

# The effects of exhaust gas recirculation on NO<sub>x</sub> storage pathway

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**Abstract.** A LNT (lean NO<sub>x</sub> trap) model coupled with EGR (exhaust gas recirculation) was developed based on the Langmuir–Hinshelwood mechanism to investigate the EGR effects on NO<sub>x</sub> adsorption pathway of LNT catalysts with temperature changed in range 150°C~550°C. Both the nitrate and nitrite adsorption paths were considered for the NO<sub>x</sub> storage process in the model as well as the spillover of stored NO<sub>x</sub> between Ba and Pt sites. The data and validation for modelling were from literatures of predecessors and our previous lean-burn gasoline engine experiment\*. The model quantified the contributions of both nitrate route and nitrite route to the NO<sub>x</sub> storage with change of EGR rate (0%~30%) under raw emission atmosphere from tested gasoline engine. The model captured key feature of different trends of nitrate route and nitrite route with increasing temperature (150°C~550°C) under EGR rate varying from 0% to 25%. The LNT model provided insight of reaction mechanism for interpreting the behaviour of NO<sub>x</sub> storage with change of GER rate and temperature, which contributed to improve the NO<sub>x</sub> storage capacity when mapping EGR rate for lean-burn engine and catalyst operation strategy optimization.

## Highlights

- Nitrate route and nitrite route had complementary correlation with each other
- There were opposite effects of EGR on two NO<sub>x</sub> storage routes in low EGR rate range
- Ratio of nitrate route to nitrite route was lowest at moderate EGR rate
- Ratio of two routes was mainly decided by nitrite route at low and high temperature
- The degree to which EGR affected the two routes varied with EGR rate and temperature

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## 1 Introduction

Lean NO<sub>x</sub> Trap also known as NSR (NO<sub>x</sub> storage and reduction) is one of effective ways to reduce NO<sub>x</sub> emission of diesel and lean-burn engines with good fuel economy[1]. The common LNT consisted of a noble metal (PGM specially Pt as catalyst sites for NO<sub>x</sub> oxidation and reduction) plus alkaline or alkaline-earth compounds (mostly Ba as NO<sub>x</sub> storage sites) deposited on alumina over a monolithic structure, usually cordierite[2]. NO<sub>x</sub> adsorption and reduction are based on cyclical engine operation alternating between lean-burn (lean fuel, high air-to-fuel ratio A/F) and rich-burn (fuel rich, A/F<13.63/1 w/w) modes[3]. NO<sub>x</sub> is adsorbed on the catalyst surface by alkali or alkaline-earth oxides under lean-burn environment, while the adsorbed NO<sub>x</sub> is reduced during rich-burn phase to regenerate catalyst[4][5].

Generally summarize literatures of LNT or NSR, there are five following steps to reveal the NO<sub>x</sub> storage and reduction mechanisms[6][7]: 1. NO Oxidation during lean conditions; 2. NO<sub>x</sub> adsorption on storage sites as nitrites and nitrates; 3. reductant agent evolution and by-products reaction; 4. stored NO<sub>x</sub> release from catalyst surface to gas flow; 5. Reduction of gaseous NO<sub>x</sub> or stored NO<sub>x</sub> to N<sub>2</sub> during the rich environment. The work about NO<sub>x</sub> adsorption process is a focus among recent LNT researches. Basically, NO<sub>x</sub> adsorption in LNT can be summarized as two parallel pathways. NO is oxidized to NO<sub>2</sub> with precious metal catalyzing firstly, and subsequently adsorbed on NO<sub>x</sub> storage sites as nitrates involving the disproportionation reaction of NO<sub>x</sub> and formation of barium peroxide and so on, which was noted as nitrate route[8]. Another path is nitrite route, i.e., NO can be stored directly in the presence of NO and oxygen as nitrite species, then further oxidized to stable nitrates by O<sub>2</sub> and NO<sub>2</sub> from both gas phase and surface sites[9].

Lots of researches were done to study the difference between two pathway and respective contribution to NO<sub>x</sub> storage performance, at same boundary conditions such as inlet gas components and temperature which have a great influence on both NO<sub>x</sub> storage pathways. Morandi S et al.[10] pointed out that the nitrites possess is significantly lower stability due to thermal stability of the nitrates is significantly higher. Nova et al.[11] and Lietti et al.[8] demonstrated that the NO<sub>x</sub> disproportionation reaction did not represent the major storage route under NO and NO/O<sub>2</sub> mixtures due to the presence of nitrites in higher amounts than nitrates during the initial NO<sub>x</sub> adsorption at low temperatures. Same conclusion can be seen in Castoldi L et al.[12] works which have confirmed participation of nitrite at 150°C, and nitrite only can be observed at the beginning of adsorption phase at 350°C. Epling W S et al.[13] revealed that the two of major components of lean-burn engine exhaust, CO<sub>2</sub> and H<sub>2</sub>O, compete for the same NO<sub>x</sub> adsorption sites, resulting in reduction of NO<sub>x</sub> storage capacity of LNT. Lindholm A et al.[14] through the study, Influence of H<sub>2</sub>O and CO<sub>2</sub> on NO<sub>x</sub> storage and reduction over Pt based catalysts with hydrogen as the reducing agent, has shown that H<sub>2</sub>O and CO<sub>2</sub> of the inlet stream lead to the formation of hydroxide and carbonate species on adsorption sites. The hydroxide and carbonate species associated with the alkaline or alkaline-earth adsorption sites reduced the trapping efficiency of NO<sub>x</sub>, because it's more difficult to store NO<sub>x</sub> on Ba(OH)<sub>2</sub> and BaCO<sub>3</sub> than on BaO. Furthermore, Epling W S et al.[13] found that hydroxide species formed by H<sub>2</sub>O with Ba sites could be displaced by carbonate species due to its higher stability. It should be aware of that oxidation of NO to NO<sub>2</sub> is a key initial step before NO<sub>x</sub> storage on alkaline or alkaline-earth component because NSR catalyst is more efficient to sorb NO<sub>2</sub> compared with NO on the NO<sub>x</sub> storage sites. Auvray X P, Olsson L et al.[15] studied the inhibition effects of H<sub>2</sub>O on NO oxidation, pointed out that Pt sites are blocked by water adsorbed on it at low temperature for oxygen adsorption on Pt surface. Whereas Ren Y, Harold M P et al.[16] demonstrated that NO<sub>x</sub> storage or global NO<sub>x</sub> convection were almost impervious to H<sub>2</sub>O effects on NO oxidation.

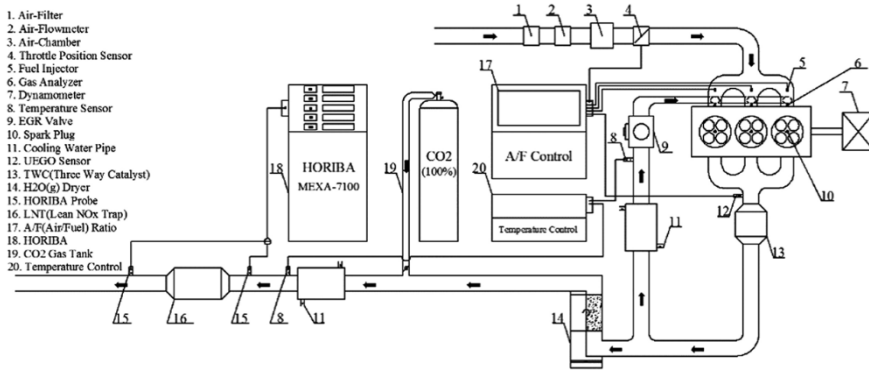
The nitrites on certain temperature range are discussed in reference [17] and [10], and CO<sub>2</sub> has inhibition effect on adsorption, H<sub>2</sub>O has little influence on both adsorption paths.

EGR is an effective way to reduce engine NO<sub>x</sub> emissions. F. Sarikoc, M. Kettner et al.[18] research studied the potential of reducing the NO<sub>x</sub> emissions in a spray guided DI gasoline engine by stratified exhaust gas recirculation (EGR). Lapuerta, M. et al.[19] research showed that low-pressure exhaust gas recirculation was more efficient than high-pressure exhaust gas recirculation to reduce NO<sub>x</sub> emissions, mainly due to the higher recirculation potential and the lower temperature of the recirculated gas. However, such a differential benefit decreased as the coolant temperature decreased, which suggests the use of high-pressure exhaust gas recirculation during the engine warm-up. It was also shown that the lean-NO<sub>x</sub> trap storage efficiency decreased more rapidly at high engine load than at medium load and that such reduction in efficiency was much faster when high-pressure exhaust gas recirculation was used than when low-pressure exhaust gas recirculation was used. Previous researches of our group were about influence of the coupling of EGR and lean-burn gasoline engine with the LNT catalyst[20]. We pointed out that the main reason of the EGR effects on LNT overall performance was the inlet components CO<sub>2</sub>/H<sub>2</sub>O concentration and ratio changed with EGR rate.

There are few researches combining CO<sub>2</sub> and H<sub>2</sub>O to the overall level of EGR to study detailed mechanism of its effects on LNT catalyst specific work stage such as NO<sub>x</sub> storage step under raw emission atmosphere from tested gasoline engine, though lots of researches done to study the effects of inlet components CO<sub>2</sub>/H<sub>2</sub>O on NO oxidation, NO<sub>x</sub> trap efficiency and NO<sub>x</sub> convection. In addition, our preliminary experimental researches focused on the discovery of the phenomenon and overall performance of synergetic system of coupling EGR with LNT, which did not conduct deep research on the influence of EGR on LNT and the underlying detailed mechanism. Hence, a detailed lean NO<sub>x</sub> trap (LNT) adsorption model coupled with EGR was developed based on the Langmuir–Hinshelwood mechanism, and both the nitrate and nitrite adsorption pathways were considered in the model as well as the NO<sub>x</sub> spillover steps between Ba/Pt sites. In additional, raw emission compositions were as boundary conditions for the LNT-EGR model.

## 2 Experiment setup

Figure 1 showed the layout of lean-burn gasoline engine test bench with EGR and LNT after-treatment system. A commercial LNT catalytic converter (Pt/Ba/Al<sub>2</sub>O<sub>3</sub>) made by Toyota with the volume of 1.9 L was chosen for simulation and experiment. The rate of exhaust flow was 950 L/min, and tested initial exhaust temperature was set as 350 °C which was favorable for high NO<sub>x</sub> conversion. The fixed inlet temperature of LNT can be controlled by the device 20 showed in Figure 1. The ratio of lean-burn time to rich-burn time was set as 56 s : 7 s in consideration of the balance the NO<sub>x</sub> storage capacity and slip of NO<sub>x</sub> during the switch of lean-rich condition, i.e., NO<sub>x</sub> storage sites were not saturated within the adsorption time 56s for the sake of reducing NO<sub>x</sub> release and maintaining overall NO<sub>x</sub> conversion efficiency. The AFR (Air/Fuel ratio) during lean-burn phase was 23, while the AFR for rich condition was 12.



**Fig. 1.** Layout of lean-burn gasoline engine test bench with EGR and LNT after-treatment system.

**Table 1.** The main characteristic parameters of LNT catalyst.

LNT Characteristic Parameters	Numerical value
Catalyst	Pt/BaO/Al <sub>2</sub> O <sub>3</sub>
Pt Loading (g/ft <sup>3</sup> )	50
Active metal surface (m <sup>2</sup> /g)	28
Pt dispersion (%)	25
Surface site density S <sub>DEN</sub> of Pt (mol/cm <sup>2</sup> )	8.095E-08
Surface site density S <sub>DEN</sub> of Ba(mol/cm <sup>2</sup> )	8.846E-07
Catalyst volume(L)	1.9
Carrier length(mm)	200
Carrier diameter(mm)	110
Catalyst length(mm)	480
Catalyst inlet diameter(mm)	50
Diffusion/shrink length(mm)	40
CPSI(Cells Per Square Inch)	400

Table 1 listed the LNT characterization parameters, and measured raw emissions of engine under different EGR rate which were used as inlet conditions for the LNT-EGR model were shown in Table 2, the more details about the bench experiment can be found in our previous paper.[20]

**Table 2.** Measured inlet gas composition and concentration of LNT with different EGR rate.

EG R	HC/ppm( ppm)	CO/ppm( ppm)	CO <sub>2</sub> /ppm( ppm)	NO/ppm( ppm)	NO <sub>2</sub> /ppm( ppm)	O <sub>2</sub> /ppm(p pm)	H <sub>2</sub> O/ppm( ppm)
0%	58.90	14.05	106000	1090	109	68400	34328
	3590	30180	110000	27.6	2.76	27400	38799
10%	63.9	15.35	119000	1000	100	64500	25320
	3610	35200	123000	24.4	2.44	23500	24663
15%	68.9	15.85	125000	882.7	88.27	60600	23344
	3670	40200	129000	22.4	2.24	19600	17505
20%	73.9	16.13	127800	414.6	41.5	56800	24853
	3720	45200	131800	20	2	15800	13458
25%	78.9	16.63	136300	391	39.9	52000	21174
	3770	50200	140600	17.8	1.78	13000	2410

30	83.9	17.13	146100	375	37.5	48000	15386
%	3820	55200	150600	17.2	1.72	11000	1000

Noting that there were two rows data of inlet gas composition and concentration corresponded to each EGR rate in the first column on left side, the data of above row referred to lean conditions of inlet gas composition, while the below row was belonging to rich condition. (The rest inlet gas is N<sub>2</sub> by default)

### 3 Modelling

#### 3.1 Reactor model

The Perfectly Stirred Reactor (PSR) model is a reaction model in the CHEMKIN software to simulate the process and mechanism of NO<sub>x</sub> storage and reduction in LNTs. It is a coupled system consisting of gas phase chemical reactions and surface chemical reactions, in which chemical kinetic processes play a leading role. There are assumptions and limitations, first the mass transport from bulk gas to surface (channel wall) was infinitely fast, and the relative importance of the reaction depends only on the specific surface area of the substance. Second, the flow through reactor is characterized by a nominal residence time, which can be deduced from the flow rate and the reactor volume. Based on the above assumptions, the equations used in the PSR reactor model are listed below.

Global mass conservation in the reactor volume

$$\frac{d}{dt}(\rho V) = \dot{m}^* - \dot{m} + \sum_{m=1}^M A_m \sum_{k=1}^K \dot{s}_{k,m} W_k \tag{1}$$

Left side of the Equation 1 is the time-rate of change of the mass in the reactor, and the right side is the difference between the mass flow in and the mass flow out, plus the net production of species on the surface material.  $\rho$  is the mass density of a gas mixture (g/cm<sup>3</sup>),  $V$  is control volume (cm<sup>3</sup>),  $\dot{m}^*$  is the inlet mass flow rate (g/sec),  $\dot{m}$  is the outlet mass flow rate (g/sec).  $A_m$  is the surface area of the material  $m$  defined within the reactor (cm<sup>2</sup>).  $\dot{s}_{k,m}$  is the molar surface production rate of the species  $k$  on the material  $m$  per unit surface area (mole/(cm<sup>2</sup>/sec)).  $W_k$  is molecular weight of the species  $k$ .  $K$  and  $M$  represent the total gas-phase species and materials, respectively.

Surface species conservation equation

$$\frac{d}{dt}(A_m c_k W_k) = A_m \dot{s}_{k,m} W_k \tag{2}$$

Here  $A_m$  is the surface area of the material  $m$  in the reactor and  $c_k$  is the molar concentration of the surface species  $k$  (mole/cm<sup>2</sup>).

The model introduced in this article is an ideal PSR reaction model. Since catalysis only reacts on the surface, there is no gas phase reaction, so the energy equation of the gas phase reaction is not discussed here.

#### 3.2 Reaction mechanism

Based on the CHEMKIN which is the standard for modeling and simulating gas-phase and surface chemistry through specific development, the gas phase, surface phase and thermodynamics files developed by data from experiments and simulations of predecessors and our previous lean-burn gasoline engine experiment were rewritten for the NO<sub>x</sub> adsorption process of the LNT-EGR model. A modification LNT model based on Chatterjee D et al.[21][22][23] research was built. The detailed reactions involved in the mechanism and the

related chemical kinetic parameters were shown in Table 3, which described NO<sub>x</sub> storage and reduction under isothermal conditions.

**Table 3.** Reaction scheme of LNT and the parameter value of Arrhenius rate expression.

reaction	A <sub>i</sub>		β <sub>i</sub>		E <sub>i</sub> (cal/mole)		
	forward reaction	reverse reaction	forward reaction	reverse reaction	forward reaction	reverse reaction	
Surface mechanism on Pt							
<b>R1</b>	NO + Pt(S) ↔ NO(S)	3.890E+13	5.818E+12	0	0	25.79	72.82
<b>R2</b>	NO <sub>2</sub> + Pt(S) ↔ NO <sub>2</sub> (S)	2.248E+10	1.961E+14	0	0	17.97	100.51
<b>R3</b>	CO + Pt(S) ↔ CO(S)	2.594E+21	1.130E+14	0	0	99.99	99.99
<b>R4</b>	H <sub>2</sub> O + Pt(S) ↔ H <sub>2</sub> O(S)	5.071E+13	2.992E+12	0	0	53.83	87.07
<b>R5</b>	NH <sub>3</sub> + Pt(S) ↔ NH <sub>3</sub> (S)	7.574E+30	1.329E+27	0	0	193.14	193.44
<b>R6</b>	O <sub>2</sub> + 2Pt(S) ↔ 2O(S)	4.776E+24	2.070E+29	0	0	58.39	182.81
<b>R7</b>	H <sub>2</sub> + 2Pt(S) ↔ 2H(S)	1.058E+23	8.436E+21	0	0	51.93	81.06
<b>R8</b>	CO(S) + O(S) ↔ CO <sub>2</sub> + 2Pt(S)	1.073E+13	4.783E+21	0	-0.4874	7.54	228.90
<b>R9</b>	2N(S) ↔ N <sub>2</sub> + 2Pt(S)	2.773E+16	3.587E+11	0	0.0482	88.13	123.47
<b>R10</b>	NO(S) + NH(S) ↔ N <sub>2</sub> O(S) + H(S)	9.373E+11	2.270E+20	0.6092	0	45.87	41.70
<b>R11</b>	2N(S) + O(S) ↔ N <sub>2</sub> O(S) + 2Pt(S)	2.102E+32	1.524E+29	0	-0.6092	164.37	56.44
<b>R12</b>	NO(S) + Pt(S) ↔ N(S) + O(S)	9.392E+18	1.383E+25	0	0	85.01	174.58
<b>R13</b>	NO(S) + O(S) ↔ NO <sub>2</sub> (S) + Pt(S)	4.862E+25	1.868E+30	0.2231	0	168.59	200.69
<b>R14</b>	H(S) + OH(S) ↔ H <sub>2</sub> O(S) + Pt(S)	1.945E+20	6.140E+25	0	0.6230	0.82	160.82
<b>R15</b>	H(S) + O(S) ↔ OH(S) + Pt(S)	2.348E+21	3.379E+11	0	0	0.00	21.03
<b>R16</b>	NH <sub>3</sub> (S) + Pt(S) ↔ NH <sub>2</sub> (S) + H(S)	6.057E+18	3.619E+28	0.8602	0	105.34	142.89
<b>R17</b>	NH(S) + H(S) ↔ NH <sub>2</sub> (S) + Pt(S)	1.179E+12	4.772E+20	0	0	19.12	87.26
<b>R18</b>	N(S) + H(S) ↔ NH(S) + Pt(S)	9.604E+22	4.234E+17	0	0	89.08	74.89
<b>R19</b>	NH <sub>3</sub> (S) + O(S) ↔ NH <sub>2</sub> (S) + OH(S)	3.367E+18	2.895E+18	0	-0.8602	33.26	91.85
<b>R20</b>	NO(S) + H(S) ↔ N(S) + OH(S)	3.563E+11	.548E+07	0	0	17.43	128.03
<b>R21</b>	N <sub>2</sub> O(S) + H(S) ↔ N <sub>2</sub> +OH(S) + Pt(S)	1.976E+28	5.073E+16	0	0.6574	105.34	269.64
<b>R22</b>	2NO(S) ↔ N <sub>2</sub> O(S) + O(S)	7.201E+20	1.132E+30	0	-0.6092	86.38	157.59
<b>R23</b>	NO <sub>2</sub> (S) + CO(S) ↔ NO(S) + CO <sub>2</sub> + Pt(S)	5.620E+20	6.518E+24	0	-0.2643	87.77	277.03
<b>R24</b>	H <sub>2</sub> O(S) + CO(S) ↔ 2H(S) + CO <sub>2</sub>	6.396E+18	6.274E+31	0	-1.1104	108.42	148.75
<b>R25</b>	N(S) + CO ↔ NCO(S)	2.879E+19	7.933E+13	0	0	106.46	118.75
<b>R26</b>	NCO(S) + H <sub>2</sub> O(S) ↔ NH <sub>2</sub> (S) + CO <sub>2</sub> + Pt(S)	7.648E+20	2.116E+35	0	-1.1104	96.32	178.31
<b>R27</b>	N <sub>2</sub> O + Pt(S) ↔ N <sub>2</sub> O(S)	1.976E+11	7.936E+11	0	0	35.90	35.90
<b>R28</b>	NO(S) + NH <sub>2</sub> (S) ↔ N <sub>2</sub> + H <sub>2</sub> O(S) + Pt(S)	1.492E+09	7.240E+02	0	0.6712	6.87	258.86

Reactions on NO <sub>x</sub> storage (BaO) sites							
BaO-CO <sub>2</sub> -NO <sub>2</sub> Surface mechanism on Pt							
<b>R29</b>	CO <sub>2</sub> + BaO ↔ BaCO <sub>3</sub>	3.589E+07	1.307E+03	0	0	20.13	37.64
<b>R30</b>	NO <sub>2</sub> + BaO ↔ BaO(NO <sub>2</sub> )	1.107E+08	1.292E+01	0	0	0.00	28.55
<b>R31</b>	BaO + NO <sub>2</sub> ↔ BaO(O) + NO	1.188E+08	8.343E+11	0	0.2231	3.93	33.14
<b>R32</b>	NO <sub>2</sub> + BaO(NO <sub>2</sub> ) ↔ NO + BaO(NO <sub>3</sub> )	2.518E+08	6.599E+11	0	0	1.15	30.71
<b>R33</b>	NO <sub>2</sub> + BaO(NO <sub>3</sub> ) ↔ Ba(NO <sub>3</sub> ) <sub>2</sub>	5.896E+07	7.727E+00	0	0	7.29	35.93
Pt-BaO Spillover reactions							
<b>R34</b>	BaO + O(S) ↔ BaO(O) + Pt(S)	3.577E+13	1.655E+17	0	0	74.88	98.88
<b>R35</b>	BaO(NO <sub>2</sub> ) + O(S) ↔ BaO(NO <sub>3</sub> ) + Pt(S)	2.402E+04	4.145E+07	0	-0.2231	0.00	24.35
<b>R36</b>	BaO(NO <sub>2</sub> ) + H(S) ↔ BaO + NO + OH(S)	4.538E+08	8.496E+05	0	0.2231	2.31	0.00
<b>R37</b>	Ba(NO <sub>3</sub> ) <sub>2</sub> + H(S) ↔ BaO(NO <sub>2</sub> ) + NO <sub>2</sub> + OH(S)	7.627E+10	4.852E+04	0	0.2231	42.01	10.05
<b>R38</b>	BaO(NO <sub>2</sub> ) + CO(S) ↔ BaO + NO + CO <sub>2</sub> + Pt(S)	8.718E+12	5.055E+28	0	-0.2643	57.36	255.38
<b>R39</b>	BaO(NO <sub>3</sub> ) + CO(S) ↔ BaO(NO <sub>2</sub> ) + CO <sub>2</sub> + Pt(S)	6.517E+06	1.683E+12	0	-0.2643	0.48	197.49
<b>R40</b>	Ba(NO <sub>3</sub> ) <sub>2</sub> + CO(S) ↔ BaO(NO <sub>2</sub> ) + NO <sub>2</sub> + CO <sub>2</sub> + Pt(S)	4.423E+07	8.714E+19	0	-0.2643	19.14	187.51
<b>R41</b>	BaO(NO <sub>2</sub> ) + N(S) ↔ BaO(O) + N <sub>2</sub> O(S)	1.498E+11	1.439E+24	0	-0.3861	55.14	82.67
<b>R42</b>	BaO(NO <sub>2</sub> ) + N(S) ↔ BaO(O) + N <sub>2</sub> + O(S)	3.535E+15	6.058E+26	0	0.2713	98.45	269.25
<b>R43</b>	BaO(NO <sub>3</sub> ) + N(S) ↔ BaO(O) + N <sub>2</sub> + O <sub>2</sub> + Pt(S)	1.216E+17	2.786E+20	0	0.4944	106.20	128.23
<b>R44</b>	Ba(NO <sub>3</sub> ) <sub>2</sub> + N(S) ↔ BaO(NO <sub>3</sub> ) + N <sub>2</sub> + O <sub>2</sub> + Pt(S)	1.396E+21	1.063E+24	0	0.2713	156.02	178.31

Noting that (s) behind a specie means that Pt sites were occupied by the specie, specially Pt = Pt(s).

The kinetics model includes two kinds of NO<sub>x</sub> adsorption routes. The global reactions of nitrate route are shown in Equations 3, which consists of two types reaction path including NO<sub>x</sub> disproportionation (Equation 3.1 & Equation 3.2) and reaction involving the formation of barium peroxide (Equation 3.3 & Equation 3.4)[24]. NO<sub>x</sub> disproportionation (Equation 3.1 & Equation 3.2) involving nitrite and nitrate intermediates Ba(NO<sub>2</sub>)(NO<sub>3</sub>) (refer to as BaO(NO<sub>2</sub>) & BaO(NO<sub>3</sub>) of Table 3) in reaction R30, R32 and R33) are obtained by combining R30, R32 and R33. Then, nitrites are oxidized by NO<sub>2</sub> in a reaction where nitrates are formed, and NO is desorbed into the gas phase[24]. As we can see from the disproportionation reaction, consumption of every three molecules of NO<sub>2</sub> released one molecule of NO. As for Equations 3.3 & 3.4 involving the formation of barium peroxide and NO are the global reactions of reactions R31, R6, R9, R12, R13, R43 and R44. Barium surface can be oxidized by NO<sub>2</sub> involving the formation of barium peroxide and NO which

is released in the gas phase[24]. Then BaO(O) is involved in the NO<sub>2</sub> adsorption for the formation of nitrates.

**Nitrate route:**



NO<sub>x</sub> disproportionation

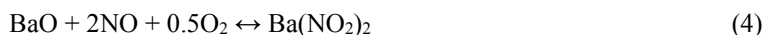


reaction involving the formation of barium peroxide



While the global reactions of nitrite route[25] which is in parallel to nitrate route are presented in Equations 4 and 5[9]. NO can be directly adsorbed as nitrite on Ba sites with help of Pt showed in Equation 4, then Ba(NO<sub>2</sub>)<sub>2</sub> are further oxidized to stable nitrates by the spilled over oxygen from Pt sites showed in Equation 5. The global reaction 4 and 5 can be derived by elementary reaction R11, R12, R13, R33, R34, R35 and the reverse reaction of R41. In this study, Ba(NO<sub>3</sub>)<sub>2</sub> site fraction and BaO-NO<sub>2</sub> site fraction are employed to characterize two kinds of NO<sub>x</sub> adsorption pathways. It is noting that Ba(NO<sub>3</sub>)<sub>2</sub> can be obtained from both nitrate route as indicated in Equation 3.1~3.4 and intermediate production conversion (nitrite route) showed in Equations 4~5. Therefore nitrate route can be indicated as difference between total Ba(NO<sub>3</sub>)<sub>2</sub> site fraction and the part of Ba(NO<sub>3</sub>)<sub>2</sub> produced by nitrite route, i.e., the BaO-NO<sub>2</sub> site fraction in consideration of relationship of stoichiometric number showed in Equation 5.

**Nitrite route:**



The Figure 2 illustrates the overall perspective of reaction path related to NO<sub>x</sub> storage to get more intuitive understanding. There were not arrows in connecting lines between species because the reactions between these species are reversible as shown in Table 3. Table 3 also gives the forward and reverse kinetic parameters for each reaction, i.e., the values of  $A_i$ ,  $\beta_i$ , and  $E_i$  in the generalized Arrhenius expression

$$k_i = A_i T^{\beta_i} e^{\frac{-E_i}{RT}} \quad (6)$$

where  $A_i$  is the pre-exponential factor,  $\beta_i$  is the temperature exponent, and the activation energy is  $E_i$ .



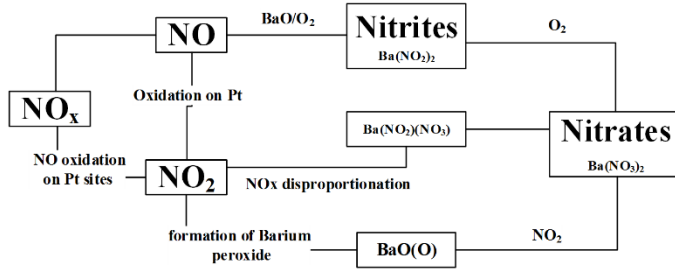


Fig. 2. Diagrammatic NO<sub>x</sub> storage routes.

### 3.3 Modelling Validation

There are 44 reactions in total involved in LNT-EGR kinetics model, which is comprised of several sub-model mentioned in section 3.2 including NO oxidation, oxidation of reductants CO, NH<sub>3</sub> and H<sub>2</sub>, NO<sub>x</sub> storage including both nitrate and nitrite routes, water–gas shift reaction, water decomposition reaction, formation of NH<sub>3</sub> and N<sub>2</sub>O, intermediate products surface isocyanate reaction, spillover process of NO<sub>2</sub> and reduction reaction of stored NO<sub>x</sub>. These sub-models which are from different research groups’ work as mentioned above were picked up here to combine final LNT-EGR model. Parameter values (pre-exponential factor, temperature exponent and the activation energy) of NO oxidation rate expressed by R1, R2, R6 and R13 are from the NO<sub>x</sub> adsorption experiments lasting long enough to show almost full NO<sub>x</sub> breakthrough conducted by Kočí P, Marek M et al.[26] Parameter values of oxidation of reductants CO, H<sub>2</sub> and NH<sub>3</sub> expressed by R8, R15, R19 were from the CO, H<sub>2</sub> and HC oxidation light-off experiments based on slow temperature ramps under both lean and rich conditions at different concentration levels conducted by Kočí P, Schejbal M et al.[27] These literature parameters values of these sub-models were used as the initial guess and followed by tuning to get a reasonable fitting for each sub-model. The Figure 3 illustrates the overall perspective of reaction path related to sub-models to get more intuitive understanding.

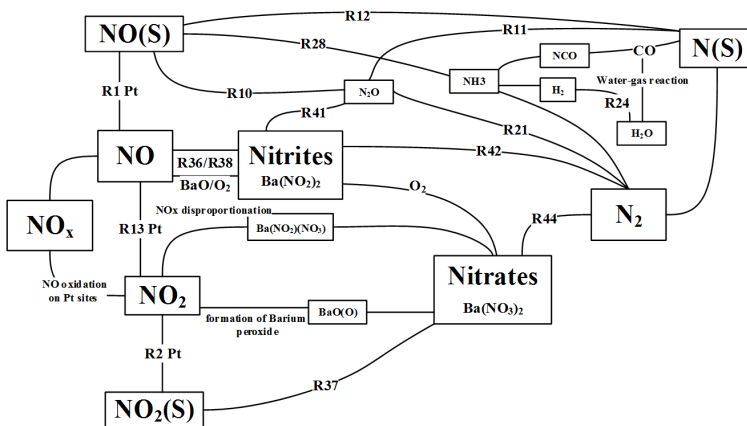


Fig. 3. Diagrammatic NO<sub>x</sub> storage and reduction reaction path.

After the preliminary determination of sub-model, the whole performance of LNT under different EGR rate was validated by the lean-burn gasoline engine test bench as we mention

above. Considering the simulation accuracy and calculation cost, the step size for setting the simulation calculation is 0.1 s. In order to verify the accuracy of the model, the exhaust conditions of the catalyst under the different EGR rates measured in the previous experiment are used as the simulated boundary conditions of the catalyst. According to the engine exhaust components and concentrations measured by the experiment, the catalyst inlet gas concentration and other boundary conditions were obtained. For the comparative study, the EGR rates are set as 0%, 10%, 15%, 20%, 25%, 30%, respectively. Corresponding gas compositions and concentrations are shown in Table 2 as mentioned in Experiment setup. The comparison of outlet NO<sub>x</sub> slip between simulation and experiment is shown in Figure 4. It can be found that NO<sub>x</sub> slip of LNT from chemical reaction kinetics simulation has the similar trend with the experimental results. Simulation values basically can represent outlet NO<sub>x</sub> slip because of catalyst desorption, adsorption saturation and storage site limitation. As shown in Figure 4, the error between simulation and experiment is about 50ppm when the EGR is below 10%, when EGR increases up to 15% the error decreases below 30ppm, which indicated that maximum relative error between simulation and experiment is 4.5%, which is lower than 5%. The error may come from the distance between measurement point of LNT outlet and HORIBA gaseous element analyzer, LNT still has adsorption ability as engine switches into rich-burn phase, and abundant desorption has delay. Meanwhile, experimental catalyst cannot switch from lean-mode to rich-mode instantaneously, but simulation can switch immediately, so the simulation has more NO<sub>x</sub> slip because of desorption. All in all, these verify the validity of the mechanism so the LNT-EGR model can be used for further investigate.

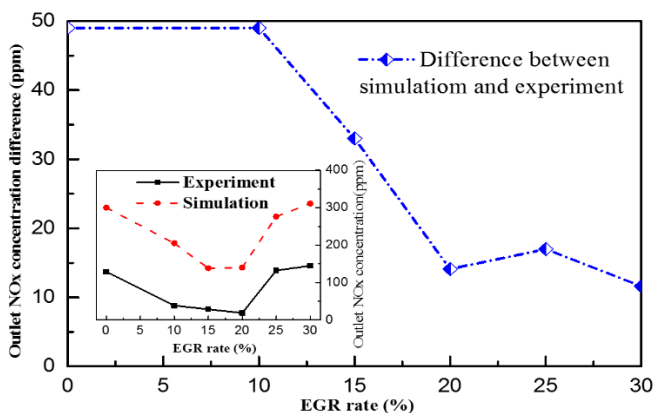


Fig. 4. Comparison of simulation and experiment of LNT.

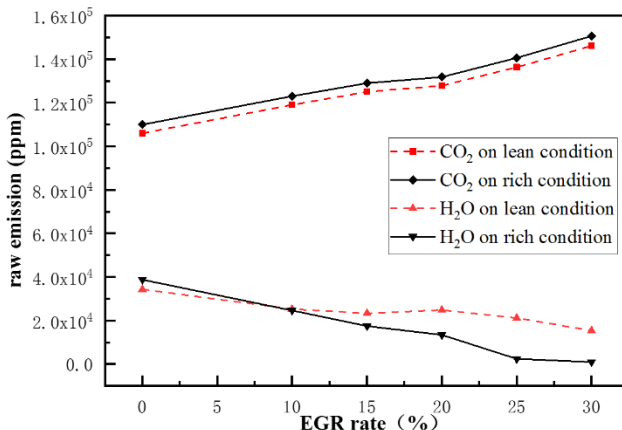
## 4 Results and discussion

### 4.1 Effects of EGR rate on NO<sub>x</sub> storage at fixed temperature

Effects of EGR rate on NO<sub>x</sub> storage process were studied by the contributions and variation tendencies of the two different NO<sub>x</sub> adsorption pathways, i.e., nitrate route and nitrite route. The nitrate route and nitrite route are characterized by Ba(NO<sub>3</sub>)<sub>2</sub> and BaO-NO<sub>2</sub> site fractions, respectively. As previously mentioned, noting that nitrates are accumulated by both nitrate route as indicated in Equation 3.1~3.4 and intermediate production conversion (nitrite route) showed in Equations 4~5. The temperature was set as 350°C.

The main reason of the EGR effects on LNT overall performance is the change of concentration and ratio of inlet components CO<sub>2</sub>\H<sub>2</sub>O as mentioned in Introduction. Before the discussion of EGR effects on NO<sub>x</sub> storage pathway, it should be aware of that the

combined influences of both CO<sub>2</sub> and H<sub>2</sub>O on NO<sub>x</sub> storage and reduction are not equivalent to the individual effects of CO<sub>2</sub> or H<sub>2</sub>O. In this paper, combined influences of both CO<sub>2</sub> and H<sub>2</sub>O on NO<sub>x</sub> storage are discussed in the level of EGR, as a matter of convenience for analysis, the trend of CO<sub>2</sub> and H<sub>2</sub>O concentration from raw emission under different EGR rate at 350 °C was showed in Figure 5.

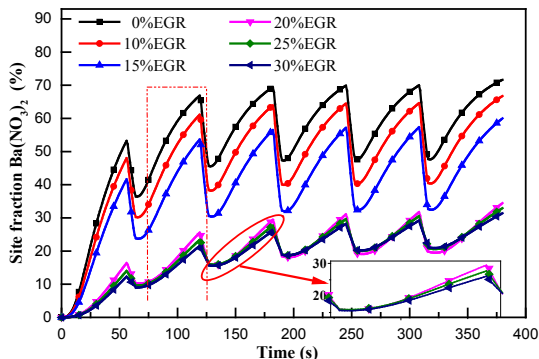


**Fig. 5.** Trend of CO<sub>2</sub> and H<sub>2</sub>O concentration from raw emission under the different EGR rate at 350 °C.

Figure 6 shows time-varying Ba(NO<sub>3</sub>)<sub>2</sub> site fraction under different EGR rates at 350 °C. EGR rates are divided into two intervals of 0%~15% and 20%~30% due to the different variation tendency of Ba(NO<sub>3</sub>)<sub>2</sub> site fraction. When the EGR rate increases from 0% to 15%, Ba(NO<sub>3</sub>)<sub>2</sub> site fraction decreased gradually, which indicates that increase of EGR rate shows inhibition effects on the NO<sub>x</sub> storage as Ba(NO<sub>3</sub>)<sub>2</sub>. Taking the 350 s of the adsorption stage as an example, when the EGR rate increases from 0% to 10%, Ba(NO<sub>3</sub>)<sub>2</sub> site fraction is reduced by 6.78%, while EGR rate increased from 10% to 15%, Ba(NO<sub>3</sub>)<sub>2</sub> site fraction is reduced by 8.58%. Therefore, inhibition of EGR on stored Ba(NO<sub>3</sub>)<sub>2</sub> slightly aggravates with the EGR rate increase. This is because CO<sub>2</sub> concentration of inlet increased with EGR rate as showed in Figure 5, resulting in production of BaCO<sub>3</sub> from the reaction R29 (CO<sub>2</sub> + BaO ↔ BaCO<sub>3</sub>) which indicated CO<sub>2</sub> was chemisorbed on the BaO sites led to reduction of entire NO<sub>x</sub> storage sites. The result was in line with Epling W S et al.[13] study mentioned before. In addition, it's more difficult for NO<sub>x</sub> absorbed on BaCO<sub>3</sub> than BaO[14] due to high thermal stability of BaCO<sub>3</sub>, which leads to reduction of Ba(NO<sub>3</sub>)<sub>2</sub> production as well. The effects of H<sub>2</sub>O on NO<sub>x</sub> storage process is neglected not only because its concentration of inlet decreases with EGR rate, but also H<sub>2</sub>O plays a much weaker role in NO<sub>x</sub> adsorption, which is widely reported in literatures such as reference[13]. The role of H<sub>2</sub>O is practiced not so much in NO<sub>x</sub> adsorption as in formation of NH<sub>3</sub> and N<sub>2</sub>O through water-gas shift reaction and subsidiarity of reactions involving intermediate products such as -NCO, -H and -OH, which would be discussed later.

When the EGR rate increases within interval of 20%~30%, Ba(NO<sub>3</sub>)<sub>2</sub> site fraction continues decreasing, maintaining range of 15%~25%, and the change amplitude significantly reduced. At moment of 150 s, when the EGR rate increased from 20% to 25% and from 25% to 30%, Ba(NO<sub>3</sub>)<sub>2</sub> site fraction reductions are 0.18% and 0.34%, respectively. EGR still shows inhibition effect but the degree weakens. The distinctly different Ba(NO<sub>3</sub>)<sub>2</sub> site fraction trends of the two EGR intervals of 0%~15% and 20%~30% are on account of the equilibrium limitations of reaction R29, which reveals competing adsorption mechanism of CO<sub>2</sub>, i.e., the same NO<sub>x</sub> storage sites (Ba sites) are occupied by CO<sub>2</sub>. Therefore, reduction

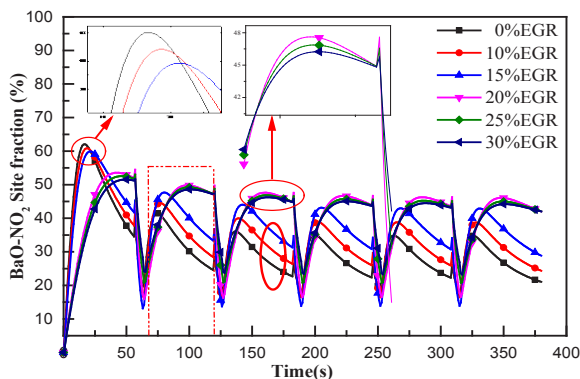
of  $\text{Ba}(\text{NO}_3)_2$  site fraction with increased EGR rate of intervals 20%~30% became less pronounced, through concentration of  $\text{CO}_2$  continuously increased with EGR rate.



**Fig. 6.** Time-varying  $\text{Ba}(\text{NO}_3)_2$  site fraction under different EGR rates at  $350^\circ\text{C}$ .

Figure 7 shows the time-varying trend of  $\text{BaO}-\text{NO}_2$  site fraction which is different from the  $\text{Ba}(\text{NO}_3)_2$  site fraction under varying EGR rate within range of 0%~30% with 5% increment. Noting the line groups inside the red dashed boxes of the figure 7 and figure 6, time interval 64s~119s is selected for comparison.  $\text{Ba}(\text{NO}_3)_2$  site fraction shows a tendency of rise while the  $\text{BaO}-\text{NO}_2$  site fraction trend is drop in the same time interval. Contacting the figure 6, the time-varying trends of site fraction for both nitrates and nitrites are complementary because of the fixed  $\text{NO}_x$  storage sites due to the limitation of commercial LNT catalytic converter.

When the EGR rate increases from 0% to 15%, the nitrite site fraction is reduced first and increases later in the  $\text{NO}_x$  storage stage such as time interval 0s~56s, however the later increase of  $\text{BaO}-\text{NO}_2$  site fraction became more evident and stable in subsequent cycles while the first reduction of  $\text{BaO}-\text{NO}_2$  site fraction with EGR rate increasing was negligible. Hence EGR shows early slightly inhibition and later promotion on the nitrite path in the EGR interval of 0%~15%. At the 350s of the adsorption stage, the  $\text{BaO}-\text{NO}_2$  site fraction respectively increases by 4.56% and 5.6% as the EGR rate increased between the two EGR rate intervals 0%~10% and 10%~15%, which shows positive effects of EGR on the nitrite path slightly aggravating with the increase of the EGR rate as the cycle was stabilized. There is different situation as EGR rate varies in the interval 20%~30%, the  $\text{BaO}-\text{NO}_2$  fraction marginally decreases with the increasing EGR rate in the  $\text{NO}_x$  storage stage, and increases in flowing  $\text{NO}_x$  reduction stage. The  $\text{BaO}-\text{NO}_2$  site fraction is reduced only by 1.08% and 0.81%, respectively for two EGR rate intervals 20%~25% and 25%~30%, which shows the weak correlation between the  $\text{BaO}-\text{NO}_2$  site fraction and EGR rate interval 20%~30%. The high overlap of the lines group of EGR rate interval 20%~30% in Figure 7 also underlines this point. The main reason of the difference between two EGR rate intervals (0%~15% and 20%~30%) above is that the reduction of Ba sites occupied by  $\text{CO}_2$  was stabilized due to equilibrium limitations of reaction R29.



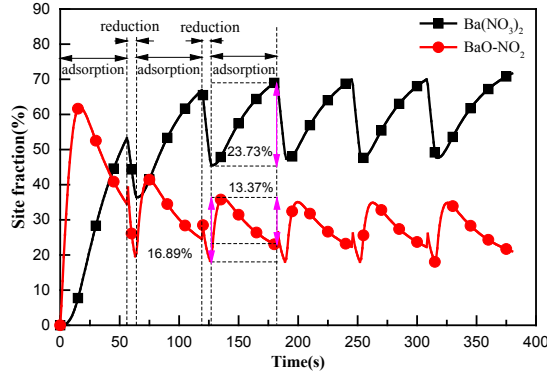
**Fig. 7.** BaO-NO<sub>2</sub> site fraction under different EGR rates at 350°C.

In addition, it can be clearly seen that two trends of Ba(NO<sub>3</sub>)<sub>2</sub> and BaO-NO<sub>2</sub> site fraction are less stable in the first cycle of the simulation from Figure 6 and 7. Furthermore, both Ba(NO<sub>3</sub>)<sub>2</sub> and BaO-NO<sub>2</sub> site fraction of first cycle are different from the corresponding flowing cycle, Ba(NO<sub>3</sub>)<sub>2</sub> site fraction is lower while BaO-NO<sub>2</sub> site fraction is higher. This phenomenon indicates that nitrite route represents the major storage during the initial NO<sub>x</sub> storage in the presence of NO<sub>x</sub> and O<sub>2</sub> mixtures under lean condition.

As for variation of Ba(NO<sub>3</sub>)<sub>2</sub> site fraction, nitrates are the final products of stable storage of NO<sub>x</sub> as showed in the Figure 2 (diagrammatic NO<sub>x</sub> storage routes) at 350 °C. Ba(NO<sub>3</sub>)<sub>2</sub> site fraction of each adsorption cycle consists of residual part from last cycle and production part of current ongoing cycle except for the first cycle which has the largest quantity of fresh NO<sub>x</sub> adsorption sites. Nitrite route and nitrate route concurrently accomplish the NO<sub>x</sub> storage, but BaO-NO<sub>2</sub> is intermediate product of the unstable nitrite route, which is in the process of continuous production and transformation. It takes long storage times to oxidize nitrites to nitrates with help of oxygen and Pt sites. Therefore, in the first adsorption cycle there is lower Ba(NO<sub>3</sub>)<sub>2</sub> site fraction than following cycles because of the absence of residual nitrates from last cycle and less production of nitrates came from oxidized nitrites for being pressed for time. Initial instability of site fraction is attributed to the largest quantity of fresh NO<sub>x</sub> adsorption sites of first cycle mentioned above. As for the situation of BaO-NO<sub>2</sub> site fraction can be explained by the complementary correlation between nitrate route and nitrite route mentioned before.

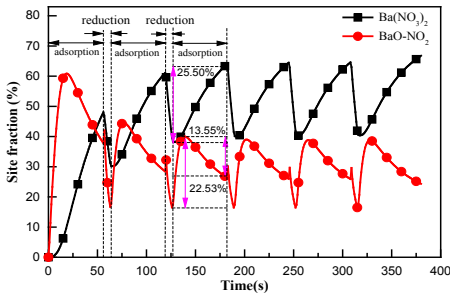
Figure 8 shows the trend of Ba(NO<sub>3</sub>)<sub>2</sub> and BaO-NO<sub>2</sub> site fraction at 0% EGR rate. During the adsorption phase of each cycle, the Ba(NO<sub>3</sub>)<sub>2</sub> site fraction shows a continuous increasing trend, i.e., NO<sub>x</sub> is continuously stored as stable nitrates through several different reaction pathways including NO<sub>x</sub> disproportionation, reaction involving the formation of barium peroxide and nitrite route expressed by Equation 4~5. It's worth noting that BaO-NO<sub>2</sub> site fraction only increases at the beginning of each NO<sub>x</sub> adsorption phase, and the increase rate is significantly higher than the Ba(NO<sub>3</sub>)<sub>2</sub> site fraction. During the late phase of adsorption, BaO-NO<sub>2</sub> fraction decreases over adsorption time until the adsorption phase completed, which has confirmed the conversion process of nitrite route due to BaO-NO<sub>2</sub> further oxidized to nitrates leading to corresponding increase of Ba(NO<sub>3</sub>)<sub>2</sub> site fraction. Therefore, the time-varying NO<sub>x</sub> storage process under lean condition at fixed temperature (350 °C) can be concluded as follows, both nitrate and nitrite storage routes proceed simultaneously and parallelly, more Ba sites are occupied though nitrite process (Equation 4 and Equation 5) at the initial NO<sub>x</sub> uptake. As time marching on, stored BaO-NO<sub>2</sub> is oxidized to Ba(NO<sub>3</sub>)<sub>2</sub> in the lean atmosphere of storage stage. Combining NO<sub>x</sub> disproportionation (Equation 3.1 & Equation 3.2) reaction involving the formation of barium peroxide (Equation 3.3 & Equation 3.4), Ba(NO<sub>3</sub>)<sub>2</sub> site fraction rises rapidly while BaO-NO<sub>2</sub> site fraction drops accordingly due

to the conserved Ba sites. Taking the adsorption phase of the third stable cycle as an example, the  $Ba(NO_3)_2$  site fraction increases by about 23.73%, of which about 13.37% is derived from the nitrite route. Hence the occupancy ratio of  $NO_x$  storage sites through the nitrate path and the nitrite path acquired by calculation is about 1:1.63, which indicated the corresponding contribution of nitrate route and the nitrite route to  $NO_x$  storage at 0% EGR rate.

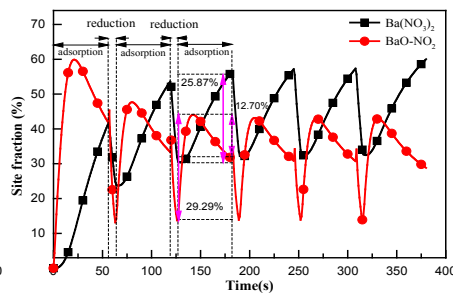


**Fig. 8.**  $Ba(NO_3)_2$  site fraction and  $BaO-NO_2$  site fraction under 0% EGR rate at 350°C.

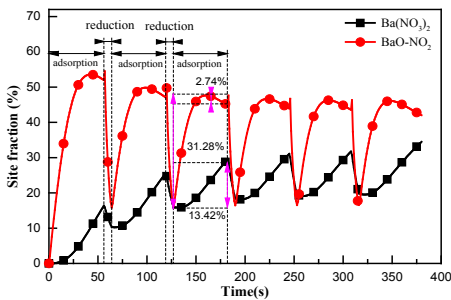
The similar  $NO_x$  storage processes under other EGR rates would not be repeated here for saving space. However, the difference of  $NO_x$  storage performance with EGR changing and the contributions to  $NO_x$  storage of both nitrate and nitrite route, which are expressed as ratio of  $NO_x$  storage sites occupied through the two different adsorption routes, were discussed below.



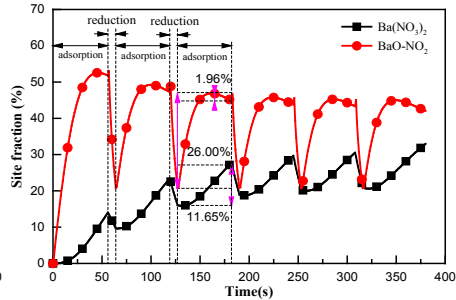
**Fig. 9.**  $Ba(NO_3)_2$  site fraction and  $BaO-NO_2$  site fraction under 10% EGR rate at 350°C.



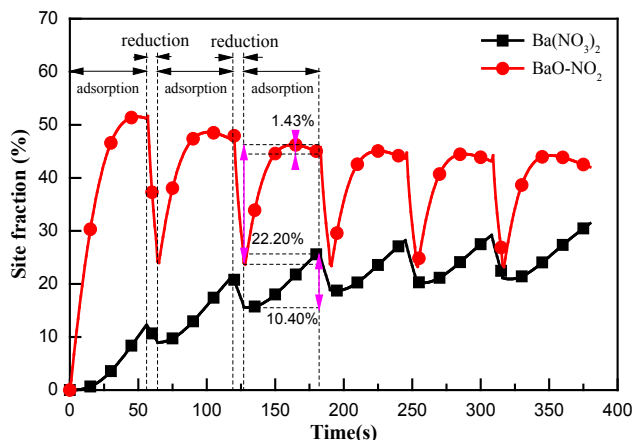
**Fig.10.**  $Ba(NO_3)_2$  site fraction and  $BaO-NO_2$  site fraction under 15% EGR rate at 350°C.



**Fig. 11.**  $Ba(NO_3)_2$  site fraction and  $BaO-NO_2$  site fraction under 20% EGR rate at 350°C.



**Fig. 12.**  $Ba(NO_3)_2$  site fraction and  $BaO-NO_2$  site fraction under 25% EGR rate at 350°C.



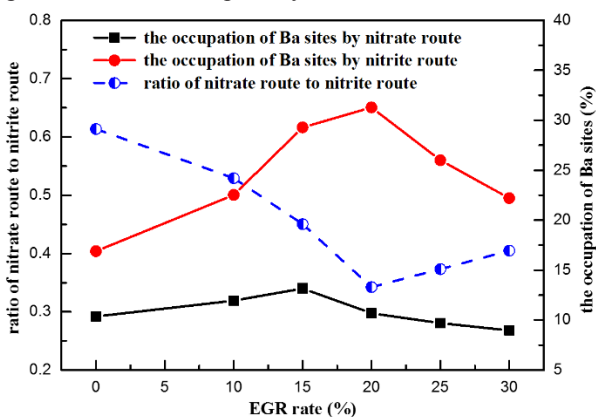
**Fig. 13.** Ba(NO<sub>3</sub>)<sub>2</sub> site fraction and BaO-NO<sub>2</sub> site fraction under 30% EGR rate at 350 °C.

For analysis of other EGR rates set, the third lean-burn cycle is selected for the rest EGR rate as 0% EGR rate did in consideration of controlling variable to minimize errors as much as possible. Figure 9 shows the time variable Ba(NO<sub>3</sub>)<sub>2</sub> site fraction and BaO-NO<sub>2</sub> site fraction of 10% EGR rate, the Ba(NO<sub>3</sub>)<sub>2</sub> increases by 25.50% and the corresponding BaO-NO<sub>2</sub> reduction was 13.55% during the third cycle. Therefore, the percentage of NO<sub>x</sub> storage sites occupied through nitrate route and the nitrite route accounts for 11.95% and 22.53%, respectively, with a view to the Ba sites consumed by CO<sub>2</sub> (R29) and the Ba sites at inactivated state. Hence the ratio of nitrate route to the nitrite route is about 1:1.89. In the third lean-burn cycle corresponding to 15% EGR showed in Figure 10, the Ba(NO<sub>3</sub>)<sub>2</sub> site fraction increase is 25.87%, and the corresponding BaO-NO<sub>2</sub> fractional decrease is 12.70%. Nitrate path and nitrite path accounted for 13.17% and 29.29%, respectively. The ratio of the two routes is about 1:2.22. Similarly, the percentage of NO<sub>x</sub> storage sites occupied through nitrate route and the nitrite route under EGR rate of 20%, 25% and 30% could be calculated by the data showed in Figure 11, 12 and 13, respectively. Therefore, the respective ratios of nitrate route to the nitrite route of each EGR rate above are 1:2.92, 1:2.68 and 1:2.47.

The ratio of nitrate route to nitrite route and Ba sites occupation of two NO<sub>x</sub> storage pathways with EGR rate changing are showed in Figure 14. It's worth noting that the connection and difference between the site fraction of Ba(NO<sub>3</sub>)<sub>2</sub> and the nitrate route. For a better understanding of the leading role of both NO<sub>x</sub> adsorption routes with EGR changing, nitrate route is separated by subtracting the Ba(NO<sub>3</sub>)<sub>2</sub> produced by nitrite route, which is equivalent to the amount of BaO-NO<sub>2</sub> involved in the nitrite oxidation reaction in consideration of relationship of stoichiometric number showed in Equation 5, from total Ba(NO<sub>3</sub>)<sub>2</sub> production.

In the range of 0% ~ 20% EGR rate, the ratio of nitrate route to nitrite route drops while raises in the 20% ~ 30% EGR rate. With EGR rate changing from 0%~30%, there is slight variation of occupation of Ba sites by nitrate route whereas Ba sites occupation by nitrite route isn't at the operating temperature (350 °C). Furthermore, similar trend of Ba sites occupation of both two NO<sub>x</sub> storage pathways is showed in Figure 14, which raises first and drops later. The change of ratio of nitrate route to nitrite route is decided by nitrite route to a great extent due to slight variation of occupation of Ba sites by nitrate route as showed above. Only when CO<sub>2</sub> concentration reaches to a certa in quantity such as the amount contented in high EGR rate over 15%, its inhibition on NO<sub>x</sub> storage process begins to emerge, though the reaction R29(CO<sub>2</sub> + BaO ↔ BaCO<sub>3</sub>) of CO<sub>2</sub> competitive adsorption on the Ba sites and NO<sub>x</sub> storage reaction coexisted. Both nitrate and nitrite routes are unaffected by increased CO<sub>2</sub>

quantity within the range of low EGR rate due to abundant Ba sites for both  $\text{NO}_x$  and  $\text{CO}_2$  adsorption. In the meantime, the amount of CO from engine exhaust raised modestly with EGR rate increase, which facilitates chemical equilibrium of reversible reaction R40 ( $\text{Ba}(\text{NO}_3)_2 + \text{CO}(\text{S}) \leftrightarrow \text{BaO}(\text{NO}_2) + \text{NO}_2 + \text{CO}_2 + \text{Pt}(\text{S})$ ) shifting to the right leading to more  $\text{BaO}-\text{NO}_2$  production. Meanwhile, the reduction of water steam with EGR rate increase shifts the chemical equilibrium of reversible reaction R36 ( $\text{BaO}(\text{NO}_2) + \text{H}(\text{S}) \leftrightarrow \text{BaO} + \text{NO} + \text{OH}(\text{S})$ ) to left resulting more  $\text{BaO}-\text{NO}_2$  formation. Water steam reduction is not conducive to chemical equilibrium of reversible reaction R37 ( $\text{Ba}(\text{NO}_3)_2 + \text{H}(\text{S}) \leftrightarrow \text{BaO}(\text{NO}_2) + \text{NO}_2 + \text{OH}(\text{S})$ ) due to both  $\text{H}(\text{S})$  and  $\text{OH}(\text{S})$  came from hydrolysis reaction which is reverse reaction of R14 ( $\text{H}(\text{S}) + \text{OH}(\text{S}) \leftrightarrow \text{H}_2\text{O}(\text{S}) + \text{Pt}(\text{S})$ ) with presence of catalyst Pt sites. Therefore, Ba sites occupation by nitrite route raises in range of 0%~20% EGR rate as well as nitrate route because of more  $\text{NO}_2$  formation through reaction R23 ( $\text{NO}_2(\text{S}) + \text{CO}(\text{S}) \leftrightarrow \text{NO}(\text{S}) + \text{CO}_2 + \text{Pt}(\text{S})$ ) with the help of increased  $\text{CO}_2$  quantity with EGR rate increased.



**Fig. 14.** ratio of nitrate route to nitrite route and Ba sites occupied by the two  $\text{NO}_x$  storage pathways under different EGR rate at  $350^\circ\text{C}$ .

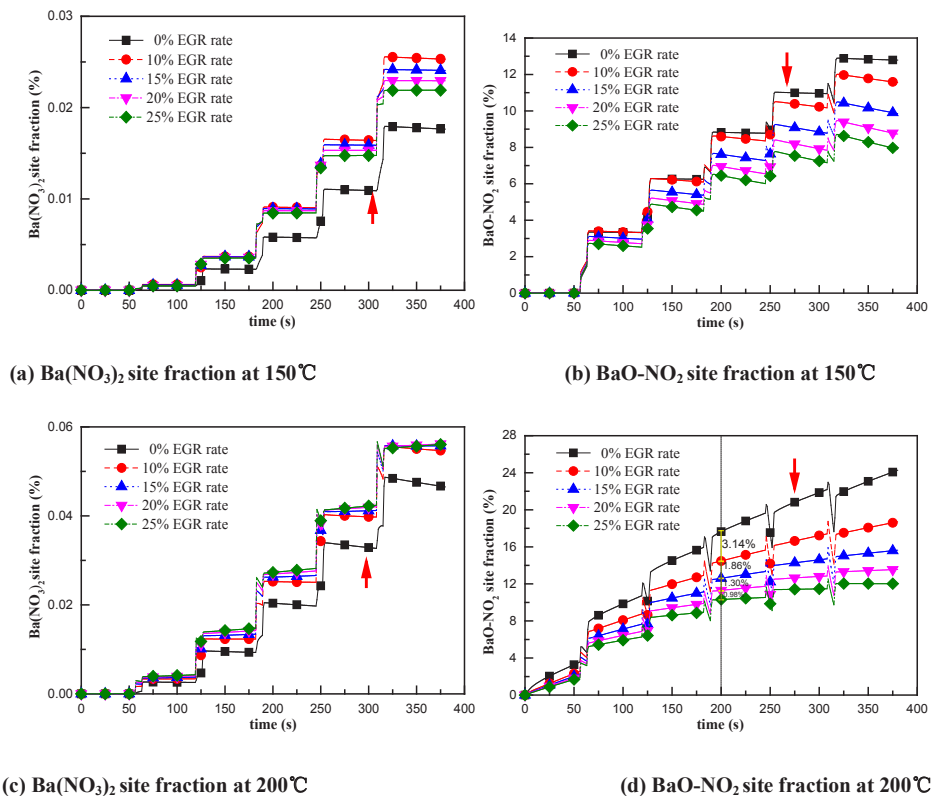
## 4.2 Effects of EGR rate under different temperature zone

Temperature is vital for chemical reaction as is well-known. The case of variation for nitrate route and nitrite routes under different EGR rate is discussed at a fixed typical LNT operating temperature  $350^\circ\text{C}$  above. Performance of EGR (0%,10%,15%,20%,25%) effects on  $\text{NO}_x$  storage course at varying temperatures would be talked about below. According to actual engine operation conditions with different EGR rates, the simulations were carried out at different inlet temperatures from  $150^\circ\text{C}$  to  $550^\circ\text{C}$ . For the sake of clearer interpretations, the numerical results were divided into three temperature zones: low temperature zone, i.e.,  $150^\circ\text{C}$  ~  $200^\circ\text{C}$ , moderate temperature zone, i.e.  $250^\circ\text{C}$ ~ $400^\circ\text{C}$ , and high temperature zone, i.e.  $450^\circ\text{C}$  ~  $550^\circ\text{C}$ .

### 4.2.1 In low temperature zone

The time-varying variation trend of  $\text{Ba}(\text{NO}_3)_2$  and  $\text{BaO}-\text{NO}_2$  site fraction under different EGR rate at low temperature zone ( $150^\circ\text{C}$ ~ $200^\circ\text{C}$ ) is showed in Figure 15.





**Fig. 15.**  $Ba(NO_3)_2$  and  $BaO-NO_2$  site fraction under different EGR rate at Low temperature.

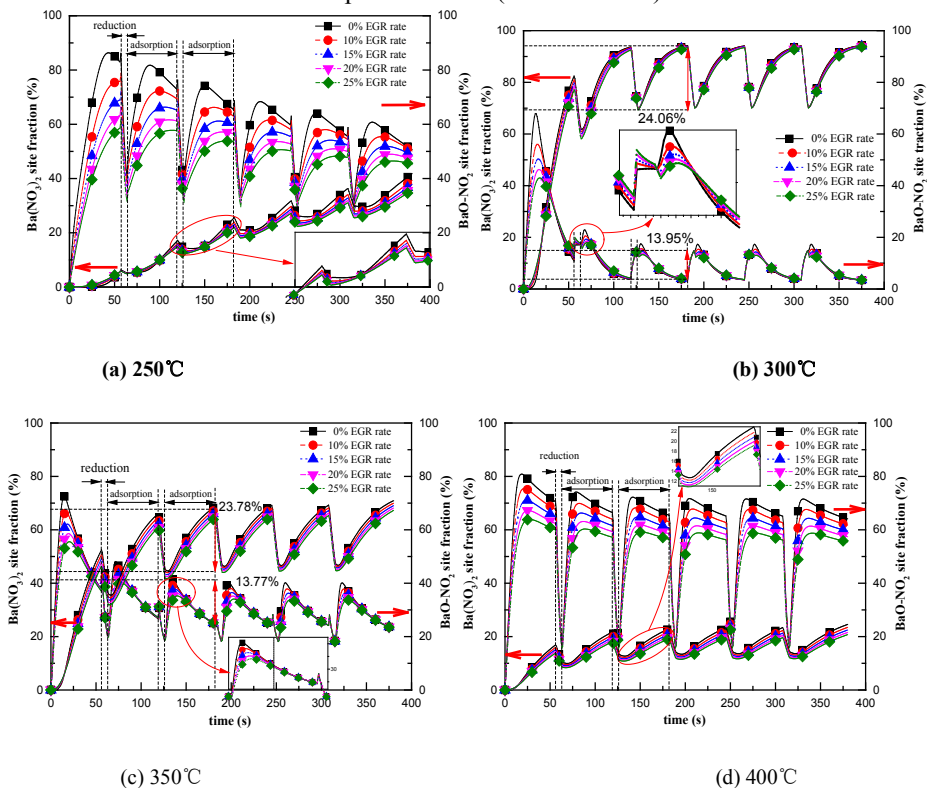
As showed in Figure 15, the  $Ba(NO_3)_2$  site fraction is no more than 0.06% in terms of simulation results while the maximum  $BaO-NO_2$  site fraction is about 25% over the whole low temperature range, which indicates that  $Ba(NO_3)_2$  site fraction is far less than  $BaO-NO_2$  site fraction. Therefore, the nitrite route dominates the  $NO_x$  storage at low temperature zone in a very explicit way. The primary cause is little  $NO_2$  which is essential for nitrates formation produced from  $NO$  oxidation because  $NO$  oxidation reaction  $R13(NO(S) + O(S) \leftrightarrow NO_2(S) + Pt(S))$  is kinetically limited at low temperature, especially near 150 °C (with about maximum 0.025%  $Ba(NO_3)_2$  site fraction), which is in line with experimental results from Olsson L[28]. Note that the change of left scale of figure 15 (a) and (c) indicates that  $Ba(NO_3)_2$  site fraction doubled due to increasing temperature from 150 °C to 200 °C. Meanwhile  $BaO-NO_2$  site fraction increased with temperature increasing as well through comparison of  $BaO-NO_2$  site fraction under same EGR rate but different temperatures as showed in Figure 15 (b) and (d).

Because of negligible amounts of the  $Ba(NO_3)_2$  site fraction, the effects of EGR rate and temperature on the  $BaO-NO_2$  site fraction (nitrite route) are mainly discussed below. As showed in Figure 15 (b) and (d), the  $BaO-NO_2$  site fraction decreases with the increase of EGR rate at both 150 °C and 200 °C for the  $CO_2$  competitive adsorption reason as mentioned before. The increase of  $BaO-NO_2$  site fraction slows down as the EGR rate increase, which is more obvious at inlet temperature of 200 °C as showed in Figure 15 (d). This is because the consumption rate of  $Ba$  sites taken for initially appeared nitrites and negligible nitrates is stable over storage time because impacts of kinetically limitation of  $NO$  oxidation fade away with temperature increase within 150 °C ~200 °C, leading to reduction of  $NO$  and

corresponding nitrites. As showed in Figure 15 (d) when the EGR rate increases from 0% to 10% at 200°C, the BaO-NO<sub>2</sub> site fraction drops approximately 3.14% at 200 s. For EGR rate increases from 10% to 25% with increment 5%, the calculations of the variation degree are conducted at 200 s as well, and the corresponding decline of BaO-NO<sub>2</sub> site fraction is about 1.86%, 1.30%, 0.98%, respectively for different EGR rate intervals. So, the inhibition degree of EGR rate on nitrite route weakens with EGR rate increased at 200°C, because CO<sub>2</sub> adsorption competitiveness gradually reaches to saturation with incremental EGR rate.

#### 4.2.2 In moderate temperature zone

Figure 16 shows the variation trend of Ba(NO<sub>3</sub>)<sub>2</sub> and BaO-NO<sub>2</sub> site fraction over time under different EGR rate at moderate temperature zone (250°C~400°C).



**Fig. 16.** Ba(NO<sub>3</sub>)<sub>2</sub> site fraction and BaO-NO<sub>2</sub> site fraction under different EGR rate at moderate temperature.

With the increase of temperature from low temperature zone to moderate temperature zone, both of the Ba(NO<sub>3</sub>)<sub>2</sub> and BaO-NO<sub>2</sub> site fraction increases significantly, especially the Ba(NO<sub>3</sub>)<sub>2</sub> site fraction. Take 10% EGR rate as an example, the maximum Ba(NO<sub>3</sub>)<sub>2</sub> site fraction is about 40% as showed in Figure 11 (a) at 250°C. For the temperature of 300°C, 350°C and 400°C, the maximum Ba(NO<sub>3</sub>)<sub>2</sub> site fraction is about 95%, 70% and 25%, respectively. Visibly from Figure 16 (a)-(d) with temperature raises from 250°C to 400°C, the Ba(NO<sub>3</sub>)<sub>2</sub> site fraction increases first and declines later and BaO-NO<sub>2</sub> site fraction trend changed oppositely at moderate temperature zone which is major turning point for NO<sub>x</sub> storage pathway conversion and change. Furthermore, Ba(NO<sub>3</sub>)<sub>2</sub> site fraction increases by

24.06% under 10% EGR rate as showed in Figure 16 (b), in the adsorption phase (127~182 s). Meanwhile, BaO-NO<sub>2</sub> site fraction decreases by 13.95%. Ba(NO<sub>3</sub>)<sub>2</sub> can be obtained from both nitrate and nitrite routes as showed in Figure 2 (diagrammatic NO<sub>x</sub> storage routes). Therefore, at 300°C the probabilities of nitrate path and nitrite path were 10.11% and 13.95%, respectively. And at 350°C, the probabilities of nitrate path and nitrite path were about 10.01% and 13.77%. So, the two adsorption pathways have approximately equivalent contribution to NO<sub>x</sub> storage at 300°C and 350°C.

The cause of nitrate route participation raises first to reach same level of BaO-NO<sub>2</sub> site fraction and drops later is result of comprehensive effects of NO oxidation thermodynamic restriction, nitrate and nitrite thermostability and conversion between nitrites and nitrates. With temperature increasing from 250°C to 350°C, there is an interval between kinetically limitation vanished and thermodynamic restriction appeared during which NO<sub>2</sub> production from NO oxidation ( $R13 \text{ NO(S)} + \text{O(S)} \leftrightarrow \text{NO}_2\text{(S)} + \text{Pt(S)}$ ) is at the highest level, which is in accordance with study of Olsson L[28]. NO<sub>x</sub> disproportionation ( $\text{BaO} + 3\text{NO}_2 \leftrightarrow \text{Ba(NO}_2\text{)(NO}_3\text{)(3.1)} \ \& \ \text{Ba(NO}_2\text{)(NO}_3\text{)} + \text{NO}_2 \leftrightarrow \text{Ba(NO}_3\text{)}_2 + \text{NO(3.2)}$ ) is more and more important with temperature raised within the interval (250°C~350°C) leading to more nitrates formation. Hence nitrate route participation raises first from 250°C to 350°C based on above two primary reasons. The absolute amount of nitrates which can be seen through Ba(NO<sub>3</sub>)<sub>2</sub> site fraction value in figure 16 (b) and (c) was at very high level at 300°C and 350°C due to formation of barium nitrate species from nitrite species ( $\text{Ba(NO}_2\text{)}_2 + \text{O}_2 \leftrightarrow \text{Ba(NO}_3\text{)}_2$  (Equation5)) with Pt catalyzing is optimum in this temperature range (300°C~350°C) which is also reported by Forzatti P[29].

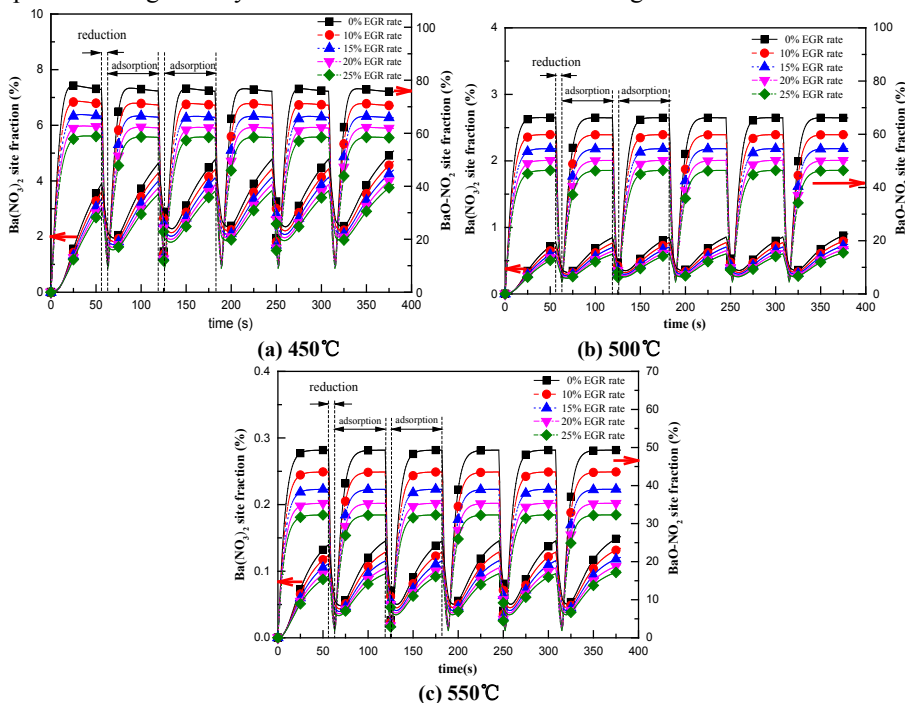
As the temperature subsequently raises to 400°C, reduction of nitrates generation from NO<sub>2</sub>( $\text{BaO} + 3 \text{NO}_2 \leftrightarrow 2 \text{Ba(NO}_3\text{)}_2 + \text{NO}$  (Equation3)) due to thermodynamics limitation of NO oxidation above 350°C and decline of stored nitrates due to thermal instability of nitrates at high temperature like 400°C result in decrease of Ba(NO<sub>3</sub>)<sub>2</sub> site fraction above 350°C of moderate temperature zone. Meanwhile the variation tendency of BaO-NO<sub>2</sub> site fraction is opposite to Ba(NO<sub>3</sub>)<sub>2</sub> site fraction variation for the reason of NO<sub>x</sub> storage sites (Ba sites) conservation and complementary correlation between nitrate and nitrite route mentioned before.

In additional, there are fluctuations of BaO-NO<sub>2</sub> site fraction during the switching between rich and lean condition as showed in partial enlarged detail highlighted in red circle of figure 16 (b). These fluctuations came from the change of equilibrium and rates of reactions ( $\text{BaO} + 3 \text{NO}_2 \leftrightarrow 2\text{Ba(NO}_3\text{)}_2 + \text{NO}$  (Equation3),  $\text{BaO} + 2\text{NO} + 0.5\text{O}_2 \leftrightarrow \text{Ba(NO}_2\text{)}_2$  (Equation4) and  $\text{Ba(NO}_2\text{)}_2 + \text{O}_2 \leftrightarrow \text{Ba(NO}_3\text{)}_2$  (Equation5)) which are affected greatly by local concentration of NO, NO<sub>2</sub> and O<sub>2</sub>. The rich-lean switch leads to changes in NO, NO<sub>2</sub> and O<sub>2</sub> local concentrations and the ratio of arbitrary two of these species.

#### 4.2.3 In high temperature zone

The variation tendency of Ba(NO<sub>3</sub>)<sub>2</sub> and BaO-NO<sub>2</sub> site fraction over time under different EGR rate at high temperature zone (450°C~550°C) is showed in Figure 17. taking notice of different scale of left and right Y axis in Figure 17 (a), (b) and (c). It can be clearly seen that Ba(NO<sub>3</sub>)<sub>2</sub> site fraction is no more than 5% whereas BaO-NO<sub>2</sub> site fraction maintained at a very high level, which indicates that nitrite route dominates again with temperature raises to high temperature zone as a result of the reduction of nitrates formation and nitrates pyrolysis at high temperature. As mentioned before, NO oxidation is thermodynamic limited above 350°C[28] resulting in reduction of formation of NO<sub>2</sub> which is crucial reactant for nitrates formation through  $\text{BaO} + 3 \text{NO}_2 \leftrightarrow 2 \text{Ba(NO}_3\text{)}_2 + \text{NO}$  (Equation3), leading to reduction of

nitrate formation. Meanwhile the degradation of thermal stability of nitrates results in reduction of stored nitrates through reaction R33 ( $\text{NO}_2 + \text{BaO}(\text{NO}_3) \leftrightarrow \text{Ba}(\text{NO}_3)_2$ ). In addition,  $\text{Ba}(\text{NO}_3)_2$  from nitrite route also decreases because last reaction step of nitrite route ( $\text{Ba}(\text{NO}_2)_2 + \text{O}_2 \leftrightarrow \text{Ba}(\text{NO}_3)_2$  (Equation 5)) is affected by thermodynamic limitation above  $350^\circ\text{C}$  [29]. As EGR rate increases from 0% to 25%, both of  $\text{Ba}(\text{NO}_3)_2$  and  $\text{BaO}-\text{NO}_2$  site fraction decreases in high temperature zone which is similar with tendency of low and moderate temperature zone except for the special circumstance of  $\text{Ba}(\text{NO}_3)_2$  site fraction under 0% EGR rate at  $150^\circ\text{C}$  and  $200^\circ\text{C}$  explained before. The decline degree of  $\text{Ba}(\text{NO}_3)_2$  and  $\text{BaO}-\text{NO}_2$  site fraction decreases with EGR rate increasing, because  $\text{CO}_2$  adsorption competitiveness gradually reaches to saturation with increasing EGR rate.



**Fig. 17.**  $\text{Ba}(\text{NO}_3)_2$  site fraction and  $\text{BaO}-\text{NO}_2$  site fraction under different EGR rate at high temperature.

## 5 Conclusion

A LNT model coupled with EGR was developed based on the Langmuir–Hinshelwood mechanism to investigate the EGR effects on  $\text{NO}_x$  adsorption pathway of LNT catalysts with temperature changed in range  $150^\circ\text{C}\sim 550^\circ\text{C}$ . Both the nitrate and nitrite adsorption paths were considered for the  $\text{NO}_x$  storage process in the model as well as the spillover of stored  $\text{NO}_x$  between Ba and Pt sites. The model quantified the contributions of both nitrate route and nitrite route to the  $\text{NO}_x$  storage capacity for LNT with change of EGR rate (0%~30%) at fixed temperature under raw emission atmosphere from tested gasoline engine.

At fixed inlet temperature of  $350^\circ\text{C}$  set for high  $\text{NO}_x$  conversion efficiency, EGR rate shows restraining effects on  $\text{Ba}(\text{NO}_3)_2$  site fraction within range of 0%~30% whereas promotion effects on  $\text{BaO}-\text{NO}_2$  site fraction from 0% to 15% and inhibition effects in subsequent EGR rate 20%~30%. There is opposite tendency between  $\text{Ba}(\text{NO}_3)_2$  site fraction  $\text{BaO}-\text{NO}_2$  site fraction over time in the same cycle of operation due to the complementary

correlation between nitrate route and nitrite route. Furthermore, the similar trends of site fraction assorted in EGR rate interval 0%~15% were different from the similar trends of site fraction which were assorted in EGR rate interval 20%~30% for both Ba(NO<sub>3</sub>)<sub>2</sub> site fraction and BaO-NO<sub>2</sub> site fraction due to the equilibrium limitations of the reaction about CO<sub>2</sub> was chemisorbed on the BaO sites which are supposed to be occupied by NO<sub>x</sub>. As for contributions of the two routes to NO<sub>x</sub> storage, in the range of 0% ~ 20% EGR rate, the ratio of nitrate route to nitrite route dropped while raised in the 20% ~ 30% EGR rate, the ratio is decided by nitrite route to a great extent due to slight variation of occupation of Ba sites by nitrate route due to great cardinal number of NO amounts from raw engine emission, thermodynamics limitation of NO<sub>x</sub> oxidation and in part thermal decomposition of stored Ba(NO<sub>3</sub>)<sub>2</sub> at temperature of 350°C. The process of CO<sub>2</sub> (which is major component of inlet stream in presence of EGR) competitive adsorption dynamic changed with the ratio of CO<sub>2</sub> concentration and available NO<sub>x</sub> storage sites left.

When LNT catalyst temperature varies from 150°C to 550°C, there are new changes of NO<sub>x</sub> storage process under different EGR rate. Nitrite route dominates at low temperature zone (150°C~200°C) because there are little NO<sub>2</sub> which is essential for nitrate route from NO oxidation kinetically limited at low temperature, especially near 150°C. With the increase of temperature from low temperature zone to moderate temperature zone (250°C~400°C), both of the Ba(NO<sub>3</sub>)<sub>2</sub> and BaO-NO<sub>2</sub> site fraction increases significantly, especially the Ba(NO<sub>3</sub>)<sub>2</sub> site fraction which has a 4magnitude equal to BaO-NO<sub>2</sub> site fraction. The cause of nitrate route participation raises first to reach same level of BaO-NO<sub>2</sub> site fraction and drops later is result of comprehensive effects of NO oxidation thermodynamic restriction, nitrate and nitrite thermostability and conversion between nitrites and nitrates. Nitrite route dominates again with temperature raises to high temperature zone (450°C~550°C) as a result of the reduction of nitrates formation (NO oxidation was thermodynamic limited above 350°C) and the pyrolysis of nitrates at high temperature. As EGR rate increases from 0% to 25%, both of Ba(NO<sub>3</sub>)<sub>2</sub> and BaO-NO<sub>2</sub> site fraction decreases in high temperature zone which is similar with tendency of low and moderate temperature zone except for the special circumstance of Ba(NO<sub>3</sub>)<sub>2</sub> site fraction under 0% EGR rate at 150°C and 200°C because oxygen atoms adsorption on Pt sites was blocked by adsorbed H<sub>2</sub>O on Pt sites at low temperature which retarded NO oxidation resulting in reduction of nitrates produced by NO<sub>x</sub> disproportionation (Equation 3.1 and 3.2) and reaction involving the formation of barium peroxide (Equation 3.3 and 3.4).

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