - s	0,0132380 19,857016 0,0010039 29,123624 0,0483750 23,166519 538,52229 Value 112,95198 23,518826 7,7806153 2 1 7,5,540047
46 47 48 50 51 52 53 55 55 55 55 55 55 55 55 55 55 56 57 58 59 60 61 62	2 3 4 5 8 Table 3. C No. 1 1.1 1.2 1.3 1.4 1.5 1.6 2 2.1	Load carrying capacity value Inverse value of stationary travel speed with CU CU iff height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) aculated characteristics Name of calcule Characteristics of the duration of the technological cycle Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU vertical transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the extension of a part of the cycle, which does not actual value of average cycle duration Characteristics connected to the energy consumption by a CHM ur Ratio of the aver, value of the energy spent on CHM unit's moven	kg h/km m s/m mm W-h ted character ion at a statio ion at a statio ion at a shunt a provided by pepend on the ue	8629,93 0,06142835 -496,54329 -496,54329 0,0101586 istic mary speed ing speed a CHM unit's CHM tech. ch implementatis	- 1500 0.06752217 2200 2 1440 40680 pickup devid aracteristics on of technolog the load carry	- 3000 0,1 7495 4 1750 50400 re	- 1500 0.07583961 2200 3.65425261 1750 40680 value	$\begin{array}{c} 0.01094053\\ 19.8570168\\ 0.00077871\\ 29.1236244\\ 0.02647602\\ 19.0627361\\ 538.52296\\ \hline\\ \hline\\$	0.0182699 39,7140336 0,0013238 99,218894 0,05205204 23,1665190 667,195765 Meas. unit m m m m s - s	0,0132380 19,857016 0,0010039 29,123624 0,0483750 23,166519 538,52229 Value 112,95198 23,518826 7,7806153 2 1 1 7,5540047 63,472203
46 47 48 50 51 52 53 54 55 55 56 57 58 59 60 61 62 63	2 3 4 5 8 Table 3. C No. 1 1.1 1.2 1.3 1.4 1.5 1.6 2 2.1 2.2	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value Inverse value of the lifting speed for pickup device with CU Inverse value of the lifting speed for pickup device with CU Inverse value of the lifting speed for pickup device with CU Nominal energy value for accumulator storage battery (ASB) aculated characteristics Name of calcul Characteristics of the duration of the technological cycle Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Actual value of the duration of a part of the cycle, which does not d Ratio of the average cycle duration Characteristics connected to the energy sonsumption by a CHM un Ratio of the aver, value of the energy spent on CHM unit's movem	kg h/km m s/m km km km km km km km km km km km km km	8629,93 0,06142835 -496,54329 -496,54329 0,0101586 	- 1500 0.06752217 2200 2 1440 40680 pickup devia aracteristics on of technolo the load carry he load carry	- 3000 0,1 7495 4 1750 S0400 source re re re re re re	- 1500 0.07583901 2200 3.65425261 1750 40680 value value	0.01094053 19,8570168 0.00077871 29,1236246 0.02647602 19,0627361 19,0627361 19,0627361 19,0627361 19,0627361 19,0627361 19,0627361 19,0627361 20,000 19,0000 19,0000 19,000 10,000 10,0000 10,0000 10,0000 10,000 10,0000	0,0182699 39,7140336 0,0013238 99,218894 0,05205204 23,1665196 667,195765 667,195765 67,195765 87,1957655 87,1957655 87,195765555555555555555555555555555555	0,0132380 19,857016 0,0010397 29,123624 0,0483750 23,166519 23,166519 23,1655198 23,518826 7,7806153 2 1 75,5400479 63,472203 20,532189
46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64	2 3 4 5 8 Table 3. C No. 1 1.1 1.2 1.3 1.4 1.5 1.6 2 2.1 2.2 2.3	Load carrying capacity value Inverse value of stationary travel speed with CU CU iff height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) aculated characteristics Characteristics of the duration of the technological cycle Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Specific average value of the distance of CU horizontal transportat Aver. value of the duration of a part of the cycle, which does not d Ratio of the avera value of the energy spent on CHM unit's movem Ratio of the aver. value of the energy spent on a CHM unit's movem	kg h/km m s/m mm W-h ted character ted chara	8629,93 0,06142835 4496,54329 406,6632182 0,0101586 istic anary speed ing speed a CHM unit? CHM tech. ch implementationary speed to implementationary speed to owering to the	- 1500 0,06752217 2200 2 1440 40680 pickup devia aracteristics on of technold carry the load carryit load carryit	- 3000 0,1 7495 4 1750 \$0400 source re re re re re re re re re r	- 1500 0.07583901 2200 3.65425261 1750 40680 value value	$\begin{array}{c} 0.01094053\\ 19.8570168\\ 0.00077871\\ 29.1236246\\ 0.02647602\\ 19.062762\\ 538.522296\\ \hline\\ \hline\\ \hline\\ Sign\\ \hline\\ \hline\\ \Lambda_{ID}\\ \Lambda_{ID}\\ \Lambda_{ID}\\ \Lambda_{ID}\\ \hline\\ \Lambda_{ID}\\ \hline\\ \Psi_T\\ T_c\\ \hline\\ \Theta_{ID}\\ \Theta_{ID}\\ \Theta_{ID}\\ \Theta_{ID}\\ \Theta_{ID}\\ \end{array}$	0.0182699 39,7140336 0,0013238 99,218884 0,05295204 2,31665196 667,195765 Meas. unit m m m s s - s s J/kg J/kg J/kg	0,0132380 19,857016 0,001039 29,123624 0,0483750 23,166519 538,52229 538,52229 538,52229 7,7806153 2 1 175,540047 63,472203 20,532189 44,622037
46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65	2 3 4 5 8 Table 3. C No. 1 1.1 1.2 1.3 1.4 1.5 2.1 2.2 2.3 2.4	Load carrying capacity value Inverse value of stationary travel speed with CU CU lift height value Inverse value of the lifting speed for pickup device with CU Turning radius value Nominal energy value for accumulator storage battery (ASB) aculated characteristics Characteristics of the duration of the technological cycle Specific average value of the distance of CU horizontal transportation Specific average value of the distance of CU horizontal transportation Specific average value of the distance of CU horizontal transportation Aver. value of the duration of a part of the cycle, which does not divide actual value of average cycle duration Characteristics connected to the energy spent on CHM unit's movem Ratio of the aver. value of the energy spent on CHM unit's movem Ratio of the aver. value of the energy spent on CHM unit's movem Ratio of the aver. value of the energy spent on CHM unit's movem Ratio of the aver. value of the energy spent on CHM unit's movem Ratio of the aver. value of the energy spent on CHM unit's movem Ratio of the aver. value of the energy spent on CHM unit's movem Ratio of the aver. value of the energy spent on CHM unit's movem	kg h/km m s/m mm W-h ted character ted chara	8629,93 0,06142835 4496,54329 406,6632182 0,0101586 istic anary speed ing speed a CHM unit? CHM tech. ch implementationary speed to implementationary speed to owering to the	- 1500 0,06752217 2200 2 1440 40680 pickup devia aracteristics on of technold carry the load carryit load carryit	- 3000 0,1 7495 4 1750 \$0400 source re re re re re re re re re r	- 1500 0.07583901 2200 3.65425261 1750 40680 value value	$\begin{array}{c} 0.01094053\\ 19.8570168\\ 0.00077871\\ 29.1236246\\ 0.02647602\\ 19.062762\\ 538.522296\\ \hline\\ \hline\\ Sign\\ \hline\\ \Lambda_{Irrc}\\ \Lambda_{Irrc}\\ \Lambda_{Irrc}\\ \Lambda_{Irrc}\\ \Lambda_{Irrc}\\ \Lambda_{Irrc}\\ \Psi_{T}\\ T_{c}\\ \hline\\ \Theta_{Irrc}\\ \Theta_{Irrc}\\ \Theta_{Irrc}\\ \Theta_{Irrc}\\ \Theta_{Irrc}\\ \Theta_{Irrc}\\ \Lambda_{Irrc}\\ \Lambda_{I$	0.0182699 39.7140336 0.0013238 99.218894 0.05295204 23.1665196 667.195765 Meas. unit m m m m s s - - s s	0,01323801 19,8570161 0,00100397 29,1236240 0,0483750- 23,1665199 538,522290 Value 112,951988 23,518826 7,78061533 2 1 1 75,5400479 63,472203- 20,5321891 44,6220377 14,5178566
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Fig. 1. The general view of the "Microsoft Excel" worksheet.

As received results correspond to the assigned ranges of permissible values, the created model is adequate and can be used as the effective tool for solving of corresponding applied tasks. However, there are several important features that have significant influence on the practical significance of the optimization results. The mentioned-above features are the following:

- adequacy of the optimization results is directly connected to the adequacy of the analytical model describing the dependence of the rental cost for a CHM unit on its technical characteristics (see expression (1)). So, before the preparation of the optimization model, the adequacy of analytical model must be verified (for example, with the use of determination ratio R^2);
- configuration of the feasible region (and optimal solution as well) depends on the value of parameter δ_{ASB} (item 3.3 in Table 2) within the element $A_{ASB}^{condmin}$ (item 2.5 in Table 4) of the expressions (12) and (13) connected to the indirect constraints. Nevertheless, as the parameter δ_{ASB} varies from 0 to 1, it is possible to find the single value of parameter δ_{ASB} that corresponds to the most preferable variant of optimal solution of the model by sequential conduction of optimization experiments with different values of parameter δ_{ASB} .

Setting item	Value	Structural element of mathematical description
Target cell	O69	
Optimization type	maximize	Expression (11)
Variables cells	O44:O50	Table 3, items 1.1, 2.1, 2.2
	O44:O50 >= M44:M50	Left part of the expressions (15), (16)
Constraints	O44:O50 <= N44:N50	Right part of the expressions (15), (16), expression (13)
	O67 <= O66	Expression (12)
	O59 = 1	Expression (14)
Solver method	Simplex LP	-

Table 5. Settin	ngs for the "Solver"	add-in used for im	plementation of the mo	odel.
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4 Conclusion

On the basis of the conducted research, the following main conclusions have been made:

- 1. Review and analysis of the modern scientific developments in the research filed has been carried out. Corresponding results have shown the lack of the tools for determination of the construction machinery unit's characteristics that provide adequate taking into account of productivity and economic efficiency indicators.
- 2. Optimization model for determination of the construction machinery unit's technical characteristics with application of fractional linear programming has been created. On the basis of the results of the model's implementation on a practical case the conclusion has been made about the adequacy of the proposed tool.

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