# Econometric modeling and forecasting the development of the postal service in Uzbekistan 

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#### Abstract

This article is devoted to econometric modeling and forecasting of development of postal services in Uzbekistan. As a result of digitization and optimization of postal services using the VAR and ARDL models with 2SLS, the number of post offices, the number of postmen closely associated with it, has been shown to decrease.


## 1 Introduction

Any research on the strategic development of an enterprise is based on econometric modeling. Therefore, a lot of research in this area has been done in foreign and domestic scientific work.
D.W.Caves [1] proved that postal services are associated with transportation costs based on econometric models. In world practice, it has been found that the development of transport, especially air transport, has a high impact on the development of postal services.

In 2005, B.A.Graf, then vice president of FedEx, one of the world's largest postal services gigs. The article notes that the most important factors for postal services are speed and accuracy. This requires that postal services be digitized in an optimized way at a time when information is rapidly evolving [2].

## 2 Methods

VAR and ARDL models in the research process,2SLS model, Dickey-Fuller (DF) test,ADF test,trend method, grinding method, STATA program and others were used.

## 3 Results and Discussion

During our study, VAR and ARDL models with 2 SLS We will optimize the number of suppliers of postal services by modeling the strategic activities of postal services of

[^0]Uzbekistan.
In our study we use the following model:

$$
\begin{equation*}
y=\alpha_{0} x_{1}^{\alpha_{1}} x_{2}^{\alpha_{2}} \tag{1}
\end{equation*}
$$

If we logarithmize both sides of this equation, the equation looks like this:

$$
\begin{equation*}
\ln y=\ln \alpha_{0}+\alpha_{1} \ln x_{1}+\alpha_{2} \ln x_{2} \tag{2}
\end{equation*}
$$

We hypothesize that the number of post offices depends on the number of postmen delivering mail, and the number of postmen depends on the required postal services, and that their change is linked from year to year, not from year to year. This concept is defined by the lag in econometrics, i.e., the calculation of changes in the previous year's step. The correlation represents the need to apply the VAR model . VAR (vector auto regression) model, which also includes lags of the resulting sign. The ARDL model (autoregressive distributed lag) is a model in which factor lags are also involved.
According to our hypothesis, there are two equations, the first equation is the relationship between the number of parcels ( $\mathrm{y}_{1}$ ) and the number of couriers ( $\mathrm{y}_{2}$ ) based on the VAR model, the second equation depends on the number of couriers ( $\mathrm{y}_{2}$ ) and the demand for postal services. The ARDL model is created. The first equation is generated using the second equation regression results, which represents the 2 SLS model in econometrics. Thus, based on our hypothesis, the following system of equations is formed:

$$
\left\{\begin{array}{c}
\ln y_{1}=\beta_{0}+\beta_{1} \sum_{i=1}^{n} \ln \hat{y}_{1 t i}+\beta_{2} \sum_{i=1}^{n} \ln \hat{y}_{2 t i}+\varepsilon  \tag{3}\\
\ln y_{2}=\alpha_{0}+\alpha_{1} \sum_{i=1}^{n} \ln \hat{y}_{2 t i}+\alpha_{2} \sum_{i=1}^{n} x_{t i}
\end{array}\right.
$$

In the model we can identify the outcome and factor characters involved.

Table 1. Information on the variables involved in the study

| № | Name of indicators | Unity | Variables | Status in the model |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Number of delivery <br> points for postal <br> services | s | The resulting <br> character | Y 1 |
| 2 | Including in rural <br> areas | s | Factor character | X 1 |
| 3 | Number of postmen <br> delivering mail | person | The resulting <br> character | Y 2 |
| 4 | Shipments | Thousands | Factor character | X 2 |
| 5 | Letters, envelopes, <br> cards | millions | Factor character | X 3 |
| 6 | Newspapers and <br> magazines | millions | Factor character | X 4 |
| 7 | Money transfers | Thousands | Factor character | X 5 |
| 8 | Pension payments | millions | Factor character | X 6 |
| 9 | Telegrams | Thousands | Factor character | X 7 |
| 10 | Mail sent by air | tons | Factor character | X 8 |

We begin our study by examining the indicators for stationary. In the scientific literature, nonstationary periodic series are also referred to as "integrated processes". The degree of integration of a series is determined by how many times it needs to be differentiated to make it stationary. Thus, stationary rows are "zero-degree integrated" and are abbreviated as I (0). Once a series becomes stationary after differentiation, it is called first-order
integrated and is denoted by I (1). In general, periodicseries dif stationary after times differentiated, dis called degree integrated and is denoted as I (d).

In this case, $\mathrm{Y}_{\mathrm{t}}$ and $\mathrm{X}_{\mathrm{t}}-\mathrm{I}(1)$ level integrated, $\varepsilon_{1 \mathrm{e}}$ ва $\varepsilon_{1 \mathrm{e}}$ is independent and averaged " 0 " and is uniformly distributed with constant variance. Also, the value of at least $\alpha_{1}$ ва $\alpha_{2}$ one of the coefficients must be different from zero. Both equations are balanced because both sides of the equation are equally integrated. Agar, $Y_{t}=v+\beta x_{t}$ if the equation $\mathrm{Y}_{\mathrm{t}}$ and $\mathrm{X}_{\mathrm{t}}$ determine the long-term relationship between the variables, $\left(Y_{t-1}-v+\beta x_{t}\right)$ the degree of deviation from the equilibrium position, $\alpha_{1}$ ва $\alpha_{2}$ and the coefficients reflect the power of the economic system to strive for equilibrium.

Because cointegration link verification requires a degree of integration of variables, the degree of integration is determined for each variable before cointegration tests. The DickeyFuller (DF) test is used for this [3, 4-10]. This test was developed by Dickey and Fuller, is based on equation (4) and is called the "Unit Root Test":

$$
\begin{equation*}
\Delta L n y_{t}=\delta L n y_{t-1}+u_{t} \tag{4}
\end{equation*}
$$

or

$$
\begin{equation*}
L n y_{t}=(1+\delta) L n y_{t-1}+u_{t} \tag{5}
\end{equation*}
$$

In general checking of indicators for stationary is carried out in three ways. The graph method is autocorrelation correlogram and ADF test.
study, the STATA program was selected and all work was carried out in this program. First, graphs and integrated cases of the resulting symbols were formed.


Fig. 1. The resulting character change dynamics
As can be seen from Fig. 1. $y_{1}$ and $y_{2}$ are non-stationary, in particular, the number of sections and postmen providing postal services tends to decrease, did not become stationary in the first integrated state, and in our opinion there is stationary in the second-order integrated indicators.

We check this condition by means of a korelagram, if in the korelogram all the lags are located in the confidence interval, a strong stationary is represented.


Fig. 2. Chorelogram of the resulting characters
Figure 2 clearly shows the presence of stationary in the second-order integrated case.
Table 2. ADF test results

| Variable | ADF <br> statistics | Critical <br> values $10 \%$ | Probably | Decision |
| :---: | :---: | :---: | :---: | :---: |
| Y1 | 0.615 | -2.630 | 0.98 | Unitrootavailablenot |
| Y2 | 0.502 | -2.630 | 0.98 | Unitrootavailablenot |
| Variabledegree <br> difference | ADF <br> statistics | Critical <br> values $10 \%$ | Probably | Decision |
| Dy1 | -1.90 | -2.630 | 0.32 | Unitrootavailablenot |
| Dy2 | -2.331 | -2.630 | 0.16 | Unitrootavailablenot |
| D2y1 | -3.433 | -2.630 | 0.0099 | Unitrootavailable |
| D2y2 | -4.449 | -2.630 | 0.0002 | Unitrootavailable |

2 show that the hypothesis "there is no unit root" for all variables was rejected in the $1 \%$, $5 \%$, and $10 \%$ confidence ranges. As a logical continuation of the analysis, the hypothesis that the variables have a "secondary root" was tested, and it was concluded that all three variables were level 1 integrated.
If all indicators are non-stationary and become stationary after first-order integration, then the VAR and ARDL models are selected by selecting an alternative lag.
STATA program, we have developed more than 30 models, in which $\mathrm{x} 4, \mathrm{x} 5, \mathrm{x} 6, \mathrm{x} 7$, x 8 have been found to have a strong impact on optimizing the number of post offices, digitization and optimizing the number of postmen. All model results are presented in the appendix, using the ARDL method in selecting the most optimal model we used.
reg lny2 lag2lnx2 laglnx3


Fig. 3. Optimal model results
This is optimal the model includes factor x 2 and x 3 factor characters. The model looks like this:

$$
\begin{equation*}
\ln y_{2}=-0.94 L .3 \ln x_{2}-1.2 L \cdot \ln x_{3}+15.05 \tag{6}
\end{equation*}
$$

Proves that the number of postmen can be reduced by $1.2 \%$ after one year.
Based on our hypothesis, we relate the regression results of this model to the number of parcels delivering mail, i.e., we use the 2SLS model.

```
. reg lny1 laglny1 lny2fit
```

| Source | SS | df | MS | Number of obs | $=$ | 19 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\mathrm{F}(2,16)$ | = | 139.17 |
| Model | 1.01761233 | 2 | . 508806164 | Prob > F | $=$ | 0.0000 |
| Residual | . 058495144 | 16 | .003655946 | R -squared | $=$ | 0.9456 |
|  |  |  |  | Adj R-squared | = | 0.9388 |
| Total | 1.07610747 | 18 | . 059783748 | Root MSE | $=$ | . 06046 |


| lny1 | Coef. | Std. Err. | t | P>\|t| | $[95 \%$ Conf. Interval] |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| laglny1 | .9512949 | .0741156 | 12.84 | 0.000 | .7941769 | 1.108413 |
| lny2fit | .1438155 | .0614447 | 2.34 | 0.033 | .0135584 | .2740725 |
| _cons | -.81916 | .5764469 | -1.42 | 0.174 | -2.041173 | .4028529 |

Fig. 4.Optimal model results

$$
\begin{equation*}
\ln y_{1}=0.95 L \cdot \ln y_{1}+1.4 \ln \hat{y}_{2}-0.81 \tag{7}
\end{equation*}
$$

According to the model, a $1 \%$ increase in the number of postmen would lead to a $1.4 \%$ increase in the number of parcels. Both models were validated based on $t$-test, F-test, and Akayke Schwartz criteria. Our study, based on our hypothesis, is fully modeled:

$$
\begin{align*}
& \ln y_{2}=-0.94 L .3 \ln x_{2}-1.2 L \cdot \ln x_{3}+15.05  \tag{8}\\
& \ln y_{1}=0.95 L \cdot \ln y_{1}+1.4 \ln \hat{y}_{2}-0.81 \tag{9}
\end{align*}
$$

Based on these models, we determine the forecast values for 2022-2026 years. In general, several forecasting methods are used in time series. There are MAPE, MAD, and MSD indicators that represent error quality in determining the optimal type of forecasting methods. These indicators measure the error between the values of the forecasting methods and the data provided. MAPE to the results of the forecasting method is the average of the sum:

$$
\begin{equation*}
M A P E=\frac{\sum \frac{\left|e_{t}\right|}{Y_{t}}}{n} \tag{10}
\end{equation*}
$$

MAD represents the average of absolute errors:

$$
\begin{equation*}
M A D=\frac{\sum\left|e_{t}\right|}{n} \tag{11}
\end{equation*}
$$

MSD absolute errorssquares represents the average:

$$
\begin{equation*}
M A D=\frac{\Sigma\left|e_{t}^{2}\right|}{n} \tag{12}
\end{equation*}
$$

In the forecasting methods used, the method with the lowest results, which explains their reliability, is the most optimal forecasting method, and the forecast indicators calculated on the basis of this optimal method are more accurate.

For our study, we use three trend methods and one grinding method to determine the forecast values. The main reason for this is that the indicators are non-stationary and there is a trend factor in their change. Of the trend methods, linear, quadratic, and exponential are acceptable. Holt Winter seasonal, one of the grinding methods, covers the trend, seasonality and level of grinding, which means that this method is one of the advantages.

Grinding methods are determined on the basis of levels, the degree is from 0 to 1 . Three types of grinding are widely used in scientific research, including exponential grinding, Double exponential grinding, and Holt Winter seasonal grinding. Only in the exponential grinding method $\alpha$ determines the degree of grinding of the method, this method is characterized as follows:

$$
\begin{equation*}
\hat{x}=\alpha x_{t}+\alpha(1-\alpha) x_{t-1}+\alpha(1-\alpha)^{2} x_{t-2}+. . \tag{12}
\end{equation*}
$$

Double exponential grinding, Holt Winter seasonal grinding types are represented in the same way.
Equation (13) with ( $t-1$ ) and multiplying both sides by $(1-\alpha)$ gives the following equation:

$$
\begin{equation*}
(1-\alpha) x_{t-1}=\alpha(1-\alpha) x_{t-1}+\alpha(1-\alpha)^{2} x_{t-2}+\alpha(1-\alpha)^{3} x_{t-3}+. . \tag{14}
\end{equation*}
$$

By equating the thirteenth equation from Equation (14), we obtain the following equation:

$$
\begin{equation*}
\widehat{x_{t}}=\left(1 \widehat{-\alpha)} x_{t-1}+\alpha x_{t} 0 \ll \alpha_{1}\right. \tag{15}
\end{equation*}
$$

This equation is the final equation of exponential grinding and is the $\widehat{x_{t}}$ actual level of the forecast values.$x_{t}$ Given that factor x 2 and x 3 are involved in our model, we first analyze these indicators.

Table 3. O mil characters prognoz methods
$\left.\begin{array}{|c|c|c|c|c|}\hline № & \text { Types of forecast models } & \text { MAPE } & \text { MAD } & \text { MSD } \\ \hline & 1 & 2 & 3 & 4 \\ \hline 1 & \mathrm{X} 2=65.3019+1.37169 * \mathrm{t} & 18.85 & 13.84 & 220.73 \\ \hline 2 & \mathrm{X} 2=52.4866+4.71481 * \mathrm{t}-0.151960 * \mathrm{t} * * 2 & 16.91 & 12.22 & 196.06 \\ \hline 3 & \mathrm{X} 2=101.594+0.0301456^{*} \mathrm{t}-0.00118726^{*} \mathrm{t} * 2 \\ \hline 4 & \begin{array}{c}\text { Smoothing ConstantsAlpha (level) } 0.6 \\ \text { Gamma (trend) } 0.2 \text { Delta (seasonal) } 0.2\end{array} & 18.83 & 14.61 & 228.18 \\ \hline 5 & \mathrm{X} \mathrm{3} \mathrm{=} \mathrm{12.6267} \mathrm{+} \mathrm{0.163377} \mathrm{t}\end{array}\right)$

Holt Winter grinding method was found to be the most optimal method for forecasting for both factor marking because MAPE, MAD, MSD quality indicators representing forecast errors achieved less results than other models. We can also check this condition on a graphical basis.


Fig. 5. Appearance of model factor symbols based on the Holt Winter grinding method
Another advantage of the Holt Winter grinding method is that it is possible to determine both pessimistic and optimistic forecast values through this forecast. This means that the effects of the current pandemic have been taken into account. We know that under the influence of the pandemic, postal services will expand.

Table 4. O mil characters prognoz values

| № | Years | Forecast | Optimistic | Pessimistic |
| :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 |
|  | X2 for factor character |  |  |  |
| 1 | 2022 y | 72.2673 | 99.509 | 45.0252 |
| 2 | 2023 y | 66.6677 | 97.939 | 35.3968 |
| 3 | 2024 y | 66.3795 | 102.544 | 30.2146 |
| 4 | 2025 y | 60.7799 | 102.400 | 19.1599 |
| 5 | 2026 y | 60.4917 | 107.935 | 13.0486 |
|  | X2 for factor character |  |  |  |
| 6 | 2022 y | 14.6203 | 16.6626 | 12.5781 |
| 7 | 2023 y | 14.2264 | 16.5707 | 11.8822 |
| 8 | 2024 y | 14.4137 | 17.1248 | 11.7025 |
| 9 | 2025 y | 14.0197 | 17.1398 | 10.8996 |
| 10 | 2026 y | 14.2070 | 17.7636 | 10.6504 |

## 4 Conclusions

Based on our research, it has been established that shipments in 2022 may amount to 72.26 thousand units, and according to an optimistic theory, they can amount to 99.50 thousand units. By 2026, this figure, according to an optimistic theory, could reach 108,000 , which is 34,000 more than now.
Letters, envelopes and postcards will reach 14.6 million in 2022, and according to the optimistic theory, 16.66 million. By 2026, this figure, according to the optimistic theory, will reach 17.76 million. This means an increase of 3.76 million more than at present time. Based on these indicators, in our model, developed on the basis of improved VAR and ARDL methods of 2SLS methods, we develop forecast figures for the number of post offices and the number of postmen for 2022-2026.

Table 5. Forecasts of postal services of Uzbekistan for 2022-2026

| oo | Years | Forecast | Optimistic | Pessimistic |
| :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 |
|  | Change in the number of postmen |  |  |  |
| 1 | 2022 y | 1681.33 | 2404.93 | 957,722 |
| 2 | 2023 y | 1337.40 | 2168,01 | 506,784 |
| 3 | 2024 y | 1026.38 | 1986,99 | 65,768 |
| 4 | 2025 y | 682.45 | 1787.96 | 423,056 |
| 5 | 2026 y | 571.43 | 1631.61 | 388,749 |
|  | Number of post offices |  |  |  |
| 6 | 2022 y | 3244,26 | 3829.08 | 2659,44 |
| 7 | 2023 y | 2978.51 | 3649.82 | 2307.21 |
| 8 | 2024 y | 2684.69 | 3461.06 | 1908.32 |
| 9 | 2025 y | 2418.95 | 3312,42 | 1525.47 |
| 10 | 2026 y | 2125,12 | 3143.61 | 1106.64 |

For the next five years, there will be a downward trend in the number of post offices and postal services, by 2026 the number of postmen will be 572, while the number of post offices will be 2125 .
Based on our model, the need for digitization and optimization of all postal services has been proven.

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