Influence of the initial hydrostatic pressure on contact area coefficient under drainage condition

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Abstract. The expression of effective stress proposed by Terzaghi has always been questioned. Many correction formulas are modification of pore pressure term. The pore pressure factor is related to porosity, contact area and other factors. When the particles are in point contact, the expression of the effective stress is that proposed by Terzaghi, while for the surface contact particles, the actual effective stress increases the stress produced by pore pressure passing through the contact surface based on the Terzaghi effective stress. There are many factors that affect the development of contact area and pore pressure, therefore, a series of the drained triaxial tests were carried out on four groups of sand samples with different initial hydrostatic pressures to study the influence of different initial hydrostatic pressures on the effective stress due to the term of contact area (σ_{α}). The test results show that the shear strength is increases with the initial hydrostatic pressure under the same effective confining pressure, which indirectly indicates that the initial hydrostatic pressure increases the contact area stress.

1 Introduction

Terzaghi effective stress principle has been controversial since it was proposed, especially the approximate calculation of effective stress. Many researchers have put forward different effective stress expressions from different aspects. The modifications are mainly for the pore pressure term and these expressions can be written in the form of equation (1), where σ' is the effective stress, σ is the totle stress, p is the pore pressure, and η is the pore pressure factor. In the calculation expression of Terzaghi effective stress $\eta = 1$, other expressions for η are shown in the table 1.

$$\sigma' = \sigma - \eta p \tag{1}$$

It was pointed out by Du et.al.^[17] that the effective stress is the link between the measurable load effects such as the strength and deformation and external load. In addition, the concepts of strength related effective stress and deformation related effective stress were proposed, and the expressions of effective stress related to strength and deformation were derived respectively. It was regarded that in the expression of strength related effective stress, the pore pressure factor is related to the particle contact coefficient and the expression is given as following:

$$\sigma' = \sigma - (1 - \alpha)p = \sigma - p + \alpha_c (1 - n)p$$
(2)

Where, α_c is the ratio of contact area on the section, *n* is the porosity of saturated soil. When the contact area of

Table 1.	Expressions	for pore	pressure	factor η (According to
		the liter	rature ^[1-3])	

η	Researchers			
1	Terzaghi ^[4, 5] , Skempton ^[6] , Oka ^[7] , Li ^[8, 9] , Shao ^[10] , Lu ^[11]			
п	Biot ^[12]			
$n \le \eta \le 1$	Schiffman ^[13]			
1-α	Skempton ^[6,14] , Bishop ^[15] , Cao ^[16] , Du ^[17]			
1- <i>C</i> _s / <i>C</i> or 1- <i>K</i> / <i>K</i> _s	Boer ^[1] , Biot ^[18,19] , Chen ^[20] , Bishop ^[21] , Zhang ^[22]			
1-αtanψ/tanφ'	Skempton ^[6]			
$\frac{1-(1-n)C_{\rm s}/C [C_{\rm b}-C_{\rm s}+n(C-C_{\rm s})]/(C_{\rm b}-C_{\rm s})}{C_{\rm s}+n(C-C_{\rm s})]/(C_{\rm b}-C_{\rm s})}$	Boer ^[1] , Oka ^[7] , Suklje ^[23]			
Note: <i>n</i> is porosity of the saturated soil, α is Contact area coefficient, Cs is the compressibility of soil particles, C is the compressibility of soil skeleton, ψ is the inherent friction angle of material and ϕ' is the effective friction angle of fluid-saturated porous media.				

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particles is 0, in other word, it is point contact mode between soil particles, equation (2) is the calculation formula of Terzaghi effective stress. When the contact mode between particles is surface contact, the effective stress is composed of two parts: the effective stress proposed by Terzaghi and the effective stress term produced by pore pressure acting on the contact surface.

Strictly speaking, the contact area is influenced by the initial hydrostatic pressure (σ_0), effective consolidation pressure, porosity and overconsolidation ratio, etc. The larger the initial hydrostatic pressure and consolidation pressure are, the larger the particle contact area is, and the larger the contact area is, the smaller the area of pore pressure acting on soil particles is, when the porosity of saturated soil remains constant. For general geotechnical engineering, because the contact area coefficient is very small, its influence can be ignored. However, for the deep-sea geotechnical engineering, the influence of contact area can not be ignored and more research is needed.

However, the effect of αp on effective stress and strength is very complex. On the one hand, there are many factors affecting the contact area, and there should be some functional relationship (linear or nonlinear) between the contact area coefficient and the initial hydrostatic pressure and other factors, that is, $\alpha = \alpha(\sigma_0, \sigma'...)$. On the other hand, there are many factors influencing the development mode of pore water pressure, such as pore water pressure ratio, site boundary conditions and so on. Especially, when the dynamic characteristics of saturated sand are studied in laboratory tests, the back pressure method is used to saturate the sand samples. In fact, the back pressure represents the initial hydrostatic pressure of the saturated soil layer in the site. It is generally believed that the back pressure has no effect on the liquefaction characteristics of saturated soil, so it is not specified in the standard for geotechnical test methods. However, some researchers^[24] found that the initial hydrostatic pressure has a great influence on the development of pore pressure and the shear strength of saturated sand under undrained conditions. The effective stress calculation formula should consider the factors affecting α , because of the complexity of the contact area and pore pressure. Thus it is more rigorous to rewrite the equation (2) as following:

$$\sigma' = \sigma - p + \sigma_{\alpha} \tag{3}$$

Where, σ_{α} is the effective stress term related with the contact area, porosity and the pore pressure, in addition, it is a simple expression after considering their influence factors.

There are many factors that have influence on σ_{α} , however, there is still a lack of research on them, and it is also very difficult to measure α_c and to quantitatively analyze the influence of various factors on the contact area coefficient. As is known to all, under drainge conditions, there is no pore pressure produced, thus, the initial hydrostatic pressure will not affect the shear strength of saturated soil by affecting the development of pore pressure. However, according to the above analysis and equation (3), the initial hydrostatic pressure will affect the shear strength by affecting σ_{α} , In this paper, drained triaxial test under different consolidation pressure and different initial hydrostatic pressure were carried out. By analyzing the shear strength under different conditions, the influence of initial hydrostatic pressure on σ_{α} is qualitatively analyzed.

2 Test and result analysis

2.1. Sample preparation and test design

The back pressure saturation, isotropic consolidation and effective stress strength properties are well controlled and measured using GDS triaxial apparatus system. It provided automatic control of the applied cell- and backpressures to an accuracy of 1 kPa, along with measurement of the specimen volume change response to an accuracy of 10-3 ml. Figure (1) shows a typical sample of the conventional triaxial test. The major and minor principal stresses are denoted as σ_1 ' and σ_3 ', respectively. The relationship among them are $\sigma_1' > \sigma_3' =$ σ_2 '. The Fujian standard sand is used. In order to avoid the impact of particle breakage on the mechanical properties of the sand, the sample is only used once in the test and is not reused. In the process of sample loading, the diameter and height of the samples will be strictly controlled. The diameter and height of all samples are well controlled to be 50.8 mm and 106.5 mm, and the mass of wet sand in saturated sample is 456.6g with the precision of ± 0.02 g.



Fig.1. The stress condition of sample in conventional triaxial test.

The consolidation drainage test (CD) is used and in the process of saturation, axial loading was conducted at an axial strain rate of 0.1 mm/min under a drained condition, allowing excess pore water pressures to dissipate in theory, and the back pressure is controlled to reach the predetermined value, and remains constant in the consolidation and loading stages. The B value of all samples is above 98%, which satisfies the requirement of saturation. The test conditions are shown in table 2.

 Table 2. Samples conditions in conventional triaxial tests of saturated sands.

σ_3 '	Test No.	σ_0 (kPa)	Test type
100	1	300	CD
100	2	500	CD

	3	700	CD
	4	900	CD
	5	300	CD
200	6	500	CD
200	7	700	CD
	8	900	CD
	9	300	CD
200	10	500	CD
300	11	700	CD
	12	900	CD
	13	300	CD
400	14	500	CD
	15	700	CD

2.2 Test results and analysis

In the conventional triaxial compression test, the generalized shear stress is $q = \sigma_1 - \sigma_3$. The relationships between the the generalized shear stress and axial strain under different initial hydrostatic pressures and effective confining pressures are given in figure 2. It should be noted that, when the effective confining pressure (σ_3) is 400kPa and the back pressure (σ_0) is 900kpa, the test instrument reaches the maximum range, thus the results can not be obtained.

If there exist peak point in stress-strain relationship, the failure is thought to occur at the peak value of deviator stress. When the stress-strain relationship has no peak value, the failure takes place at strain of $15\%^{[25]}$. According to the figure 2, the drained shear strength is taken as the deviator stress at the maximum value. It can be seen from the figure 2 that the shear strength of soil is increasing with effective confining pressures. Under the same effective confining pressure, the shear strength of soil is increasing with the initial hydrostatic pressure. Taking the effective confining pressure of 100kPa as an example, when the initial hydrostatic pressure is 300kPa, the maximum shear strength is 280kPa and when the initial hydrostatic pressure to 900 kPa, the maximum shear strength is about 310 kPa.





Fig.2. CD test results under four different confining pressures.

The shear strength of specimens under different initial hydrostatic pressure and consolidation pressure is depicted in figure 3. Although the influence of initial hydrostatic pressure on shear strength is small, the four groups of test data have a unified rule, which can eliminate the possibility of test error. It can be concluded that under the same consolidation pressure and porosity, the effect of initial static shear strength of sand.



Fig.3. Effect of different initial hydrostatic pressure on drained shear strength of soil

3 Conclusion

In this paper, the effective stress term caused by contact area is discussed αp , which is directly related to the contact area coefficient and pore pressure. The contact area coefficient is directly related to the contact area ratio and porosity, and the factors that affect the contact area ratio and porosity also directly affect the contact area coefficient; In addition, the factors that affect the development of pore water pressure also directly affect the development of pore water pressure αp . Due to the complexity of the above factors, this paper simplifies the term to σ_a . The influence of initial hydrostatic pressure on shear strength of saturated sand is obtained by triaxial drainage test, which is verified by lateral test σ_{α} The effect of term on shear strength. Under the condition of drainage, the influence of initial hydrostatic pressure on shear strength is small, but it still presents regularity, that is, the greater the initial hydrostatic pressure is, the stronger the shear strength is.

The influence of initial hydrostatic pressure on the shear strength of sand under drainage condition is studied in this paper, and the results indirectly show that σ_{α} should be considered in the calculation of effective stress, and the initial hydrostatic pressure theoretically has an influence on the contact area of particles. Therefore, the tests also give the influence law of initial hydrostatic pressure on σ_{α} . However, a lot of researches are needed to verify the equation (3). In this paper only a feasible research method are provided. In addition, further researches are needed to study the influencing factors of contact area, so as to adapt to the development trend of ultra-deep engineering.

Acknowledgments

This research was supported by National Natural Science Foundation of China (51722801). The supports from the above organizations are gratefully acknowledged.

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